9.3 Static and fatigue criteria

Name: _____ Class: _____ Date: _____ **Total: 13 marks**

KEY WORDS fatigue • S-N curve S-N • endurance limit • Marin factors • Goodman line

Objective

Correct a test-bar endurance limit for a real part, read strength from the S-N line, and check a shaft against fatigue with the Goodman line and against first-cycle yield.

1 Key knowledge and worked examples

■ **From test bar to real part**

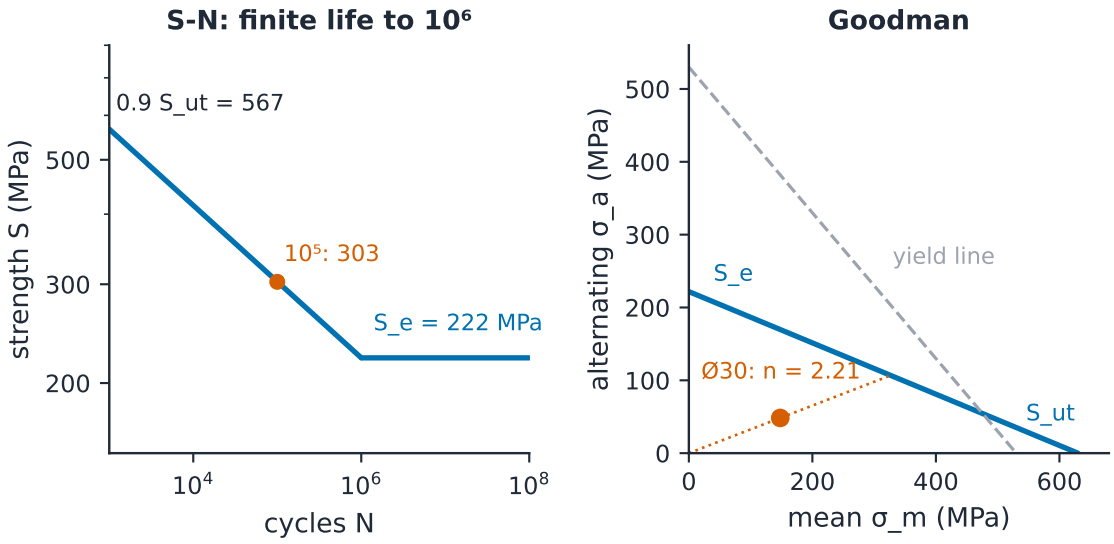
- **Fatigue** : steel's **S-N curve** S-N flattens at the **endurance limit** , $S'_e = 0.5S_{ut}$ (up to 1400 MPa).
- **Marin factors** : $S_e = k_a k_b S'_e$, machined $k_a = 4.51 S_{ut}^{-0.265}$, size $k_b = 1.24 d^{-0.107}$ (2.79 to 51 mm).
- S-N line from $0.9S_{ut}$ at 10^3 to S_e at 10^6 cycles.
- **Goodman line** : $1/n = \sigma_a/S_e + \sigma_m/S_{ut}$; yield: $n_y = S_y/(\sigma_a + \sigma_m)$ by von Mises.

■ **Worked example. The 30 mm shaft**

C45: $S_{ut} = 630$ MPa, $S_y = 530$ MPa, machined, $d = 30$ mm.

- $k_a = 4.51 \times 630^{-0.265} = 0.817$; $k_b = 1.24 \times 30^{-0.107} = 0.862$.
- $S_e = k_a k_b S'_e = 0.817 \times 0.862 \times 315 =$ **222** MPa.
- With $\sigma_a = 48.4$ and $\sigma_m = 148.0$ MPa: $1/n = 48.4/222 + 148.0/630$, so $n =$ **2.21**; yield $n_y = 530/\sqrt{48.4^2 + 148.0^2} = 3.40$. Fatigue governs.

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2 Practice

C45 steel, $S_{ut} = 630$ MPa, $S_y = 530$ MPa, machined finish.

2.1 Find k_a, k_b and S_e for a 40 mm shaft (three decimals, three decimals, nearest MPa). [4]

2.2 Using that S_e, find the fully reversed strength at 10^4 cycles from the S-N line (nearest MPa). [3]

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3 Exam-style questions

3.1 At its shoulder the 40 mm shaft carries $\sigma_a = 60$ MPa (bending, K_f included) and a von Mises mean $\sigma_m = 120$ MPa. Find the Goodman factor of safety and the first-cycle yield factor of safety (two decimals). Which governs, and what would you change first to raise it? [6]

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