12.4 Feedback and PID control

Name: _____ Class: _____ Date: _____ **Total: 14 marks**

KEY WORDS error • PID controller PID • rate limit • integrator windup • anti-windup

Objective

Find the steady error a load leaves under proportional control, add integral action to remove it, and see how actuator saturation causes integrator windup.

1 Key knowledge and worked examples

■ P, I and D, and the limits

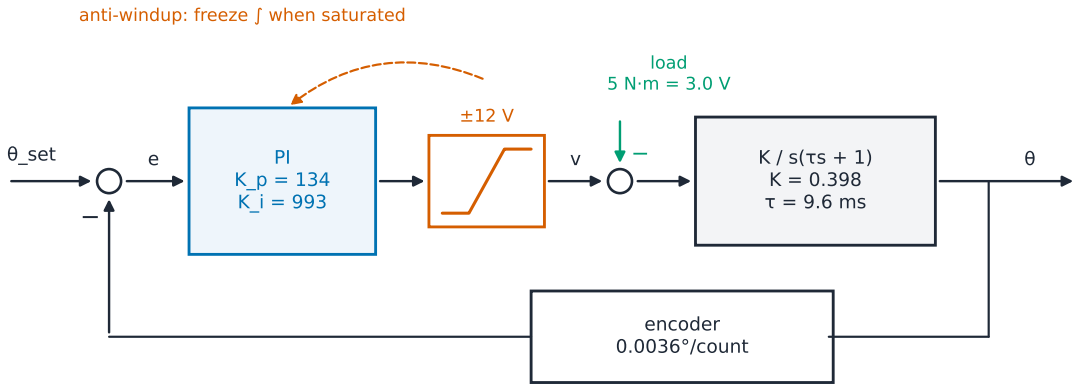
- **PID controller** PID : $u = K_p e + K_i \int e\,dt + K_d \dot{e}$, acting on the **error** e.
- A constant disturbance d (volts at the motor) leaves $e = d/K_p$ under P; the integral supplies d with $e = 0$.
- Common start: $K_i = K_p \omega_n / 10$ (zero a decade below ω_n), costing about 9° of phase margin.
- Saturated, the drive moves at its **rate limit** ; the integrator keeps growing: **integrator windup** . **Anti-windup** clamps it.

■ Worked example. Tuning against a spec

Valve loop, $K_p = 134$ V/rad, $\omega_n = 74.4$ rad/s; a 5 N · m load is 3.0 V at the motor; spec: error $\leq 0.5°$.

- P alone: $e = d/K_p = 3.0/134 = 0.0225$ rad = **1.29°**: fails.
- $K_i = K_p \omega_n / 10 =$ **993** V/(rad · s): error 0.
- A 90° step asks $134 \times 1.571 = 210$ V of 12 V: without anti-windup the valve overshoots to 159°.

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2 Practice

The valve drive of sheet 12.3: $K_p = 79.4$ V/rad, $\omega_n = 46.0$ rad/s, plant gain 0.414 rad/s per volt at the valve, 24 V supply. The 8 N · m load needs 7.84 V at the motor.

2.1 Find the steady error under P control (four decimals, rad, and two decimals, degrees). Does it meet a 0.5° spec? [3]

2.2 Choose K_i by the decade rule (one decimal) and give the steady error with it. Why is derivative action usually left out with an encoder? [3]

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3 Exam-style questions

3.1 A 90° step is commanded. (a) Find the voltage P control asks for at once (one decimal, V) and say what happens. (b) Find the valve speed at the rate limit under load (two decimals, rad/s) and the time the slew takes. (c) Explain integrator windup during the slew and its effect on arrival. (d) Describe clamping anti-windup and one other remedy. [8]

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