

12.4 FIR filter design

Name: _____ Class: _____ Date: _____ **Total: 25 marks**

KEY WORDS FIR • Hamming window

Objective

Size FIR filters from window tables, verify measured responses against promises, and account for linear-phase delay.

1 Key knowledge and worked examples

■ The window table

Approximate first sidelobes of the windows: rectangular -13 dB, Hann -31 dB, Hamming -43 dB, Blackman -58 dB. These describe the windows, not a guaranteed stopband level for every resulting filter. Use transition $\approx 3.3 \cdot f_s/N$ as a Hamming design estimate. Symmetric taps: exactly linear phase, delay $(N - 1)/2$ samples.

■ Worked example: size and verify

50 Hz transition at $f_s = 1$ kHz: $N = 3.3 \times 1000/50 = 66 \rightarrow$ take 67 (odd, Type-I), delay 33 samples. This estimates the length; without specified taps and a measured frequency response, it does not verify the stopband attenuation.

■ The verification step

Generate $|H(f)|$ from the taps and check passband ripple and stopband depth against the stated filter specification. If a -43 dB stopband target is met only to -37 dB, the design fails that target. Check the cutoff, tap count and window; that result alone does not identify the cause.

2 Practice

2.1 Hamming FIR, $f_s = 8$ kHz, transition 100 Hz: estimate N and the linear-phase delay for the odd choice. [3]

2.2 Which of Hann, Hamming and Blackman has a tabulated first window sidelobe below -50 dB? Explain why this comparison does not verify a designed filter’s stopband. [3]

2.3 Why must a Type-I design use an odd N ? [3]

3 Exam-style questions

3.1 Design a Hamming low-pass at $f_s = 1$ kHz: passband to 200 Hz, transition 50 Hz. The design targets are stopband level at or below -43 dB and passband ripple within ± 0.05 dB.

Size N (odd). State the delay in samples and milliseconds. Compute what transition $N = 31$ would deliver, and state which way the design misses. Give the two measurements that verify the design, with their expected values. [8]

3.2 An anti-alias FIR before a $\downarrow 4$ decimator at $f_s = 48$ kHz must pass 0–5 kHz and attenuate above 6 kHz.

Compute the transition band available and the required N (Hamming). The group delay of this filter in ms; the decimator drops 3 of 4 samples – explain why the filter must run BEFORE the drop. Compare the multiply rate of filtering at 48 kHz versus a polyphase scheme. [8]
