

1.4 Source transformations and network theorems

Name: _____ Class: _____ Date: _____

Total: 24 marks

KEY WORDS Thévenin's theorem • Norton's theorem
 • source transformation • superposition • maximum power transfer

Objective

Reduce a linear network to its Thévenin or Norton equivalent, apply superposition correctly (including knowing where it stops), and compute maximum power transfer with its efficiency limit.

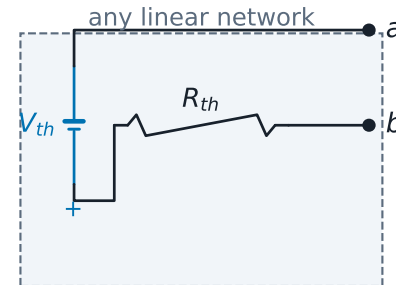
1 Key knowledge and worked examples

■ Thévenin: the network becomes one source and one resistor

Thévenin's theorem : any linear two-terminal network behaves, at its terminals, like a voltage source V_{th} in series with R_{th} . Find V_{th} as the open-circuit voltage; find R_{th} as the resistance seen from the terminals with independent sources zeroed (voltage sources shorted, current sources opened).

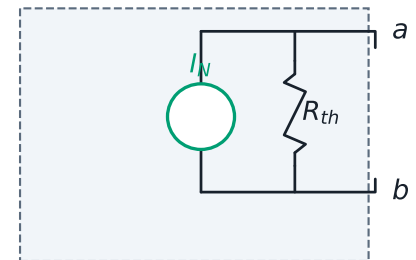
Norton's theorem is the same statement as $I_N = V_{th}/R_{th}$ in parallel with R_{th} ; swapping between the two is the **source transformation**.

Thévenin: series form



measure: V_{th} open-circuit,
 R_{th} with sources zeroed

Norton: parallel form



swap the pair freely:
 $I_N = V_{th}/R_{th}$

■ Worked example: divider, then maximum power

A 10 V source with 4 Ω in series feeds a 6 Ω shunt; the load connects across the 6 Ω .

- $V_{th} = 10 \times 6/10 = 6V$ (open-circuit voltage across the shunt).
- $R_{th} = 4 \parallel 6 = 2.4\Omega$ (source shorted).
- With $R_L = R_{th} = 2.4\Omega$: $I = 6/4.8 = 1.25A$, $P_L = 1.25^2 \times 2.4 = 3.75W$, matching $P_{max} = V_{th}^2/(4R_{th}) = 36/9.6$.

At that match the source resistance burns another 3.75 W: **50% efficiency**. Matched loads belong in signal stages, not on the power grid.

■ Superposition: add responses, never powers

Superposition : with several independent sources, the total current or voltage is the sum of the responses to each source acting alone (others zeroed).

A 9 V source through 2 Ω feeds node A; a 1 A source pulls current out of A; an 8 Ω resistor goes from A to ground. Voltage source alone: $I = 9/10 = 0.9A$ in the 8 Ω . Current source alone: the 1 A leaves through 8 $\Omega \parallel 2 \Omega$, contributing $1 \times 2/10 = 0.2A$ out of the 8 Ω . Total: $0.9 - 0.2 = 0.7$ A down the 8 Ω . Nodal check: $4(V-9) + V + 8 = 0$ ($\times 8$) gives $V = 5.6V$, and $5.6/8 = 0.7$ A. ✓

Power is quadratic – i^2R does not add across sub-solutions, so superposition never applies to power directly.

2 Practice

2.1 A 10 V source feeds $5\ \Omega$ in series with $20\ \Omega$. For the terminals across the $20\ \Omega$: compute V_{th} and R_{th} , then the short-circuit current I_N . [4]

2.2 Using the network of 2.1, find the load resistance for maximum power transfer and the maximum load power. [3]

2.3 In the panel example above (9 V, $2\ \Omega$; 1 A out of A; $8\ \Omega$ to ground), compute the $8\ \Omega$ current caused by each source alone, then show that adding the two POWER values gives a different (wrong) answer from the true $8\ \Omega$ power. [4]

3 Exam-style questions

3.1 A 15 V source with $3\ \Omega$ in series feeds a $6\ \Omega$ shunt; a variable load R_L connects across the shunt terminals.

Find V_{th} and R_{th} . Then, for $R_L = R_{th}$, compute the load current, the load power, the power wasted in R_{th} , and the efficiency. Finally state, with one calculation, whether halving R_L to $R_{th}/2$ raises or lowers the load power. [7]

3.2 Two sources feed one node: a 6 V source through $3\ \Omega$ and a 3 V source through $3\ \Omega$ (both driving current into the node), with a $3\ \Omega$ resistor from the node to ground.

Use superposition to find the node voltage and the current in the grounded resistor; verify by direct nodal analysis. Then explain why the energy dissipated in the grounded resistor is NOT the sum of the energies the two sources would dissipate it with alone. [6]
