

# 1.4 Source transformations and network theorems

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Name: \_\_\_\_\_ Class: \_\_\_\_\_ Date: \_\_\_\_\_

**Total: 24 marks**

**KEY WORDS** Thévenin's theorem • Norton's theorem  
 • source transformation • superposition • maximum power transfer

## Objective

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Reduce a linear network to its Thévenin or Norton equivalent, apply superposition correctly (including knowing where it stops), and compute maximum power transfer with its efficiency limit.

## 1 Key knowledge and worked examples

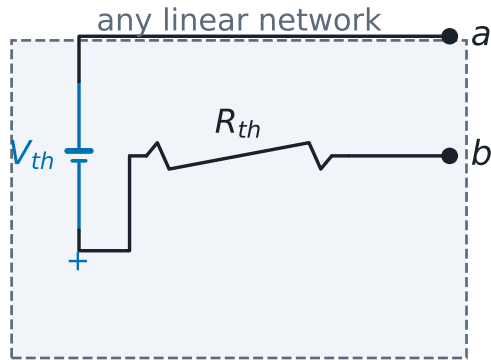
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### ■ Thévenin: the network becomes one source and one resistor

**Thévenin's theorem** : any linear two-terminal network behaves, at its terminals, like a voltage source  $V_{th}$  in series with  $R_{th}$ . Find  $V_{th}$  as the open-circuit voltage; find  $R_{th}$  as the resistance seen from the terminals with independent sources zeroed (voltage sources shorted, current sources opened).

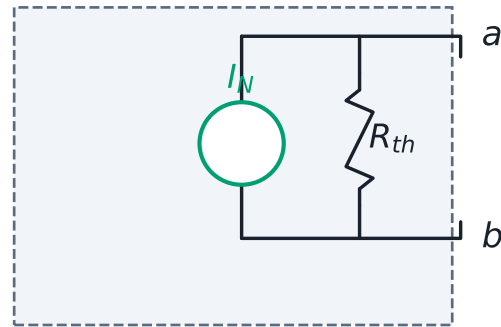
**Norton's theorem** is the same statement as  $I_N = V_{th}/R_{th}$  in parallel with  $R_{th}$ ; swapping between the two is the **source transformation** .

## Thévenin: series form



measure:  $V_{th}$  open-circuit,  
 $R_{th}$  with sources zeroed

## Norton: parallel form



swap the pair freely:  
 $I_N = V_{th}/R_{th}$

### ■ Worked example: divider, then maximum power

A 10 V source with 4  $\Omega$  in series feeds a 6  $\Omega$  shunt; the load connects across the 6  $\Omega$ .

- $V_{th} = 10 \times 6/10 = 6V$  (open-circuit voltage across the shunt).
- $R_{th} = 4 \parallel 6 = 2.4\Omega$  (source shorted).
- With  $R_L = R_{th} = 2.4\Omega$ :  $I = 6/4.8 = 1.25A$ ,  $P_L = 1.25^2 \times 2.4 = 3.75W$ , matching  $P_{max} = V_{th}^2/(4R_{th}) = 36/9.6$ .

At that match the source resistance burns another 3.75 W: **50% efficiency**. Matched loads belong in signal stages, not on the power grid.

### ■ Superposition: add responses, never powers

**Superposition** : with several independent sources, the total current or voltage is the sum of the responses to each source acting alone (others zeroed).

A 9 V source through 2  $\Omega$  feeds node A; a 1 A source pulls current out of A; an 8  $\Omega$  resistor goes from A to ground. Voltage source alone:  $I = 9/10 = 0.9A$  in the 8  $\Omega$ . Current source alone: the 1 A leaves through 8  $\Omega \parallel 2 \Omega$ , contributing  $1 \times 2/10 = 0.2A$  out of the 8  $\Omega$ . Total:  $0.9 - 0.2 = 0.7$  A down the 8  $\Omega$ . Nodal check:  $4(V-9) + V + 8 = 0$  ( $\times 8$ ) gives  $V = 5.6V$ , and  $5.6/8 = 0.7$  A. ✓

Power is quadratic –  $i^2R$  does not add across sub-solutions, so superposition never applies to power directly.

## 2 Practice

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**2.1** A 10 V source feeds 5  $\Omega$  in series with 20  $\Omega$ . For the terminals across the 20  $\Omega$ : compute  $V_{th}$  and  $R_{th}$ , then the short-circuit current  $I_N$ . [4]

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**2.2** Using the network of 2.1, find the load resistance for maximum power transfer and the maximum load power. [3]

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**2.3** In the panel example above (9 V, 2  $\Omega$ ; 1 A out of A; 8  $\Omega$  to ground), compute the 8  $\Omega$  current caused by each source alone, then show that adding the two POWER values gives a different (wrong) answer from the true 8  $\Omega$  power. [4]

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### 3 Exam-style questions

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**3.1** A 15 V source with  $3\ \Omega$  in series feeds a  $6\ \Omega$  shunt; a variable load  $R_L$  connects across the shunt terminals.

Find  $V_{th}$  and  $R_{th}$ . Then, for  $R_L = R_{th}$ , compute the load current, the load power, the power wasted in  $R_{th}$ , and the efficiency. Finally state, with one calculation, whether halving  $R_L$  to  $R_{th}/2$  raises or lowers the load power. [7]

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**3.2** Two sources feed one node: a 6 V source through  $3\ \Omega$  and a 3 V source through  $3\ \Omega$  (both driving current into the node), with a  $3\ \Omega$  resistor from the node to ground.

Use superposition to find the node voltage and the current in the grounded resistor; verify by direct nodal analysis. Then explain why the energy dissipated in the grounded resistor is NOT the sum of the energies the two sources would dissipate it with alone. [6]

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