1.5 Forces

Name: _____ Class: _____ Date: _____ **Total: 41 marks**

0 Vocabulary

Word	Example
load–extension graph 载荷-伸长图 /ləʊd ek'stenʃn græf/	A **load–extension graph** shows how a spring stretches. **载荷-伸长图**显示弹簧如何伸长。
limit of proportionality 比例极限 /'lɪmɪt ɒv prəˌpɔːʃə'nælɪti/	After the **limit of proportionality**, the graph is no longer straight. 超过**比例极限**后，图线不再是直线。
circular motion 圆周运动 /'sɜːkjʊlə 'məʊʃn/	A car going round a roundabout is in **circular motion**. 绕环岛行驶的汽车在做**圆周运动**。
radius /'reɪdɪəs/ 半径	The **radius** of a circle is the distance from the centre to the edge. 圆的**半径**是从圆心到圆周的距离。
friction /'frɪkʃn/ 摩擦力	**Friction** between the tyres and the road stops the car sliding. 轮胎与路面之间的**摩擦力**防止汽车打滑。
principle of moments 力矩原理 /'prɪnsɪpl ɒv 'məʊmənts/	The see-saw balances, as the **principle of moments** says. 跷跷板保持平衡，正如**力矩原理**所描述的那样。
centre of gravity 重心 /'sentə ɒv 'grævɪti/	A bus tips over if its **centre of gravity** is too high. 如果公共汽车的**重心**太高，就会翻倒。
lamina /'læmɪnə/ 薄片	A **lamina** is a flat shape with no thickness. **薄片**是没有厚度的平面形状。
stability /stə'bɪlɪti/ 稳定性	A low centre of gravity gives a bus **stability**. 低重心能提高公共汽车的**稳定性**。
stable /'steɪbl/ 稳定	A **stable** sort keeps equal items in the same order. **稳定**的排序会保持相等元素的原有顺序。

1 Key knowledge and worked examples

■ Forces change shape, speed or direction

A force can change an object's **shape** 形状, its speed, or its direction. **Solid friction** 固体摩擦 is the force between two surfaces that touch: it acts against the motion, tries to stop it, and heats the surfaces. Drag is friction in a liquid or a gas (air resistance).

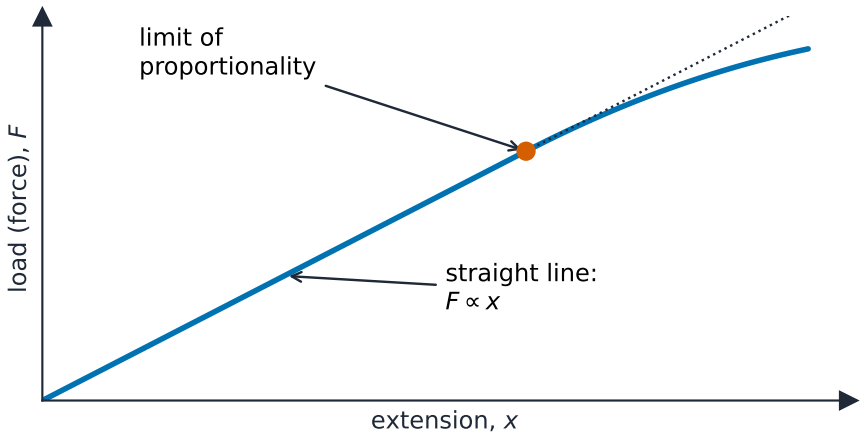
A resultant force at right angles to the motion changes only the direction, so the object moves in a circle at a steady speed. A bigger force is needed for a faster speed or a smaller radius, and for a bigger mass.

■ Hooke's law and the load–extension experiment

Hang the spring from a clamp with a ruler beside it. Read the position of the bottom of the spring with no load: that is the original length. Add loads one at a time and record the new length each time; the **extension** 伸长量 is the new length minus the original length. Plot load (y) against extension (x).

The graph is a straight line through the origin up to the **limit of proportionality** 比例极限, then it curves away. The **spring constant** 弹簧常数 is the force per unit extension:

$$k = \frac{F}{x}$$



$F = kx$ (straight section)
$k =$ gradient

Load is proportional to extension up to the limit of proportionality; the gradient of the straight part is k

Worked example 1. A spring stretches 4.0 cm under a load of 20 N. Then $k = \dfrac{20}{4.0} = 5.0$ N/cm.

■ Resultant force and $F = ma$

Add forces on a straight line with signs: one direction positive, the other negative. If the resultant is zero, the object stays at rest or keeps moving in a straight line at constant speed. If it is not zero, the object accelerates in the direction of the resultant:

$$F = ma$$

Worked example 2. A car of mass 1200 kg has a driving force of 3000 N and friction of 600 N.

1. Resultant: $3000 - 600 = 2400$ N.
2. $a = \dfrac{F}{m} = \dfrac{2400}{1200} = 2.0 \ \dfrac{\text{m}}{\text{s}^2}$.

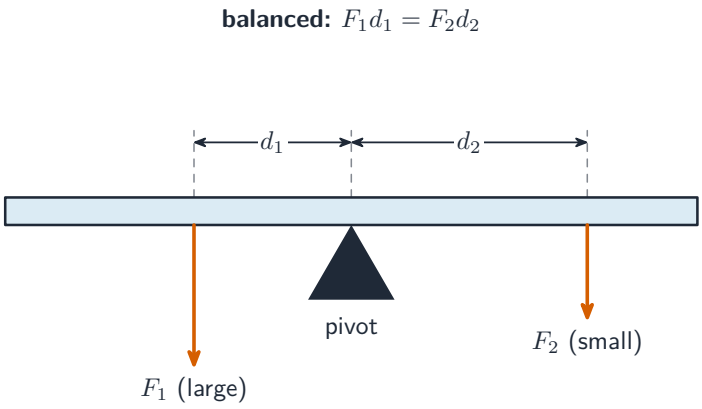
If the question asks why the engine must produce more force than $F = ma$ suggests, the answer is friction and air resistance: some of the driving force is used against them.

■ Moments and equilibrium

The **moment** 力矩 of a force is its turning effect about a **pivot** 支点:

$$\text{moment} = \text{force} \times \text{perpendicular distance from the pivot}$$

Principle of moments: for a balanced object, total clockwise moment = total anticlockwise moment. An object is in equilibrium when there is **no resultant force and no resultant moment**.



Balanced: clockwise moment equals anticlockwise moment

Worked example 3. A 30 N weight sits 0.20 m left of a pivot. How far right must a 20 N weight sit?

$30 \times 0.20 = 20 \times d$, so $d = \dfrac{6.0}{20} = 0.30$ m.

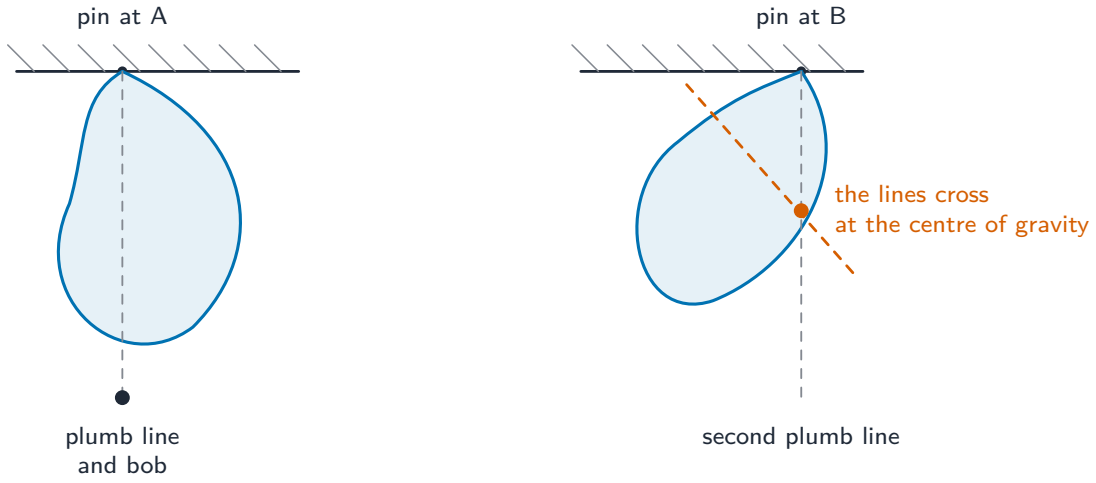
The experiment. Balance a metre rule at its centre. Hang a known weight each side and move them until it balances again. Measure both distances. Force × distance

on the left equals force × distance on the right within the measurement errors, so a balanced object has no resultant moment.

■ Centre of gravity and stability

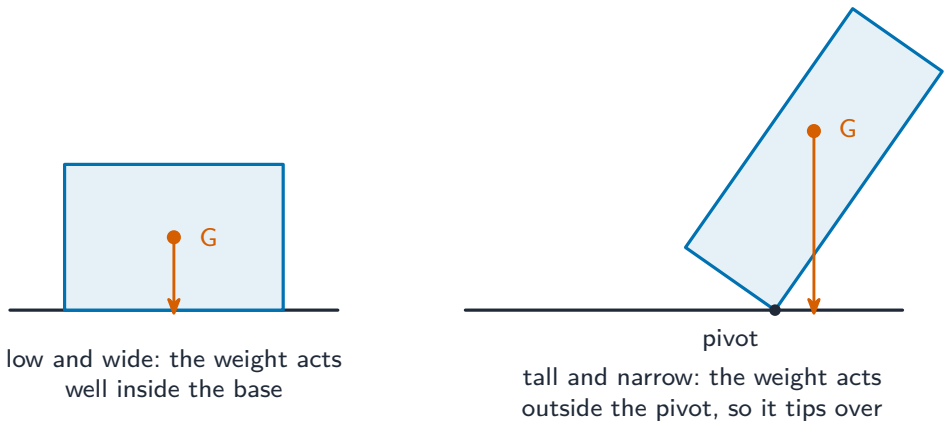
The **centre of gravity** is the single point where all the weight of an object seems to act.

Finding it for a lamina 薄片 (a flat shape): hang the shape from a pin at a point near its edge and let it settle. Hang a plumb line from the same pin and draw the vertical line on the shape. Repeat from a second point. The centre of gravity is where the two lines cross. (A third line is a useful check.)



The two vertical lines cross at the centre of gravity

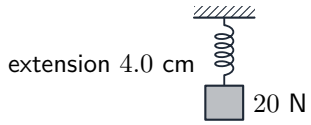
Stability 稳定性 depends on where the centre of gravity is and how wide the base is. A low centre of gravity and a wide base make an object stable. It tips over once a vertical line down from the centre of gravity falls outside the base.



While the weight acts inside the base the object settles back; once it acts outside the pivot corner the object tips over

2 Practice

2.1 A spring stretches 4.0 cm under a 20 N load. Find the spring constant in N/cm. [2]



2.2 State the principle of moments. [1]

principle of moments

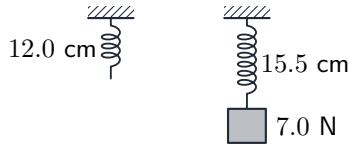
2.3 Describe what is meant by solid friction, and state one effect it has besides slowing an object down. [2]

solid friction

2.4 State the two conditions for an object to be in equilibrium. [2]

equilibrium

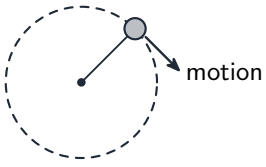
2.5 A spring of original length 12.0 cm stretches to 15.5 cm under a load of 7.0 N. Calculate its spring constant in N/cm. (Hint: use the extension, not the whole length.) [3]



2.6 State what is meant by the centre of gravity of an object. [1]

centre of gravity

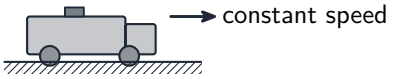
2.7 A ball on the end of a string is whirled in a horizontal circle at a steady speed. State the direction of the resultant force on the ball, and state what the force changes. [2]



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3 Exam-style questions

3.1 A car is travelling along a straight road at a constant speed. Which statement about the forces on the car is correct? [1]



☐ **A** The driving force is larger than the total resistive force.

B The driving force is equal to the total resistive force.

C There is no driving force and no resistive force.

D The driving force is smaller than the total resistive force.

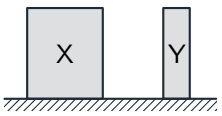
3.2 Two objects, X and Y, have the same mass and the same height. X has a wide base and Y has a narrow base. Which is more stable, and why? [1]

☐ **A** X, because its centre of gravity is further from the ground.

B X, because the weight stays inside its base for a bigger tilt.

C Y, because it is narrower and lighter at the top.

D They are equally stable, because they have the same mass.



3.3 A train has a total mass of 520 000 kg. It accelerates uniformly along a straight, level track.

(a) Define acceleration. [1]

(b) The train speeds up from 15 $\frac{\text{m}}{\text{s}}$ to 28 $\frac{\text{m}}{\text{s}}$ with an acceleration of 1.1 $\frac{\text{m}}{\text{s}^2}$. Calculate the time this takes. [2]



(c) Calculate the resultant force needed to produce this acceleration. [2]

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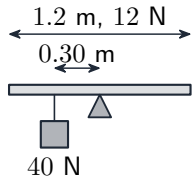
(d) The force produced by the train's motors is larger than the value in (c). Explain why. [1]

(e) The driver then applies the brakes and the train slows down. State how the direction of the resultant force compares with the direction of motion. [1]

3.4 A uniform beam of weight 12 N and length 1.2 m rests on a pivot at its centre. A 40 N weight hangs 0.30 m to the left of the pivot.

(a) Explain why the weight of the beam itself has no turning effect about this pivot. [1]

(b) A weight F_W is hung 0.50 m to the right of the pivot so that the beam balances. Calculate F_W. [3]



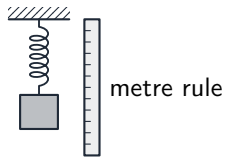
(c) The 40 N weight is now moved to 0.45 m from the pivot. State and explain what happens to the beam. [2]

(d) Describe an experiment that shows there is no resultant moment on a balanced beam. [3]

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3.5 A student investigates how a spring stretches.

(a) Describe how she should carry out the experiment, including the measurements she takes. [3]



(b) Sketch the load–extension graph she obtains, continuing the line beyond the limit of proportionality. Label the limit of proportionality on your sketch. [3]

(c) Her spring stretches 2.5 cm for a load of 10 N, within the straight part of the graph. Calculate the extension for a load of 6.0 N. [3]

(d) Explain why her method for the load of 60 N gives an extension larger than the calculation predicts. [1]

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Solutions

Each answer shows the steps, then the **result**.

2.1

- $k = F/x$

$$k = \frac{F}{x} = \frac{20\ \text{N}}{4.0\ \text{cm}} = \mathbf{5.0}\ \text{N/cm}$$

2.2

- for a balanced object, the total clockwise moment about the pivot equals the total anticlockwise moment

2.3

- the force between two surfaces that touch, which acts against (impedes) the motion
- it also produces heating of the surfaces

2.4

- no resultant force
- and no resultant moment

2.5

- extension $x = l - l_0 = 15.5\ \text{cm} - 12.0\ \text{cm} = 3.5\ \text{cm}$
- $k = F/x$

$$k = \frac{F}{x} = \frac{7.0\ \text{N}}{3.5\ \text{cm}} = \mathbf{2.0}\ \text{N/cm}$$

2.6

- the single point at which all of the weight of the object appears to act

2.7

- towards the centre of the circle
- it changes the direction of the velocity, not the speed

3.1 B

- constant speed in a straight line means zero resultant force, so the driving force balances the resistive forces
- **A** would make it accelerate; **D** would make it slow down; **C** cannot be right because friction and air resistance always act

3.2 B

- a wide base means the object can tilt further before the vertical line from the centre of gravity leaves the base
- **A** has the reasoning the wrong way round; **C** is untrue; **D** ignores the shape

3.3

(a) the change in velocity per unit time

(b) $t = \Delta v / a$

$$t = \frac{v - u}{a} = \frac{28\ \frac{\text{m}}{\text{s}} - 15\ \frac{\text{m}}{\text{s}}}{1.1\ \frac{\text{m}}{\text{s}^2}} = \mathbf{12}\ \text{s}$$

(c) $F = ma$

$$F = ma = (520\,000\ \text{kg})(1.1\ \frac{\text{m}}{\text{s}^2}) = \mathbf{570\,000}\ \text{N}$$

(d) extra force is needed to overcome friction (or air resistance / drag), because $F = ma$ gives only the resultant force

(e) the resultant force is in the opposite direction to the motion

3.4

(a) the beam is uniform, so its centre of gravity is at its centre, directly above the pivot; the perpendicular distance is zero, so its moment is zero

(b) clockwise moment = anticlockwise moment

$$\sum M_{\text{anticlockwise}} = \sum M_{\text{clockwise}} : \quad (40\ \text{N})(0.30\ \text{m}) = F_W \times (0.50\ \text{m})$$

$$12\ \text{N m} = (0.50\ \text{m}) F_W \Rightarrow F_W = \mathbf{24}\ \text{N}$$

(c) the anticlockwise moment becomes $M = Fd = (40\ \text{N})(0.45\ \text{m}) = 18\ \text{N m}$, which is larger than the clockwise $M = Fd = (24\ \text{N})(0.50\ \text{m}) = 12\ \text{N m}$

- so the beam turns anticlockwise: the left-hand side goes down

(d) balance a metre rule at its centre on a pivot

- hang a known weight on each side and adjust the distances until it balances, then measure both distances
- show that force × distance is the same on both sides, within the measurement errors

3.5

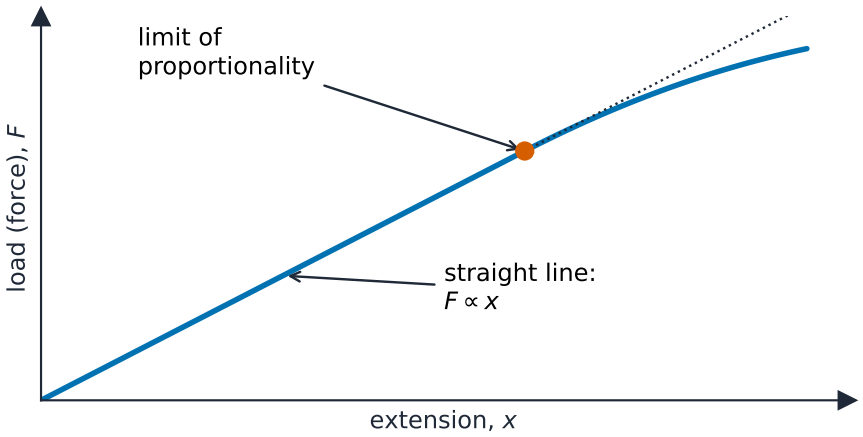
(a) hang the spring from a clamp with a ruler fixed beside it and record the position of the bottom with no load

- add loads one at a time, recording the load and the new length each time
- calculate the extension as new length minus original length

(b) a straight line through the origin

- a marked point where the line stops being straight, labelled “limit of proportionality”
- beyond it the line curves so that extension grows faster than load

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$F = kx$ (straight section)
$k =$ gradient

(c) $k = F/x$

$$k = \frac{F}{x} = \frac{10 \text{ N}}{2.5 \text{ cm}} = 4.0 \text{ N/cm}$$

- $x = F/k$

$$x = \frac{F}{k} = \frac{6.0 \text{ N}}{4.0 \text{ N/cm}} = \mathbf{1.5} \text{ cm}$$

(d) a load of 60 N is beyond the limit of proportionality, so extension is no longer proportional to load