

1.2 Motion

Name: _____ Class: _____ Date: _____

Total: 28 marks

KEY WORDS speed–time graph 速度-时间图 • acceleration 加速度 • terminal velocity 终极速度
• deceleration 减速 • uniform 均匀

Objective

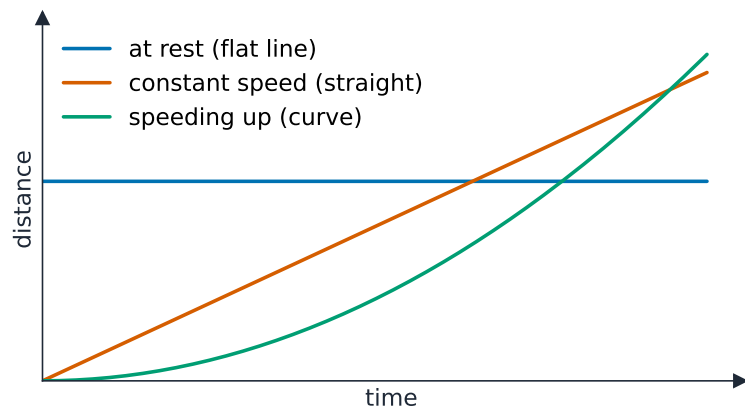
Build the skills to answer exam questions on **motion** 运动 — speed, velocity, **acceleration** 加速度, motion graphs, and **terminal velocity** 终极速度.

You must be able to:

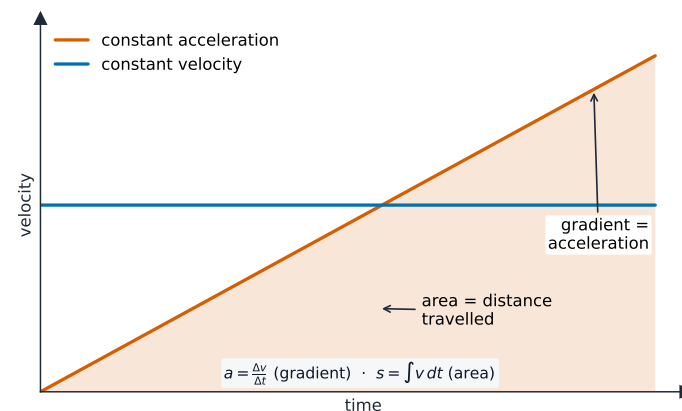
- use $v = \frac{s}{t}$ and $a = \frac{\Delta v}{\Delta t}$
- read distance–time and speed–time graphs (gradient and area)
- describe falling objects and terminal velocity

1 Worked examples

■ Graphs and acceleration



Distance–time: flat = at rest, straight slope = constant speed, rising curve = speeding up



Velocity–time: gradient = acceleration, area under the line = distance

Car 8 → 20 m/s in 4.0 s: $a = \frac{20 - 8}{4.0} = 3.0 \text{ m/s}^2$.

■ Reading a speed–time graph, and deceleration

Describe each straight section of a speed–time graph by name: a horizontal line is **constant speed**; a line sloping up is **constant (uniform) acceleration**; a line sloping down is **constant deceleration**. A **deceleration** 减速 is a negative acceleration, so put a minus sign in the arithmetic: slowing from 12 m/s to 4 m/s in 4.0 s gives $a = \frac{4 - 12}{4.0} = -2.0 \text{ m/s}^2$, a deceleration of 2.0 m/s^2 .

The **area under a speed–time line** is the distance travelled. Split the area into rectangles and triangles: a rectangle is speed × time; a triangle is $\frac{1}{2} \times \text{base} \times \text{height}$.

Worked example (show that). A bus is at 10 m/s for 120 s, then decelerates uniformly to rest in 40 s. Show that it travels about 1400 m. Rectangle: $10 \times 120 = 1200 \text{ m}$. Triangle: $\frac{1}{2} \times 40 \times 10 = 200 \text{ m}$. Total 1400 m. In a "show that" question, always finish with the number the question quotes.

Near the Earth all objects fall with the same **acceleration of free fall** $g \approx 9.8 \text{ m/s}^2$ while air resistance is small. As speed rises, air resistance grows until it equals the weight; the resultant force is then zero and the object falls at a steady **terminal velocity** 收尾速度.

2 Practice

2.1 A runner covers 100 m in 12.5 s. Find the average speed. [2]

2.2 State what the area under a speed–time graph represents. [1]

2.3 A car slows from 18 m/s to 6.0 m/s in 4.0 s. Calculate its acceleration and state what the sign means. [3]

2.4 State how you find the distance travelled from a speed-time graph. [1]

3 Exam-style questions

3.1 On a distance–time graph, a horizontal (flat) line means the object is: [1]

- **A** accelerating
- **B** at rest
- **C** at constant speed
- **D** decelerating

3.2 A car accelerates uniformly from rest to 24 m/s in 8.0 s.

(a) Find the acceleration. [2]

(b) Find the distance travelled (area under the speed–time graph). [2]

3.3 A skydiver falls and reaches terminal velocity. Explain, in terms of forces, why the speed becomes steady. [3]

3.4 Fig. 3.1 describes the first five minutes of a bus journey. The bus is at rest until $t = 0.90$ min, speeds up uniformly to 7.5 m/s at $t = 2.9$ min, holds that speed until $t = 3.5$ min, then slows uniformly to rest at $t = 4.5$ min.

(a) Describe the motion of the bus between $t = 2.9$ min and $t = 3.5$ min, and between $t = 3.5$ min and $t = 4.5$ min. [2]

(b) Calculate the acceleration of the bus between $t = 0.90$ min and $t = 2.9$ min. [3]

(c) Show that the bus travels about 270 m while it is speeding up. [2]

(d) Calculate the deceleration of the bus in the last minute, and state what the sign of your answer means. [3]

(e) A stone is dropped from a tall building. Describe how its acceleration changes from the moment it is released until it reaches terminal velocity, and explain why. [3]

Solutions

Each answer shows the steps, then the **result**.

2.1

- $v = s/t$

$$v = \frac{100 \text{ m}}{12.5 \text{ s}} = \mathbf{8.0 \text{ m/s}}$$

2.2

- the distance travelled

2.3

- $a = \Delta v / \Delta t$

$$a = \frac{6.0 \text{ m/s} - 18 \text{ m/s}}{4.0 \text{ s}} = \mathbf{-3.0 \text{ m/s}^2}$$

- the minus sign means the car is decelerating, so the acceleration is opposite to the motion

2.4

- find the area under the line (between the line and the time axis)

3.1 B

- a flat line on a distance–time graph means the distance is not changing — at rest

3.2

(a) $a = \Delta v / \Delta t$

$$a = \frac{24 \text{ m/s} - 0}{8.0 \text{ s}} = \mathbf{3.0 \text{ m/s}^2}$$

(b) distance = area of the triangle

$$s = \frac{1}{2}(8.0 \text{ s})(24 \text{ m/s}) = \mathbf{96 \text{ m}}$$

3.3

- as the diver speeds up, air resistance increases
- when air resistance equals the weight, the resultant force is zero
- so there is no acceleration and the speed stays constant (terminal velocity)

3.4

(a) between 2.9 and 3.5 min: constant speed

- between 3.5 and 4.5 min: constant (uniform) deceleration to rest

(b) time = $(2.9 - 0.90) \times 60 \text{ s} = 120 \text{ s}$

- $a = \Delta v / \Delta t$

$$a = \frac{7.5 \text{ m/s} - 0}{120 \text{ s}} = \mathbf{0.063 \text{ m/s}^2}$$

(c) distance = area of the speeding-up triangle

$$s = \frac{1}{2}(120 \text{ s})(7.5 \text{ m/s}) = \mathbf{450 \text{ m}}$$

- for the first 72 s of it the area is 270 m

(d) time = 60 s; $a = \Delta v / \Delta t$

$$a = \frac{0 - 7.5 \text{ m/s}}{60 \text{ s}} = \mathbf{-0.13 \text{ m/s}^2}$$

- the minus sign means the bus is slowing down, so the resultant force is opposite to the motion

(e) at first the acceleration is g , because only the weight acts

- as the stone speeds up, air resistance grows and the resultant force falls, so the acceleration decreases
- when air resistance equals the weight the resultant force and the acceleration are zero and the speed is constant