

E7.3 Magnitude of a vector

Name: _____ Class: _____ Date: _____

Total: 15 marks

KEY WORDS magnitude 模 • column vector 列向量 • component 分量 • scalar multiple 数乘
• exact form 精确值

Objective

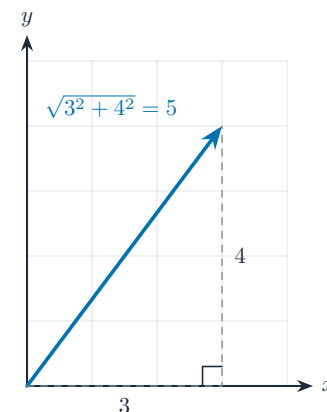
Build the skills to answer Extended exam questions on the **magnitude of a vector** 向量的模 — finding $|\mathbf{a}|$ from a **column vector** 列向量, combining vectors first and then taking the magnitude, and working backwards from a given magnitude.

You must be able to:

- find the magnitude of a column vector using Pythagoras
- add, subtract and multiply column vectors before finding a magnitude
- find a missing component when the magnitude is given

1 Worked examples

■ Magnitude is Pythagoras on the two components



The two components are the short sides; the magnitude is the hypotenuse

- **Formula:** if $\mathbf{a} = \begin{pmatrix} x \\ y \end{pmatrix}$ then $|\mathbf{a}| = \sqrt{x^2 + y^2}$.
- **The signs vanish**, because both components are squared. $\begin{pmatrix} 6 \\ -8 \end{pmatrix}$ has magnitude 10, the same as $\begin{pmatrix} 6 \\ 8 \end{pmatrix}$.
- **Combine FIRST.** $|\mathbf{a} + \mathbf{b}|$ means add the vectors and then take the magnitude; it is NOT $|\mathbf{a}| + |\mathbf{b}|$.
- **Scalar multiple:** $2\mathbf{a}$ multiplies BOTH components by 2.

Answer shapes (marked by **method marks** — M1 for a correct method, A1 for the correct answer): the combined column vector, and the square root expression, are separate method marks.

2 Practice

2.1 $\mathbf{a} = \begin{pmatrix} 3 \\ 4 \end{pmatrix}$. Find $|\mathbf{a}|$.

[2]

2.2 $\mathbf{b} = \begin{pmatrix} -5 \\ 12 \end{pmatrix}$. Find $|\mathbf{b}|$. [2]

2.3 $\mathbf{c} = \begin{pmatrix} 6 \\ -8 \end{pmatrix}$. Find $|\mathbf{c}|$. [2]

3 Exam-style questions

3.1 $\mathbf{a} = \begin{pmatrix} 4 \\ -3 \end{pmatrix}$ and $\mathbf{b} = \begin{pmatrix} -1 \\ 5 \end{pmatrix}$.

(a) Find $\mathbf{a} + \mathbf{b}$ as a column vector. [1]

(b) Find $|\mathbf{a} + \mathbf{b}|$, giving your answer in exact form. [2]

(c) Find $|2\mathbf{a} - \mathbf{b}|$, correct to 3 significant figures. [3]

3.2 The vector $\begin{pmatrix} k \\ 8 \end{pmatrix}$ has magnitude 17. Find the positive value of k . [3]
