

C9.5 Scatter diagrams

Name: _____ Class: _____ Date: _____

Total: 20 marks

KEY WORDS correlation 相关性 • positive correlation 正相关 • scatter diagram 散点图
 • line of best fit 最佳拟合线 • negative correlation 负相关

Objective

Use scatter diagrams to solve Core IGCSE Mathematics problems.

You must be able to:

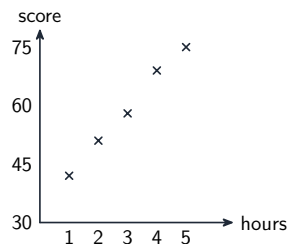
- Plot paired observations and identify correlation
- Draw a balanced by-eye best-fit line
- Distinguish interpolation, extrapolation and a causal claim

1 Key knowledge and worked examples

■ Key knowledge: Scatter diagrams

A scatter diagram plots paired observations with small crosses; do not join consecutive points. Positive correlation rises overall, negative falls, zero has no clear pattern. Draw a single ruled line of best fit by eye across the whole data range, with roughly balanced points on either side. It need not pass through the origin or a data point. Use it to estimate within the observed range; extrapolation outside is less reliable. Correlation does not establish cause.

■ Worked example: Scatter diagrams



Paired study hours and scores are $(1, 42)$, $(2, 51)$, $(3, 58)$, $(4, 69)$, $(5, 75)$.

- Plot each pair as a cross. Scores generally increase: positive correlation.
- A reasonable best-fit line is $s = 8.5h + 34$, giving $s = 8.5(3.5) + 34 = 63.75$, about 64 marks.

- This is an estimate for these data, not a guarantee for a student. Extending to 12 hours goes far outside the sample.
- A line of best fit need not go through a data point. For five observations, judge the balance across the full range rather than forcing two selected points to define it.

■ Method check

Keep each pair together when plotting. A fitted line is an estimate for the observed relationship, not proof that one variable causes the other.

2 Practice

2.1 Name the correlation when points tend to fall from left to right. [2]

2.2 Explain why scatter points should not be joined in order. [2]

2.3 A best-fit line is $y = 2x + 10$. Estimate y at $x = 7$. [2]

2.4 Observations cover $2 \leq x \leq 8$. Which estimate is usually safer: $x = 5$ or $x = 20$? Explain. [2]

3 Exam-style questions

3.1 Apply the scatter diagrams methods below. Show working and include units where appropriate.

(a) Plot crosses for (1, 12), (2, 15), (3, 19), (4, 20), (5, 24) and state the correlation. [2]

(b) Draw a line of best fit and estimate y at $x = 3.5$. [2]

(c) Explain why this diagram does not show that increasing x causes y to increase. [2]

3.2 A scatter diagram records room temperatures from 15°C to 25°C and drink sales. A by-eye best-fit line is $s = 4T - 20$, where T is temperature and s is sales.

(a) Use the line to estimate sales at 22°C. Find the temperature corresponding to an estimate of 60 sales. [3]

(b) Evaluate a prediction at 35°C and the claim that raising the room temperature must increase sales. Give reasons using the data range and meaning of correlation. [3]