

C5.4 Surface area and volume

Name: _____ Class: _____ Date: _____

Total: 20 marks

KEY WORDS cylinder 圆柱 • cuboid 长方体 • surface area 表面积 • sphere 球
• cross-section 横截面

Objective

Use surface area and volume to solve Core IGCSE Mathematics problems.

You must be able to:

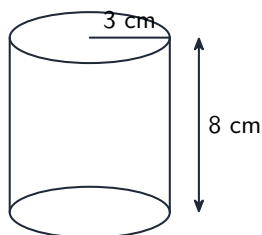
- Find prism, cylinder, cone, pyramid and sphere volumes
- Calculate surface area from the exposed faces
- Use perpendicular height for volume and slant height where area requires it

1 Key knowledge and worked examples

■ Key knowledge: Surface area and volume

Volume measures space inside; surface area totals exposed faces. Cuboid: $V = lwh$, $S = 2(lw + lh + wh)$. Prism: $V = Ah$, where A is cross-section area and h is length. Cylinder: $V = \pi r^2 h$, curved area $2\pi rh$; add circular ends when needed. Cone: $V = \pi r^2 h/3$, curved area πrl , using slant height l . Pyramid: $V = Ah/3$. Sphere: $V = 4\pi r^3/3$, $S = 4\pi r^2$.

■ Worked example: Surface area and volume



A closed cylinder has radius 3 cm and height 8 cm.

- Volume: $V = \pi r^2 h = \pi(3)^2(8) = 72\pi \text{ cm}^3$.
- Surface area: $S = 2\pi rh + 2\pi r^2 = 2\pi(3)(8) + 2\pi(3)^2 = 66\pi \text{ cm}^2$.
- A cone with $r = 3$, $h = 4$, $l = 5$ has $V = \pi(3)^2(4)/3 = 12\pi$ and total $S = \pi(3)(5) + \pi(3)^2 = 24\pi$ in the appropriate units.
- A triangular prism with cross-section base 6 cm, height 4 cm and length 9 cm has $A = bh/2 = 6(4)/2 = 12 \text{ cm}^2$, then $V = Ah = 12(9) = 108 \text{ cm}^3$.

- For a pyramid of base area 30 cm^2 and height 8 cm , $V = Ah/3 = 30(8)/3 = 80 \text{ cm}^3$. A sphere of radius 3 cm has $V = 4\pi r^3/3 = 36\pi \text{ cm}^3$ and $S = 4\pi r^2 = 36\pi \text{ cm}^2$.

■ Method check

Draw or list the exposed faces before adding areas. A prism's volume uses its cross-section area multiplied by the distance between its ends.

2 Practice

2.1 Find the volume and surface area of a $5 \times 3 \times 2 \text{ cm}$ cuboid. [2]

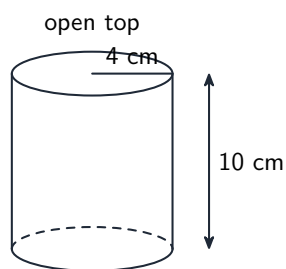
2.2 A triangular prism has cross-section base 6 cm and height 4 cm ; length is 9 cm . Find its volume. [2]

2.3 A pyramid has base area 30 cm^2 and perpendicular height 8 cm . Find its volume. [2]

2.4 Find the volume and surface area of a sphere of radius 3 cm in terms of π . [2]

3 Exam-style questions

3.1 Apply the surface area and volume methods below. Show working and include units where appropriate.

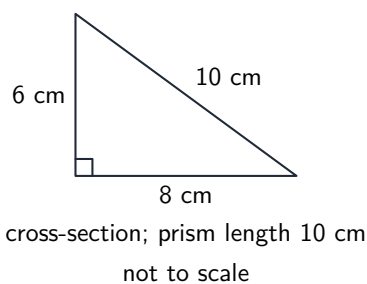


(a) An open-top cylindrical container has radius 4 cm and height 10 cm. Find its volume in terms of π . [2]

(b) Find its exposed area, including its circular base but not its open top. [2]

(c) A cone has the same radius and height. Find its volume, and compare it with the cylinder. [2]

3.2 A triangular prism is 10 cm long. Its right-triangle cross-section has perpendicular sides 6 cm and 8 cm and hypotenuse 10 cm.



(a) Find the prism volume. [3]

(b) Find its total surface area, explaining how the two ends and three rectangular faces are included. [3]
