

E4.7 Circle theorems I

Name: _____ Class: _____ Date: _____

Total: 9 marks

Objective

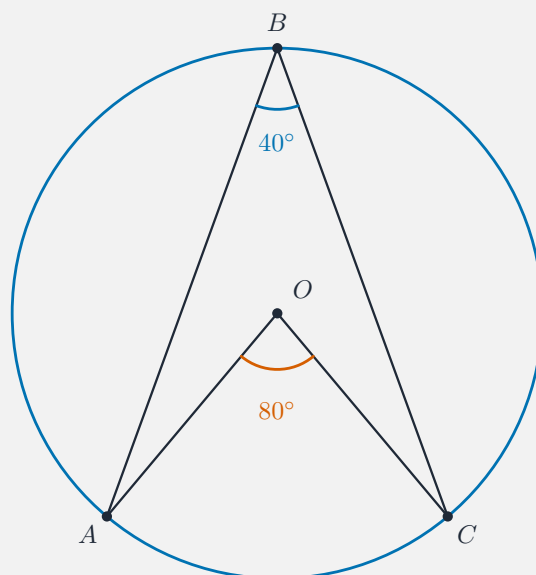
Build the skills to answer Extended exam questions on **circle theorems** 圆定理—the angle at the **centre**, angles in the **same segment**, the **cyclic quadrilateral** 圆内接四边形, and the semicircle/tangent facts. Always **give a reason**.

You must be able to:

- use "angle at the centre = twice the angle at the circumference"
- use "angles in the same segment are equal" and the cyclic-quadrilateral rule
- use the semicircle and tangent–radius right angles

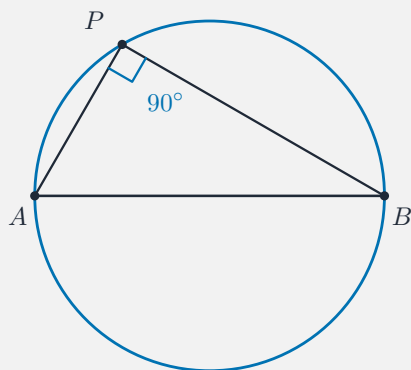
1 Worked examples

■ Circle theorems

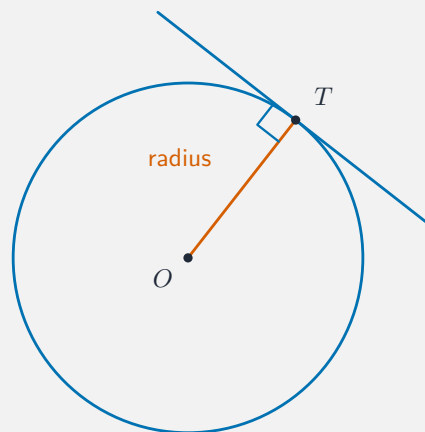


angle at centre = $2 \times$ angle at circumference

Standing on the same arc



angle in a
semicircle = 90°



tangent meets
radius = 90°

Further circle theorems: angle in a semicircle and the tangent

- Angle at **centre** = $2 \times$ angle at **circumference** (same arc).
- Angles in the **same segment** are equal; opposite angles of a **cyclic quadrilateral** add to 180° .
- Angle in a **semicircle** = 90° ; tangent meets radius at 90° .
- **Worked:** circumference angle $40^\circ \rightarrow$ centre angle = $2 \times 40 = 80^\circ$.

Answer shapes: M1 a correct method, A1 the correct answer.

2 Practice

2.1 The angle at the circumference standing on an arc is 35° . Find the angle at the centre on the same arc. [1]

2.2 A triangle is drawn with one side a diameter. State the angle at the point on the circle. [1]

2.3 In a cyclic quadrilateral, one angle is 85° . Find the opposite angle. [2]

3 Exam-style questions

3.1 A, B, C lie on a circle, centre O . The angle AOC at the centre is 130° . Find the angle ABC at the circumference, giving a reason. [2]

3.2 $PQRS$ is a cyclic quadrilateral. Angle $PQR = 95^\circ$ and angle $QRS = 70^\circ$. Find angles PSR and SPQ . [3]

4 Go further

You are now ready for the real exam questions on this subtopic. Open the **E4.7 Circle theorems I** past-paper sheet in the Library, or try these in **Practice mode**:

- 0580/21 N25 —Q14 (circle theorems)
- 0580/23 N25 —Q21 (circle theorems, applied)

Solutions

Marking: **M1** a correct method, **A1** the correct answer.

2.1 $2 \times 35 = 70^\circ$.

2.2 90° (angle in a semicircle).

2.3 opposite angles of a cyclic quadrilateral add to 180° : $180 - 85 = 95^\circ$.

3.1 angle $ABC = \frac{1}{2} \times 130 = 65^\circ$ (reason: angle at the centre is twice the angle at the circumference).

3.2 opposite angles add to 180° : $PSR = 180 - 95 = 85^\circ$; $SPQ = 180 - 70 = 110^\circ$.