14.2 Standing waves and resonance (full C.4)

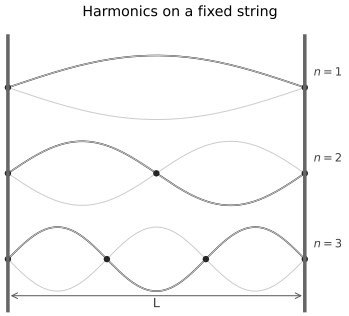
Name: _____ Class: _____ Date: _____ **Total: 25 marks**

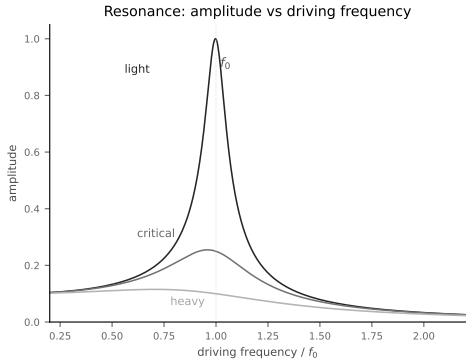
KEY WORDS standing wave • node • antinode • resonance • damping

Objective

Practise the full guide C.4 toolkit: standing waves as superposition of two identical opposite-travelling waves, nodes and antinodes with their amplitude and phase relations, boundary-condition patterns on strings and in pipes (fixed/fixed, fixed/free; closed/closed, closed/open, open/open), nth-harmonic wavelength and frequency from length and wave speed, resonance with natural and driving frequency, and the effect of light, critical and heavy damping. Original practice; not an official IB paper.

1 Key knowledge and worked examples





■ The C.4 rule set

Node–node or antinode–antinode ends: $\lambda_n = 2L/n$, $f_n = nv/2L$. Node–antinode ends (closed–open pipe, fixed–free string): $\lambda_n = 4L/(2n-1)$, $f_n = (2n-1)v/4L$ – odd harmonics only. A fixed end or closed pipe end is a displacement node; a free end or open pipe end is an antinode. Points between neighbouring nodes oscillate in phase; points either side of a node are in antiphase.

■ Worked example: one pipe, two configurations

A 0.50 m pipe with air at 340 m/s. Open at both ends: $f_1 = v/2L = 340/1.0 = 340$ Hz. Closed at one end: $f_1 = v/4L = 340/2.0 = 170$ Hz, and only odd harmonics – 170, 510, 850 Hz – can sound. Two habits: write the boundary condition at each end before choosing the formula, and check the harmonic list against the pattern (every n, or odd n only).

2 Practice

2.1 State how a standing wave forms, and what is meant by a node. [2]

2.2 State the phase difference between two points on a standing wave that lie on the same side of a node, and between two points on opposite sides of a node. [2]

2.3 A string fixed at both ends is 0.80 m long and carries waves at 160 m/s. Calculate the first and second harmonic frequencies. [3]

2.4 State two changes damping makes to the resonance curve of a driven oscillator. [2]

3 Exam-style questions

3.1 A pipe closed at one end is 0.34 m long; the speed of sound is 340 m/s. Calculate the first harmonic frequency and the next harmonic frequency above it, and explain why no harmonic exists between them. [4]

3.2 A guitar string is fixed at both ends. State the boundary condition at each end, and explain why only certain wavelengths can form standing waves on the string. [4]

3.3 A car's suspension oscillates at a natural frequency of about 1.5 Hz. Describe what happens to the amplitude as the car is driven over regular bumps at increasing speed, and explain the role of the shock absorbers in this context. [4]

3.4 A pipe of length 0.50 m is first tested open at both ends and then closed at one end (air speed 340 m/s). Calculate both first harmonic frequencies and state the ratio between them. [4]