

6.3 Searching, sorting and Big O

Name: _____ Class: _____ Date: _____

Total: 21 marks

KEY WORDS linear search • binary search • bubble sort
• selection sort • Big O O

Objective

Build the skills to answer exam questions on **searching, sorting and efficiency** – linear and binary search, bubble and selection sort, and Big O notation.

You must be able to:

- trace a **linear search** and a **binary search**, giving each value compared
- state why binary search needs a sorted list
- show a list after each pass of a **bubble sort** and a **selection sort**
- state the **Big O** of each algorithm and compare their efficiency

1 Key knowledge and worked examples

Study these first. Each one shows the method for a question type used later.

■ Key knowledge: Big O

Big O	Example	Steps for $n = 1000$
$O(1)$	reading <code>a[5]</code>	1
$O(\log n)$	binary search	about 10
$O(n)$	linear search	1000
$O(n^2)$	bubble sort, selection sort	about 1 000 000

- Big O gives the worst case as n grows. One loop over the data: $O(n)$; a loop inside a loop: $O(n^2)$.

■ Worked example: binary search

	0	1	2	3	4	5	6	7	8
probe 1: $16 < 23$, go right	2	5	8	12	16	23	38	56	72
probe 2: $38 > 23$, go left	2	5	8	12	16	23	38	56	72
probe 3: found at index 5	2	5	8	12	16	23	38	56	72

```

low, high = 0, len(a) - 1
while low <= high:
    mid = (low + high) // 2
    if a[mid] == target:
        return mid
    elif a[mid] < target:
        low = mid + 1
    else:
        high = mid - 1
return -1

```

low	high	mid	a[mid]	Action
0	8	4	16	$16 < 23$: low = 5
5	8	6	38	$38 > 23$: high = 5
5	5	5	23	found: return 5

Three comparisons; a linear search would need six. On an unsorted list the discarded half might hold the target.

■ Worked example: two sorts

Sort [7, 3, 9, 1] into ascending order.

After pass	Bubble sort	Selection sort
1	[3, 7, 1, 9]	[1, 3, 9, 7]
2	[3, 1, 7, 9]	[1, 3, 9, 7]
3	[1, 3, 7, 9]	[1, 3, 7, 9]

1. **Bubble:** compare neighbours, swap if out of order. Pass 1 moves 9 to the end.
2. **Selection:** find the smallest of the unsorted part and swap it into place. Pass 1 swaps 1 with 7.
3. Both are $O(n^2)$. A bubble sort with a **swapped** flag stops after a pass with no swaps.

2 Practice

2.1 List the values compared when a linear search looks for 40 in [12, 7, 40, 3, 25], and the number of comparisons if it looks for 99. [2]

2.2 Show [5, 2, 8, 1, 4] after each of the first **two** passes of a bubble sort. [2]

2.3 Show [5, 2, 8, 1, 4] after each of the first **two** passes of a selection sort. [2]

2.4 A sorted list has 1000 items. State the greatest number of items compared by (i) a linear search; (ii) a binary search. [2]

3 Exam-style questions

3.1 Which statement about binary search is true? [1]

- ☐ **A** it works on any list
B it checks every item in turn
C it needs the list to be sorted
D it is $O(n^2)$

3.2 Which is the Big O of a selection sort? [1]

- ☐ **A** $O(1)$
B $O(\log n)$
C $O(n)$
D $O(n^2)$

$$[1]$$

A the list is sorted
B the list has duplicates
C one more pass is needed
D the list is in reverse order

[104, 117, 131, 148, 152, 166, 179, 183, 190, 205, 218]