

32.1 Diffraction envelopes and missing interference orders

Name: _____ Class: _____ Date: _____ **Total: 10 marks**

KEY WORDS diffraction envelope • missing order

Objective

Derive and evaluate the far-field single-slit intensity using amplitude superposition; Separate double-slit interference spacing from finite-aperture envelope width; Identify missing orders and state the limits of far-field and small-angle formulas. Original public practice; not an ETS paper.

1 Key knowledge and worked examples

Uniform far-field slit amplitude is $\sin\beta/\beta$, $\beta=\pi a \sin\theta/\lambda$. Square it for intensity and take its centre limit as one. Zeros have a $\sin\theta=m\lambda$, $m\neq 0$.

For small angles, first-zero displacement is $L\lambda/a$ and central width $2L\lambda/a$. Use $\theta=asin(m\lambda/a)$, $y=L \tan\theta$ for larger angles; the far-field assumption remains necessary.

Two coherent equal finite slits give normalised $I=(\sin\beta/\beta)^2\cos^2\alpha$, $\alpha=\pi d \sin\theta/\lambda$. Interference spacing $\approx\lambda L/d$; envelope width $\approx 2\lambda L/a$. Width and separation have different roles.

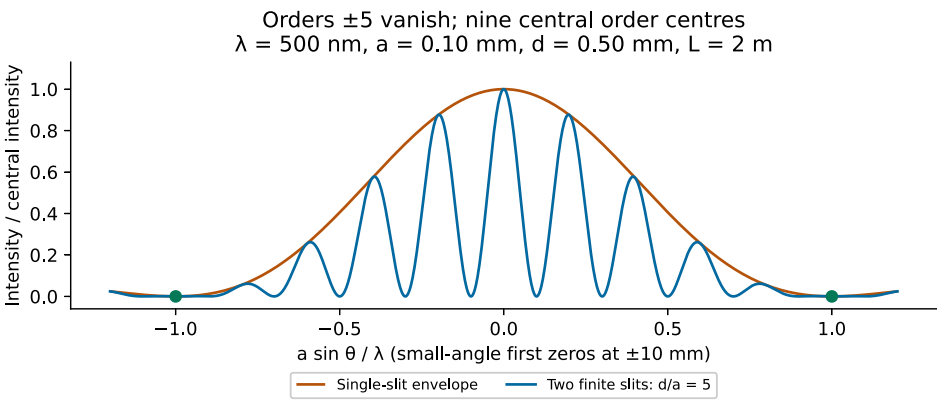
Missing orders satisfy $n=m d/a$. Integer $d/a=r$ cancels $\pm r$, $\pm 2r$, etc.; central-envelope nominal order centres satisfy $|n|<r$, giving $2r-1$. Exact product maxima can be slightly shifted.

■ Worked method

For two finite slits, separate interference spacing from the single-slit envelope.

$$I/I_{centre} = (\sin \beta/\beta)^2 \cos^2 \alpha, \quad \beta = \pi a \sin \theta/\lambda, \quad \alpha = \pi d \sin \theta/\lambda.$$

If $d = 5a$, the first envelope zero $a \sin \theta = \lambda$ coincides with order $n = 5$. Nominal order centres in the central envelope are $n = -4$ through $+4$: nine in total. These are interference centres; the envelope can shift the exact product maxima slightly.



2 Practice

2.1 Choose one answer. Two equal finite slits have $d=4a$. Which nominal interference orders are cancelled by the first single-slit minima? [1]

- A ± 1
- B ± 2
- C ± 3
- D ± 4
- E Only 0

2.2 Choose one answer. Double slit width a is doubled while d , λ and L stay fixed in the small-angle far field. What changes? [1]

- A Spacing and envelope both double
- B Fringe spacing halves; envelope fixed
- C Fringe spacing fixed; envelope width halves
- D Envelope doubles; fringe spacing fixed
- E All intensity zeros disappear

2.3 With $\lambda=600 \text{ nm}$, $L=1 \text{ m}$ and $a=0.20 \text{ mm}$, small-angle central single-slit width is _____ mm. Show your relation and units. [2]

[2]

[4]