

8.1 Solid-state, nuclear and particle models

Name: _____ Class: _____ Date: _____

Total: 10 marks

KEY WORDS band gap • half-life

Objective

Use band and carrier descriptions; Apply radioactive decay and binding-energy ideas; Check conservation laws in particle reactions. Original public practice; not an ETS paper.

1 Key knowledge and worked examples

Filled bands cannot carry ordinary current without accessible nearby states. Metals have partially filled or overlapping bands; semiconductors have a small band gap. Donor and acceptor doping change carrier populations.

Fermi–Dirac occupancy is $1/[\exp((E-\mu)/(kT))+1]$. At zero temperature it becomes a step at the Fermi energy; thermal broadening does not make every state half occupied.

Radioactive populations obey $N=N_0e^{-(\lambda t)}$, activity λN and half-life $\ln 2/\lambda$. Binding energy comes from a mass deficit multiplied by c^2 ; compare binding energy per nucleon when discussing stability.

Nuclear and particle processes must conserve charge, energy, momentum and the applicable quantum numbers. Beta decay includes a neutrino or antineutrino; a two-body electron-only story cannot explain its continuous energy spectrum.

■ Worked method

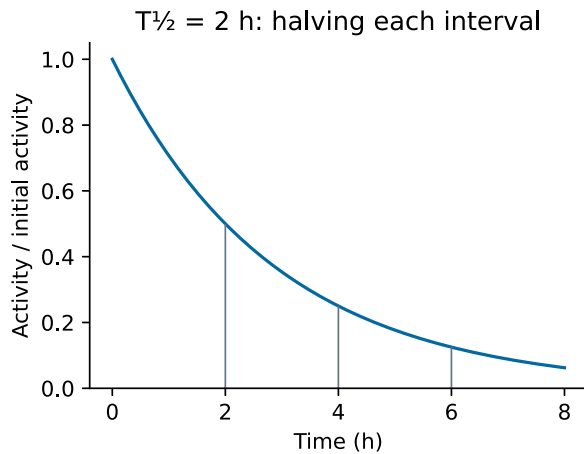
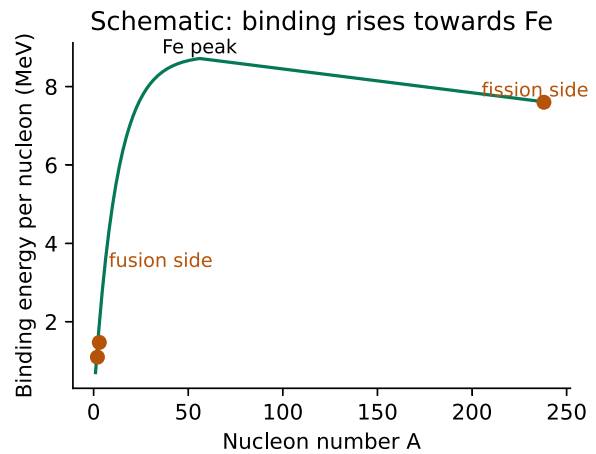
Binding energy is the positive energy required to separate a nucleus into free nucleons. For a reaction use total initial and final rest masses, with a consistent mass convention.

$$Q = (M_i - M_f)c^2.$$

A mass decrease of 0.0040 atomic mass units gives

$$Q = \Delta Mc^2 = (0.0040 \text{ u})(931.5 \text{ MeV/u}) = 3.73 \text{ MeV}.$$

Positive Q means energy release. Charge, nucleon number, energy and momentum must still balance; Q alone does not establish a reaction rate.



2 Practice

2.1 Choose one answer. After two half-lives, the remaining fraction is: [1]

- A $1/2$
- B $1/4$
- C $1/8$

2.2 Choose one answer. Donor doping commonly supplies: [1]

- A additional electron carriers
- B only photons
- C no mobile carriers

2.3 After four half-lives, one part in _____ remains. Show your relation and units. [2]

2.4 Decide whether this claim is true. Justify it: Charge conservation alone is sufficient to validate any particle reaction. [2]

3 Exam-style questions

3.1 A neutral stationary parent nucleus decays into two neutral fragments with masses m and $3m$. Released kinetic energy is Q , small compared with either rest energy. Find each fragment's kinetic energy and speed ratio. [4]