

29.1 Polarisation, magnetisation and material fields

Name: _____ Class: _____ Date: _____

Total: 11 marks**KEY WORDS** electric polarisation • magnetisation

Objective

Relate free and bound charge to D , E and polarisation; Compare fixed-charge and fixed-voltage dielectric changes; Use magnetic constitutive response and free-current boundary conditions. Original public practice; not an ETS paper.

1 Key knowledge and worked examples

P is electric dipole moment per volume. $D = \epsilon_0 E + P$ obeys $\nabla \cdot D = \rho_{\text{free}}$. Bound charges obey $\rho_{\text{b}} = -\nabla \cdot P$ and $\sigma_{\text{b}} = P \cdot n$ with outward n . Uniform P can give surface charge but no bound bulk charge.

For a linear isotropic dielectric, $P = \epsilon_0 \chi_{\text{e}} E$ and $\epsilon_{\text{r}} = 1 + \chi_{\text{e}}$. In a fully filled large parallel-plate capacitor, $D = \sigma_{\text{free}}$ and $E = \sigma_{\text{free}} / \epsilon$. A dielectric need not have zero internal E .

$C = \epsilon A / d$. At fixed Q , $V = Q / C$ and $U = Q^2 / (2C)$ fall as C rises. At fixed V , $Q = CV$ and $U = CV^2 / 2$ rise. The voltage source exchanges energy. Normal D jumps by σ_{free} ; static tangential E is continuous.

M is magnetic dipole moment per volume; $B = \mu_0 (H + M)$. Linear $M = \chi_{\text{m}} H$ gives $B = \mu_0 (1 + \chi_{\text{m}}) H$. A long solenoid has $H \approx nI$. Normal B is continuous; tangential H jumps with free surface current. Hysteresis needs more than constant susceptibility.

■ Worked method

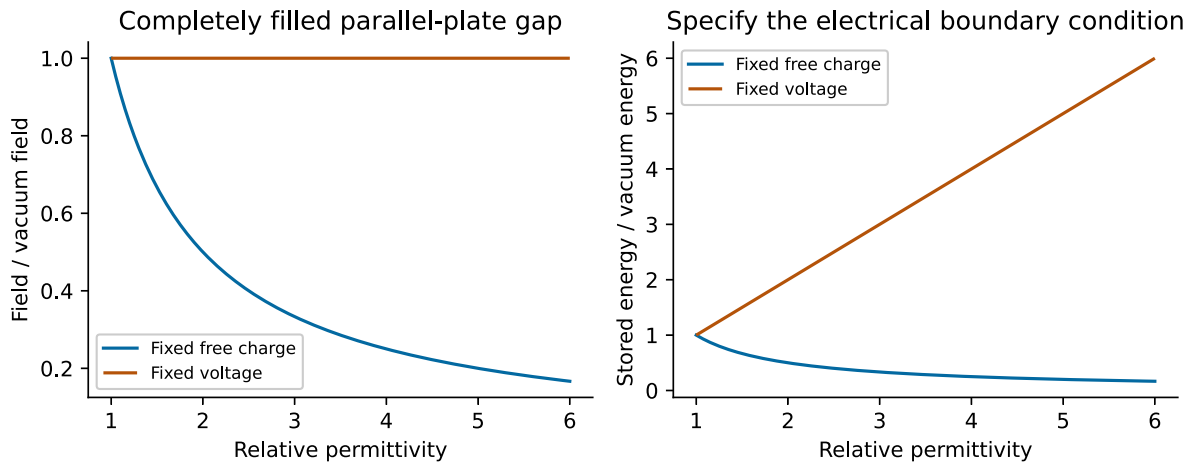
A capacitor is disconnected before inserting a linear dielectric with relative permittivity 4. Free charge stays fixed; capacitance becomes four times its original value.

$$V' = Q / (4C) = V / 4, \quad U' = Q^2 / (2 \times 4C) = U / 4.$$

If an ideal battery stays connected instead, V is fixed:

$$Q' = 4CV = 4Q, \quad U' = \frac{1}{2}(4C)V^2 = 4U.$$

The source exchanges energy. Do not compare isolated charge and fixed voltage as the same experiment.



2 Practice

2.1 Choose one answer. An isolated ideal parallel-plate capacitor is fully filled with a linear dielectric of $\epsilon_r=3$. Which pair gives voltage and stored-energy ratios? [1]

- **A** 3 and 3
- **B** $1/3$ and $1/3$
- **C** 1 and 3
- **D** $1/3$ and 3
- **E** 1 and 1

2.2 Choose one answer. Uniform electric polarisation _____ in a finite dielectric necessarily implies: [1]

- **A** Nonzero bound volume charge everywhere
- **B** Zero bound surface charge everywhere
- **C** Possible bound surface charge with zero bound bulk charge
- **D** Zero internal electric field as in a metal
- **E** Identical numerical B and H

2.3 In a linear magnetic material with $H=500$ A/m and $\chi_m=0.2$, $M=$ _____ A/m. Show your relation and units. [2]

