

2.6 Calculate and interpret mean, median, mode and weighted mean

Name: _____ Class: _____ Date: _____ Total: 24 marks

KEY WORDS mean 平均数 • median 中位数 • mode 众数

Objective

Calculate and interpret mean, median, mode and weighted mean. Original GAC004-aligned practice, not an official assessment. Show the method as well as the result. All applied scenarios are invented classroom problems.

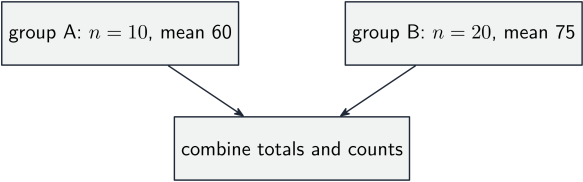
1 Key knowledge and worked examples

■ Key knowledge: the question determines which summary is useful

The **mean** 平均数 is sum divided by count. A frequency table uses $\bar{x} = \sum fx / \sum f$. The **median** 中位数 is the middle ordered value, or the mean of the middle two for an even count. The **mode** 众数 is the most frequent value; there can be several modes or no unique mode.

A weighted mean uses weights proportional to the relevant contributions. Do not average group means equally unless their group sizes are equal or equal weighting is explicitly intended. An extreme value can move the mean more than the median, but no measure is automatically best for every question. Report units and describe what the chosen summary represents.

■ Worked example: group size determines a combined mean



Known: group A has 10 scores with mean 60; group B has 20 with mean 75. Recover each group’s total before combining.

$$\bar{x} = \frac{n_A \bar{x}_A + n_B \bar{x}_B}{n_A + n_B}$$

$$\bar{x} = \frac{10(60) + 20(75)}{10 + 20} = 70$$

The unweighted mean of 60 and 75 would be 67.5, which ignores the unequal counts.

2 Practice

2.1 Find the mean of 4, 6, 8 and 10. [2]

2.2 Find the median and mode of 2, 3, 3, 7, 9. [2]

2.3 A frequency table has value 1 with frequency 2, value 2 with frequency 3, and value 4 with frequency 1. Find the mean. [3]

2.4 The ordered data are 2, 4, 6, 8. Find the median. Then replace 8 by 80 and find the new median and new mean. [3]

3 Exam-style questions

3.1 Group A has 8 learners with mean score 65. Group B has 12 learners with mean score 75. (a) Find the combined mean. (b) A single missing score is then added, bringing the combined mean for 21 learners to 70. Find that score. (c) Explain why averaging 65 and 75 equally is not the correct first calculation. [6]

3.2 Five supplied monthly incomes are 1000, 1100, 1200, 1300 and 6400 units. (a) Find the mean and median. (b) A report says, “Most people earn the mean.” Explain what the summaries do and do not show. (c) If the highest income changes to 8400 while the others stay fixed, find the new mean and median. Which measure changes more, and why? [8]