

6.6 Mixed practice: statistics and probability

Name: _____ Class: _____ Date: _____

Total: 29 marks

KEY WORDS independent events

Mixed practice: statistics and probability

Objective

Combine the topic-6 strands: density to frequency, grouped means with quartiles, ogive reads, Venn and complement shortcuts, and two-stage probability chains (objectives Foundation 6.1–6.3 and Higher 6.1–6.3).

1 Key knowledge and worked examples

One line per strand. Density is frequency over width – area is the frequency. Grouped mean by midpoints; quartiles by position; ogive reads at $n/2$, $n/4$, $3n/4$. $P(A \cup B) = P(A) + P(B) - P(A \cap B)$; complement for "at least one". Trees: multiply along, add between; without replacement adjusts the second branch.

2 Practice

2.1 A histogram bar of width 4 has density 3.5. Find its frequency. [2]

2.2 Find the mean of 6, 8, 10, 12, 14 [2]

2.3 Classes 0–6, 6–12, 12–24 hold frequencies 9, 10, 12. Which class has the highest density? [2]

2.4 $P(\text{rain})$ each independent day is 0.4. Find $P(\text{rain on exactly one of two days})$. [3]

2.5 Of 50 people, 30 speak French, 24 German, 10 both. Find $P(\text{a random person speaks neither})$. [3]

3 Exam-style questions

3.1 (*Original.*) A clinic records waiting times 0–10, 10–20, 20–30, 30–60 minutes with frequencies 8, 12, 15, 15. (a) Estimate the mean waiting time. (b) The manager claims “the typical wait is 30–60 minutes because that class holds the most”. Comment. [5]

3.2 (*Original.*) For the clinic’s data: (a) write the cumulative frequencies and plotting points; (b) estimate the median; (c) estimate how many patients waited more than 25 minutes. [6]

3.3 (*Original.*) A game: draw a counter from a bag of 3 gold, 5 silver, replace it, draw again. (a) Find $P(\text{at least one gold})$. (b) The rule changes to WITHOUT replacement: find $P(\text{at least one gold})$ now. (c) Explain why the answer increased. [6]
