

Solutions

2.1 $\bar{x} = 7$; $s^2 = \frac{2590-50(49)}{49} = \frac{140}{49} = 2.857$.

2.2 $X - Y \sim N(3, 5)$: $z = \frac{3}{\sqrt{5}} = 1.342$, $P = 0.9103$ (awrt 0.910).

2.3 9 cells $\rightarrow$ 6 after combining; $\text{df} = 6 - 1 - 2 = 3$.

3.1 Let $R = \sum_{i=1}^{28} S_i + \sum_{i=1}^5 C_i - 29P_1$. Then $E(R) = 28(18) + 5(25) - 29(15) = 504 + 125 - 435 = 194$ and $\text{Var}(R) = 28(0.0009) + 5(0.0009) + 29^2(0.04) = 0.0252 + 0.0045 + 33.64 = 33.6697$, so $R \sim N(194, 33.6697)$. The event is $R < 190$: $z = \frac{190-194}{\sqrt{33.6697}} = \frac{-4}{5.804} = -0.689$, so $P = 1 - 0.7549 = 0.245$ (awrt 0.245).

3.2 (a) $\bar{x} = \frac{92.0}{40} = 2.3$ s; $s^2 = \frac{216.32-40(2.3)^2}{39} = \frac{216.32-211.6}{39} = \frac{4.72}{39} = 0.121$. (b) With $n = 40$ large, substitute s^2 for σ^2 : $\text{SE} = \sqrt{0.121/40} = 0.055$, so the interval is $2.3 \pm 1.96(0.055) = 2.3 \pm 0.108 = (2.192, 2.408)$ s. (c) $H_0: \mu = 2.2$ vs $H_1: \mu \neq 2.2$: $z = \frac{2.3-2.2}{0.055} = 1.82$ against two-tailed critical ± 1.96 . Since $1.82 < 1.96$, do not reject H_0 – insufficient evidence, at the 5% level, against the manufacturer's claimed mean of 2.2 seconds (the true mean may still differ; 2.2 is simply consistent with the sample).

Local review guidance: the inequality rearranged before any distribution is written; the pallet coefficient squared in the variance; large-sample substitution justified by n ; two-tailed comparison with ± 1.96 and a contextual conclusion. This is authored classroom guidance.