

Solutions

2.1 $50 \pm 1.96 \times \frac{9}{\sqrt{36}} = 50 \pm 1.96 \times 1.5 = (47.06, 52.94).$

2.2 $z = \frac{50-52}{1.5} = -1.33$ vs critical -1.6449 : $-1.33 > -1.6449$, do not reject – insufficient evidence that $\mu < 52$.

2.3 The sample size is large enough that (i) $\frac{\bar{X}-\mu}{S/\sqrt{n}}$ is approximately $N(0, 1)$, and (ii) by the Central Limit Theorem the population itself need not be Normal.

3.1 (a) $\bar{y} = \frac{23200}{80} = 290$; $s_y^2 = \frac{6741351-80(290)^2}{79} = \frac{13351}{79} = 169$. (b) $H_0: \mu_x - \mu_y = 200$, $H_1: \mu_x - \mu_y > 200$. $z = \frac{(500 - 290) - 200}{\sqrt{1156/80 + 169/80}} = \frac{10}{\sqrt{16.5625}} = 2.457$. One-tailed 5%

critical value 1.6449. Since $2.457 > 1.6449$, reject H_0 – there is sufficient evidence, at the 5% level, that grey squirrels' mean weight is more than 200 g greater than red squirrels'. (c) The sample variances equal the corresponding population variances ($\sigma_x^2 = s_x^2$ and $\sigma_y^2 = s_y^2$).

3.2 (a) $503 \pm 2.5758 \times \frac{4}{\sqrt{49}} = 503 \pm 1.47 = (501.53, 504.47)$ ml. (b) $H_0: \mu = 500$ vs $H_1: \mu > 500$: $z = \frac{503-500}{4/7} = 5.25$ vs critical 2.3263. Reject H_0 – strong evidence the mean fill exceeds 500 ml (the machine overfills on average).

Local review guidance: the null gap subtracted in the numerator; combined standard error with both variances over their own n ; critical value with the correct tail and the conclusion in context. This is authored classroom guidance.