

7.4 Setting Up a Test for a Population Mean

Name: _____ Class: _____ Date: _____

Total: 10 marks

KEY WORDS degrees of freedom 自由度

Objective

Build the skills to answer exam questions on **setting up a test for a population mean**.**You must be able to:**

- state the hypotheses $H_0 : \mu = \mu_0$ and H_a
- write the test statistic $t = \frac{\bar{x} - \mu_0}{s/\sqrt{n}}$
- state the degrees of freedom $n - 1$

1 Worked examples

Study these first. Each one shows the method for a question type used later.

■ Hypotheses

- **Null** $H_0 : \mu = \mu_0$.
- **Alternative** $H_a : \mu \neq \mu_0$ (or $<$, or $>$).

■ Test statistic

$$t = \frac{\bar{x} - \mu_0}{s/\sqrt{n}}, \quad \text{df} = n - 1.$$

■ Example

$$\bar{x} = 52, \mu_0 = 50, s = 8, n = 16: t = \frac{52 - 50}{8/4} = \frac{2}{2} = 1.0.$$

2 Practice

2.1 State the null hypothesis for a test about a mean.

[1]

2.2 Write the test-statistic formula for a mean. [1]

2.3 $\bar{x} = 52$, $\mu_0 = 50$, $s = 8$, $n = 16$. Find the test statistic t . [2]

3 Exam-style questions

3.1 The test statistic for a mean is [1]

- | | |
|---|---|
| A | B |
| C | D |
- A** $\frac{\bar{x} - \mu_0}{s/\sqrt{n}}$
B $\frac{\hat{p} - p_0}{SE}$
C $\bar{x} \cdot s$
D $\frac{\mu_0}{n}$

3.2 The degrees of freedom for a one-sample mean test are [1]

- | | |
|---|---|
| A | B |
| C | D |
- A** n
B $n - 1$
C $n + 1$
D 0

3.3 A test of $\mu \neq 100$ has $\bar{x} = 104$, $s = 10$, $n = 25$.

(a) Write H_0 . [1]

(b) Compute t . [2]

(c) State the degrees of freedom. [1]