

4.12 The Geometric Distribution

Name: _____ Class: _____ Date: _____ **Total: 9 marks**

KEY WORDS geometric 几何 • independent 独立 • probability 概率 • random 随机
• random variable 随机变量

Objective

Build the skills to answer exam questions on **the geometric distribution**.

You must be able to:

- describe a **geometric** 几何 random variable as the number of trials until the first success
- use $P(\text{first success on trial } x) = (1 - p)^{x-1} p$
- find the mean, $\frac{1}{p}$

1 Worked examples

Study these first. Each one shows the method for a question type used later.

■ The geometric setting

Like a binomial, but instead of a fixed number of trials, a **geometric** random variable counts how many **trials until the first success** (independent trials, constant p).

■ Probability and mean

$$P(X = x) = (1 - p)^{x-1} p, \quad \mu_X = \frac{1}{p}.$$

With $p = 0.2$, the expected number of trials is $\frac{1}{0.2} = 5$.

2 Practice

2.1 State what a geometric random variable counts. [1]

2.2 For $p = 0.25$, find the mean number of trials to the first success. [2]

2.3 Write $P(\text{first success on trial } 1)$ in terms of p . [1]

3 Exam-style questions

3.1 A geometric random variable counts the [1]

- | | |
|---|---|
| A | B |
| C | D |
- A number of successes in n trials
 - B number of trials until the first success
 - C total number of trials
 - D number of failures only

3.2 The mean of a geometric distribution is [1]

- | | |
|---|---|
| A | B |
| C | D |
- A p
 - B $\frac{1}{p}$
 - C np
 - D $\sqrt{p}$

3.3 A game gives $P(\text{win}) = 0.1$ on each try.

(a) Find the expected number of tries until the first win. [2]

(b) Name the distribution. [1]