7.8 Setting Up a Test for the Difference of Two Population Means

Name: _____ Class: _____ Date: _____ **Total: 18 marks**

KEY WORDS two-sample t test t • matched pairs • standard error • conservative • twins • memory

Objective

Build the skills to answer exam questions on **setting up a test for a difference of two means** .

You must be able to:

- write hypotheses about $\mu_1 - \mu_2$
- check the conditions for a two-sample t test
- calculate the **two-sample t statistic** t

1 Key knowledge and worked examples

■ The two-sample t test

idea	rule
hypotheses	$H_0 : \mu_1 - \mu_2 = 0$; $H_a : \mu_1 - \mu_2 > 0, < 0$ or $\neq 0$
test statistic	$t = \dfrac{(\bar{x}_1 - \bar{x}_2) - 0}{\sqrt{s_1^2/n_1 + s_2^2/n_2}}$
degrees of freedom	technology, or the smaller of $n_1 - 1$ and $n_2 - 1$
conditions	Random (two independent samples, or random assignment); 10% for samples; Normal/Large Sample for each group
two-sample or paired	two separate groups of individuals: two-sample; two measurements on the same individuals or matched pairs: paired

Answer shapes: define μ_1 and μ_2 in words and keep the order of subtraction throughout.

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2 Practice

2.1 A teacher thinks that students who do homework online score higher on average than students who do it on paper. State the hypotheses. [2]

online homework mean μ_O paper homework mean μ_P

2.2 $\bar{x}_1 - \bar{x}_2 = 4$ and the standard error is 1.414. Calculate the test statistic. [2]



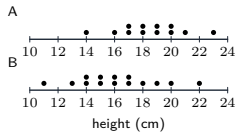
2.3 Twenty pairs of twins: one twin uses a new toothpaste and the other the usual one. Explain whether a two-sample t test is suitable. [2]



3 Exam-style questions

3.1 Plants were randomly assigned to fertilizer A or B. A: $n = 12$, mean 18.4 cm, SD 2.6 cm. B: $n = 14$, mean 16.1 cm, SD 3.0 cm.

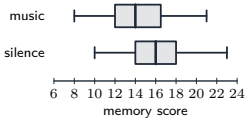
(a) State the hypotheses for a test of whether fertilizer A gives taller plants. [2]



(b) Calculate the test statistic. [2]

3.2 In an experiment, 50 volunteers were randomly assigned to study a word list with music or in silence, then took a memory test. Music: $n = 25$, mean 14.2, SD 3.5. Silence: $n = 25$, mean 16.0, SD 3.1.

(a) State the hypotheses for a test of whether music changes the mean score. [2]



(b) Check the conditions. [2]

(c) Calculate the standard error and the test statistic. [2]

(d) State the degrees of freedom you would use without technology, and explain. [2]

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