

4.14 Matrices Modeling Contexts

Name: _____ Class: _____ Date: _____

Total: 8 marks

KEY WORDS transition matrix 转移矩阵 • matrix 矩阵 • vector 向量

Objective

Build the skills to answer exam questions on **matrices modeling contexts**.

You must be able to:

- use a **transition matrix** 转移矩阵 to step a state vector forward

1 Worked examples

Study these first. Each one shows the method for a question type used later.

■ Transition matrices

A transition matrix models a process that moves between states each step:

$$\text{next state} = (\text{transition matrix}) \times (\text{current state}).$$

Repeated multiplication steps the model forward in time.

■ Example

State $\begin{bmatrix} \text{city} \\ \text{suburb} \end{bmatrix}$: each year a transition matrix redistributes the population; multiply to get next year's distribution.

2 Practice

2.1 State what a transition matrix models.

[1]

2.2 State how to get the next state from the current state.

[1]

2.3 If the current state is $\begin{bmatrix} 10 \\ 20 \end{bmatrix}$ and the transition is the identity matrix, state the next state. [1]

3 Exam-style questions

3.1 A transition matrix models [1]

- | | |
|---|---|
| A | B |
| C | D |
- A** a single number
B movement between states over steps
C a static picture
D an angle

3.2 The next state equals [1]

- | | |
|---|---|
| A | B |
| C | D |
- A** current state minus the matrix
B matrix times current state
C matrix plus current state
D the current state alone

3.3 Current state $\begin{bmatrix} 100 \\ 0 \end{bmatrix}$; transition $\begin{bmatrix} 0.5 & 0 \\ 0.5 & 1 \end{bmatrix}$ (half of state 1 moves to state 2 each step).

- (a) Compute the next state. [1]
(b) State the new value of state 1. [1]
(c) State the new value of state 2. [1]