

**2019****AP<sup>®</sup>** **CollegeBoard**

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# **AP<sup>®</sup> Physics C: Mechanics**

## **Scoring Guidelines Set 1**

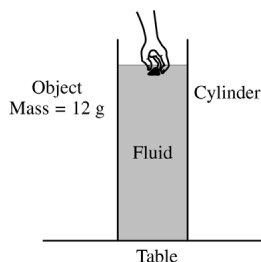
**2019 SCORING GUIDELINES****General Notes About 2019 AP Physics Scoring Guidelines**

1. The solutions contain the most common method of solving the free-response questions and the allocation of points for this solution. Some also contain a common alternate solution. Other methods of solution also receive appropriate credit for correct work.
2. The requirements that have been established for the paragraph-length response in Physics 1 and Physics 2 can be found on AP Central at <https://secure-media.collegeboard.org/digitalServices/pdf/ap/paragraph-length-response.pdf>.
3. Generally, double penalty for errors is avoided. For example, if an incorrect answer to part (a) is correctly substituted into an otherwise correct solution to part (b), full credit will usually be awarded. One exception to this may be cases when the numerical answer to a later part should be easily recognized as wrong, e.g., a speed faster than the speed of light in vacuum.
4. Implicit statements of concepts normally receive credit. For example, if use of the equation expressing a particular concept is worth 1 point, and a student's solution embeds the application of that equation to the problem in other work, the point is still awarded. However, when students are asked to derive an expression, it is normally expected that they will begin by writing one or more fundamental equations, such as those given on the exam equation sheet. For a description of the use of such terms as "derive" and "calculate" on the exams, and what is expected for each, see "The Free-Response Sections — Student Presentation" in the *AP Physics; Physics C: Mechanics, Physics C: Electricity and Magnetism Course Description* or "Terms Defined" in the *AP Physics 1: Algebra-Based Course and Exam Description* and the *AP Physics 2: Algebra-Based Course and Exam Description*.
5. The scoring guidelines typically show numerical results using the value  $g = 9.8 \text{ m/s}^2$ , but the use of  $10 \text{ m/s}^2$  is of course also acceptable. Solutions usually show numerical answers using both values when they are significantly different.
6. Strict rules regarding significant digits are usually not applied to numerical answers. However, in some cases answers containing too many digits may be penalized. In general, two to four significant digits are acceptable. Numerical answers that differ from the published answer due to differences in rounding throughout the question typically receive full credit. Exceptions to these guidelines usually occur when rounding makes a difference in obtaining a reasonable answer. For example, suppose a solution requires subtracting two numbers that should have five significant figures and that differ starting with the fourth digit (e.g., 20.295 and 20.278). Rounding to three digits will lose the accuracy required to determine the difference in the numbers, and some credit may be lost.

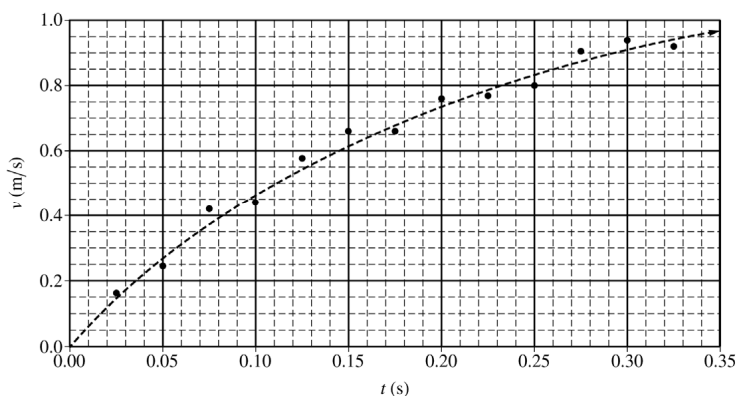
## 2019 SCORING GUIDELINES

## Question 1

15 points



In an experiment, students used video analysis to track the motion of an object falling vertically through a fluid in a glass cylinder. The object of  $m = 12\text{ g}$  is released from rest at the top of the column of fluid, as shown above. The data for the speed  $v$  of the falling object as a function of time  $t$  are graphed on the grid below. The dashed curve represents the best fit chosen by the students for these data.



(a)

- i. LO CHA-1.C, SP 7.A  
1 point

Does the speed of the object increase, decrease, or remain the same?

☐ Increase      ☐ Decrease      ☐ Remain the same

For selecting "Increase"

1 point

- ii. LO CHA-1.C, SP 4.D  
2 points

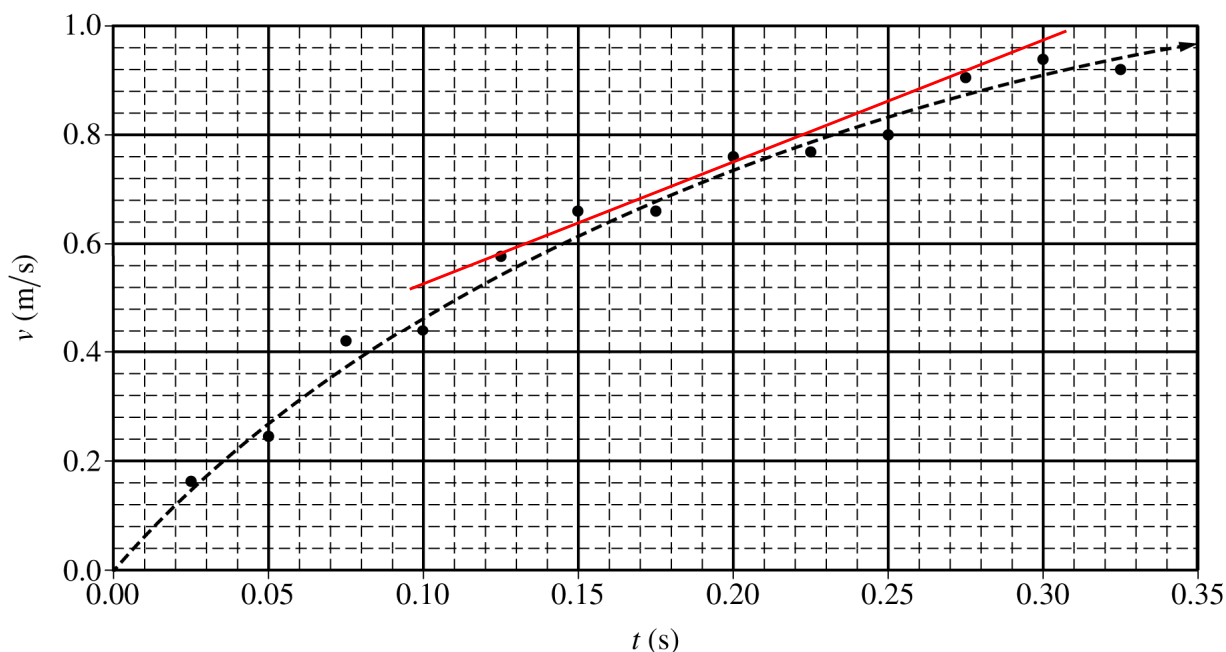
In a brief statement, describe the direction of the object's acceleration and how the magnitude of this acceleration changed as the object fell.

|                                                                                                                                                                                                                                         |         |
|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------|
| For a description that includes the direction of the acceleration as being "downwards"                                                                                                                                                  | 1 point |
| For a description that includes the decrease in the magnitude of the acceleration                                                                                                                                                       | 1 point |
| Example: Because the object is moving downwards and speeding up, the acceleration must be downwards. Because the slope of the graph of speed as a function of time is decreasing, the magnitude of the acceleration must be decreasing. |         |

## 2019 SCORING GUIDELINES

## Question 1 (continued)

(a) continued



- iii. LO CHA-1.C, SP 4.D, 6.C  
2 points

Using the graph, calculate an approximate value for the magnitude of the acceleration of the object at  $t = 0.20$  s.

|                                                                                                            |         |
|------------------------------------------------------------------------------------------------------------|---------|
| For calculating the slope of a trend line at $t = 0.20$ s                                                  | 1 point |
| $\text{slope} = a = \frac{\Delta v}{\Delta t} = \frac{(0.8 - 0.6) \text{ m/s}}{(0.226 - 0.136) \text{ s}}$ |         |
| For a correct answer using points from a tangent line                                                      | 1 point |
| $a = 2.22 \text{ m/s}^2$                                                                                   |         |

The students use the equation  $v = A(1 - e^{-Bt})$  to model the speed of the falling object and find the best-fit coefficients to be  $A = 1.18 \text{ m/s}$  and  $B = 5 \text{ s}^{-1}$ .

## 2019 SCORING GUIDELINES

## Question 1 (continued)

(b) Use the above equation to:

- i. LO CHA-1.B, SP 6.B, 6.C  
3 points

Derive an expression for the magnitude of the vertical displacement  $y(t)$  of the falling object as a function of time  $t$ .

|                                                                                                                                                                                                                |         |
|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------|
| For indicating that the vertical displacement is the integration of the velocity                                                                                                                               | 1 point |
| $\Delta y = \int v dt = \int A(1 - e^{-Bt}) dt$                                                                                                                                                                |         |
| For the equation for speed using appropriate limits or constant of integration                                                                                                                                 | 1 point |
| $\Delta y = \int_{t'=0}^{t'=t} A(1 - e^{-Bt'}) dt' = A \left[ t' - \frac{1}{-B} e^{-Bt'} \right]_{t'=0}^{t'=t} = A \left[ \left( t + \frac{1}{B} e^{-Bt} \right) - \left( 0 + \frac{1}{B} e^0 \right) \right]$ |         |
| For a correct answer                                                                                                                                                                                           | 1 point |
| $\Delta y = A \left( t + \frac{1}{B} (e^{-Bt} - 1) \right) = (1.18) \left( t + \frac{1}{5} (e^{-5t} - 1) \right)$                                                                                              |         |
| <u>Note:</u> Credit given for using $A$ and $B$ or plugging in the given values                                                                                                                                |         |

- ii. LO INT-1.C.d, SP 6.B, 6.C  
3 points

Derive an expression for the magnitude of the net force  $F(t)$  exerted on the object as it falls through the fluid as a function of time  $t$ .

|                                                                                         |         |
|-----------------------------------------------------------------------------------------|---------|
| For attempting the derivative of the equation for speed                                 | 1 point |
| $a = \frac{dv}{dt} = \frac{d}{dt} [A(1 - e^{-Bt})]$                                     |         |
| For a correct equation for the acceleration                                             | 1 point |
| $a = ABe^{-Bt}$                                                                         |         |
| For multiplying the equation above by the mass of the object                            | 1 point |
| $F = ma = m(ABe^{-Bt}) = mABe^{-Bt}$                                                    |         |
| $F = (.012)(1.18)(5)e^{-5t} = 0.071e^{-5t}$                                             |         |
| <u>Note:</u> Credit given for using $A$ , $B$ , and $m$ or plugging in the given values |         |

**2019 SCORING GUIDELINES****Question 1 (continued)**

(c)

The students repeat the experiment with a taller glass cylinder that is filled with the same fluid. The cylinder is tall enough so that the object reaches a constant speed.

i. LO INT-1.I, SP 7.A, 7.C

2 points

Determine the constant speed of the object.

Justify your answer.

|                                                                                                                                                                                                                                                               |         |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------|
| For stating the constant speed is $v = A$                                                                                                                                                                                                                     | 1 point |
| For indicating that the constant speed can be determined by setting the time equal to infinity                                                                                                                                                                | 1 point |
| Example: After a long time, the falling object will reach a terminal constant speed in the fluid. This can be determined by setting the time $t$ in the equation for speed equal to infinity. By doing this, the constant speed is determined to be $v = A$ . |         |
| <u>Note:</u> Credit given for solving mathematically                                                                                                                                                                                                          |         |

ii. LO INT-1.H.b, SP 7.A, 7.C

2 points

Determine the force exerted by the fluid on the object at this time. Justify your answer.

|                                                                                                                                                                                                                                                                                                                                             |         |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------|
| For indicating that the net force is equal to zero when the object moves with constant speed                                                                                                                                                                                                                                                | 1 point |
| For indicating the resistive force is equal to the weight of the object at this time                                                                                                                                                                                                                                                        | 1 point |
| Example: When the falling object reaches a constant speed in the fluid, the net force must be zero. Because the only vertical forces acting on the object are Earth's gravitational pull and the resistive force of the fluid, these two forces must be equal. So, the resistive force must be equal to the weight of the object or 0.12 N. |         |
| <u>Note:</u> Credit given for solving mathematically                                                                                                                                                                                                                                                                                        |         |

**2019 SCORING GUIDELINES****Question 1 (continued)****Learning Objectives**

**CHA-1.B:** Determine functions of position, velocity, and acceleration that are consistent with each other, for the motion of an object with a nonuniform acceleration.

**CHA-1.C:** Describe the motion of an object in terms of the consistency that exists between position and time, velocity and time, and acceleration and time.

**INT-1.C.d:** Derive an expression for the net force on an object in translational motion.

**INT-1.H.b:** Describe the acceleration, velocity, or position in relation to time for an object subject to a resistive force (with different initial conditions, i.e., falling from rest or projected vertically).

**INT-1.I:** Calculate the terminal velocity of an object moving vertically under the influence of a resistive force of a given relationship.

**Science Practices**

**4.D:** Select relevant features of a graph to describe a physical situation or solve problems.

**6.B:** Apply an appropriate law, definition, or mathematical relationship to solve a problem.

**6.C:** Calculate an unknown quantity with units from known quantities, by selecting and following a logical computational pathway.

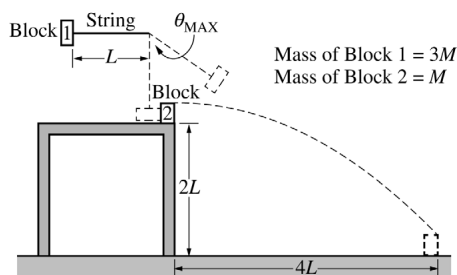
**7.A:** Make a scientific claim.

**7.C:** Support a claim with evidence from physical representations.

## 2019 SCORING GUIDELINES

## Question 2

15 points



Note: Figure not drawn to scale.

A pendulum of length  $L$  consists of block 1 of mass  $3M$  attached to the end of a string. Block 1 is released from rest with the string horizontal, as shown above. At the bottom of its swing, block 1 collides with block 2 of mass  $M$ , which is initially at rest at the edge of a table of height  $2L$ . Block 1 never touches the table. As a result of the collision, block 2 is launched horizontally from the table, landing on the floor a distance  $4L$  from the base of the table. After the collision, block 1 continues forward and swings up. At its highest point, the string makes an angle  $\theta_{\text{MAX}}$  to the vertical. Air resistance and friction are negligible. Express all algebraic answers in terms of  $M$ ,  $L$ , and physical constants, as appropriate.

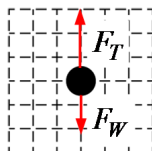
- (a) LO CON-2.C.a, SP 5.E  
1 point

Determine the speed of block 1 at the bottom of its swing just before it makes contact with block 2.

|                                                                                |  |         |
|--------------------------------------------------------------------------------|--|---------|
| For correctly calculating the speed of block 1                                 |  | 1 point |
| $U_{g1} = K_2 \therefore mgh = \frac{1}{2}mv^2 \therefore gL = \frac{1}{2}v^2$ |  |         |
| $v = \sqrt{2gL}$                                                               |  |         |
| Note: Credit is earned even if no work is shown.                               |  |         |

- (b) LO INT-2.B.b, SP 3.D  
2 points

On the dot below, which represents block 1, draw and label the forces (not components) that act on block 1 just before it makes contact with block 2. Each force must be represented by a distinct arrow starting on, and pointing away from, the dot. Forces with greater magnitude should be represented by longer vectors.



|                                                                                          |  |         |
|------------------------------------------------------------------------------------------|--|---------|
| For correctly drawing and labeling the weight of the block and the tension in the string |  | 1 point |
| For drawing the tension longer than the weight of the block                              |  | 1 point |
| Note: A maximum of one point can be earned if there are any extraneous vectors.          |  |         |

## 2019 SCORING GUIDELINES

## Question 2 (continued)

- (c) LO INT-2.B.b, SP 5.A, 5.E  
2 points

Derive an expression for the tension  $F_T$  in the string when the string is vertical just before block 1 makes contact with block 2. If you need to draw anything other than what you have shown in part (b) to assist in your solution, use the space below. Do NOT add anything to the figure in part (b).

|                                                                              |  |         |
|------------------------------------------------------------------------------|--|---------|
| For using an appropriate equation to calculate the tension in the string     |  | 1 point |
| $F_T = mg + ma_C = mg + \frac{mv^2}{r} = 3Mg + \frac{(3M)(\sqrt{2gL})^2}{L}$ |  |         |
| For a correct answer                                                         |  | 1 point |
| $F_T = 9Mg$                                                                  |  |         |

For parts (d)–(g), the value for the length of the pendulum is  $L = 75$  cm.

- (d) LO CHA-2.C, SP 6.A, 6.C  
2 points

Calculate the time between the instant block 2 leaves the table and the instant it first contacts the floor.

|                                                                                                                                                                                    |  |         |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--|---------|
| For using a correct kinematic equation to calculate the time                                                                                                                       |  | 1 point |
| $\Delta y = v_1 t + \frac{1}{2}at^2 = \frac{1}{2}at^2 \therefore t = \sqrt{\frac{2\Delta y}{a}} = \sqrt{\frac{2(2L)}{g}} = \sqrt{\frac{(4)(0.75 \text{ m})}{(9.8 \text{ m/s}^2)}}$ |  |         |
| For a correct answer                                                                                                                                                               |  | 1 point |
| $t = 0.55 \text{ s}$                                                                                                                                                               |  |         |

- (e) LO CHA-2.C, SP 6.A, 6.C  
2 points

Calculate the speed of block 2 as it leaves the table.

|                                                                       |  |         |
|-----------------------------------------------------------------------|--|---------|
| For using a correct kinematic equation to calculate the speed         |  | 1 point |
| $\Delta x = vt \therefore v = \frac{\Delta x}{t} = \frac{4L}{t}$      |  |         |
| For substituting the time from part (d) into equation above           |  | 1 point |
| $v = \frac{(4)(0.75 \text{ m})}{(0.55 \text{ s})} = 5.45 \text{ m/s}$ |  |         |

## 2019 SCORING GUIDELINES

## Question 2 (continued)

- (f) LO CON-4.E.a, SP 6.B, 6.C  
3 points

Calculate the speed of block 1 just after it collides with block 2.

|                                                                                                                    |         |
|--------------------------------------------------------------------------------------------------------------------|---------|
| For indicating the use of the correct conservation of momentum to calculate the speed                              | 1 point |
| $p_i = p_f \therefore m_1 v_{1i} + m_2 v_{2i} = m_1 v_{1f} + m_2 v_{2f}$                                           |         |
| For correctly substituting the mass into equation above                                                            | 1 point |
| $(3M)v_{1i} + 0 = (3M)v_{1f} + (M)v_{2f}$                                                                          |         |
| For substituting the speeds from parts (a) and (e) into equation above                                             | 1 point |
| $v_{1f} = \frac{(3M)v_{1i} - (M)v_{2f}}{(3M)} = \frac{(3M)\sqrt{2gL} - (M)v_{2f}}{(3M)}$                           |         |
| $v_{1f} = \frac{(3)\sqrt{(2)(9.8 \text{ m/s}^2)(0.75 \text{ m})} - (1)(5.45 \text{ m/s})}{(3)} = 2.02 \text{ m/s}$ |         |
| $(v_{1f} = 2.06 \text{ m/s when using } g = 10 \text{ m/s}^2)$                                                     |         |

- (g) LO CON-2.C.a, SP 6.B, 6.C  
3 points

Calculate the angle  $\theta_{\text{MAX}}$  that the string makes with the vertical, as shown in the original figure, when block 1 is at its highest point after the collision.

|                                                                                                                                                                   |         |
|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------|
| For using conservation of energy to calculate the angle                                                                                                           | 1 point |
| $K_1 = U_{g2}$                                                                                                                                                    |         |
| $\frac{1}{2}mv^2 = mgh$                                                                                                                                           |         |
| For correctly substituting $h = L(1 - \cos\theta)$ into the equation above                                                                                        | 1 point |
| For correctly substituting the speed from part (f) into the equation above                                                                                        | 1 point |
| $\frac{1}{2}mv^2 = mgL(1 - \cos\theta) \therefore \frac{v^2}{2gL} = 1 - \cos\theta$                                                                               |         |
| $\theta = \cos^{-1}\left(1 - \frac{v^2}{2gL}\right) = \cos^{-1}\left(1 - \frac{(2.02 \text{ m/s})^2}{(2)(9.8 \text{ m/s}^2)(0.75 \text{ m})}\right) = 43.5^\circ$ |         |
| $(\theta = 44.1^\circ \text{ when using } g = 10 \text{ m/s}^2)$                                                                                                  |         |

**2019 SCORING GUIDELINES****Question 2 (continued)****Learning Objectives**

**CHA-2.C:** Calculate kinematic quantities of an object in projectile motion, such as displacement, velocity, speed, acceleration, and time, given initial conditions of various launch angles, including a horizontal launch at some point in its trajectory.

**INT-2.B.b:** Describe forces that are exerted on objects undergoing horizontal circular motion, vertical circular motion, or horizontal circular motion on a banked curve.

**CON-2.C.a:** Calculate unknown quantities (e.g., speed or positions of an object) that are in a conservative system of connected objects, such as the masses in an Atwood machine, masses connected with pulley/string combinations, or the masses in a modified Atwood machine.

**CON-4.E.a:** Calculate the changes in speeds, changes in velocities, changes in kinetic energy, or changes in momenta of objects in all types of collisions (elastic or inelastic) in one dimension, given the initial conditions of the objects.

**Science Practices**

**3.D:** Create appropriate diagrams to represent physical situations.

**5.A:** Select an appropriate law, definition, or mathematical relationship or model to describe a physical situation.

**5.E:** Derive a symbolic expression from known quantities by selecting and following a logical algebraic pathway.

**6.A:** Extract quantities from narratives or mathematical relationships to solve problems.

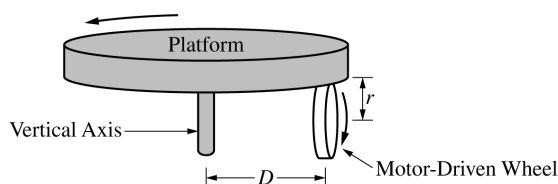
**6.B:** Apply an appropriate law, definition, or mathematical relationship to solve a problem.

**6.C:** Calculate an unknown quantity with units from known quantities, by selecting and following a logical computational pathway.

## 2019 SCORING GUIDELINES

## Question 3

15 points



A horizontal circular platform with rotational inertia  $I_P$  rotates freely without friction on a vertical axis. A small motor-driven wheel that is used to rotate the platform is mounted under the platform and touches it. The wheel has radius  $r$  and touches the platform a distance  $D$  from the vertical axis of the platform, as shown above. The platform starts at rest, and the wheel exerts a constant horizontal force of magnitude  $F$  tangent to the wheel until the platform reaches an angular speed  $\omega_p$  after time  $\Delta t$ . During time  $\Delta t$ , the wheel stays in contact with the platform without slipping.

- (a) LO INT-7.A.b, CHA-4.A.b, SP 5.A, 5.E  
2 points

Derive an expression for the angular speed  $\omega_p$  of the platform. Express your answer in terms of  $I_P$ ,  $r$ ,  $D$ ,  $F$ ,  $\Delta t$ , and physical constants, as appropriate.

|                                                                                                |  |  |         |
|------------------------------------------------------------------------------------------------|--|--|---------|
| For correctly substituting into the rotational form of Newton's second law                     |  |  | 1 point |
| $\tau = I\alpha \therefore FD = I_P\alpha$                                                     |  |  |         |
| $\alpha = \frac{FD}{I_P}$                                                                      |  |  |         |
| For correctly substituting into a rotational kinematic equation to calculate the angular speed |  |  | 1 point |
| $\omega_2 = \omega_1 + \alpha\Delta t = 0 + \left(\frac{FD}{I_P}\right)\Delta t$               |  |  |         |
| $\omega_p = \frac{FD\Delta t}{I_P}$                                                            |  |  |         |

- (b) LO INT-7.D.a, SP 5.A, 5.E  
2 points

Determine an expression for the kinetic energy of the platform at the moment it reaches angular speed  $\omega_p$ . Express your answer in terms of  $I_P$ ,  $r$ ,  $D$ ,  $F$ ,  $\Delta t$ , and physical constants, as appropriate.

|                                                                                                   |  |  |         |
|---------------------------------------------------------------------------------------------------|--|--|---------|
| For using the equation for rotational kinetic energy                                              |  |  | 1 point |
| $K = \frac{1}{2}I\omega_p^2 = \left(\frac{1}{2}\right)(I_P)\left(\frac{FD\Delta t}{I_P}\right)^2$ |  |  |         |
| For an answer consistent with part (a)                                                            |  |  | 1 point |
| $K = \frac{(FD\Delta t)^2}{2I_P}$                                                                 |  |  |         |

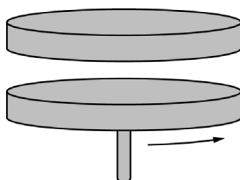
## 2019 SCORING GUIDELINES

## Question 3 (continued)

- (c) LO INT-7.C, SP 5.A, 5.E  
2 points

Derive an expression for the angular speed of the wheel  $\omega_W$  when the platform has reached angular speed  $\omega_P$ . Express your answer in terms of  $D$ ,  $r$ ,  $\omega_P$ , and physical constants, as appropriate.

|                                                                                                |  |         |
|------------------------------------------------------------------------------------------------|--|---------|
| For indicating that the linear speed of the platform is equal to the linear speed of the wheel |  | 1 point |
| $v_P = v_W$ OR $(r\omega)_P = (r\omega)_W$                                                     |  |         |
| For correctly relating the linear speeds to the angular speeds in the above equation           |  | 1 point |
| $D\omega_P = r\omega_W$                                                                        |  |         |
| $\omega_W = \frac{D\omega_P}{r}$                                                               |  |         |



When the platform is spinning at angular speed  $\omega_P$ , the motor-driven wheel is removed. A student holds a disk directly above and concentric with the platform, as shown above. The disk has the same rotational inertia  $I_P$  as the platform. The student releases the disk from rest, and the disk falls onto the platform. After a short time, the disk and platform are observed to be rotating together at angular speed  $\omega_f$ .

- (d) LO CON-5.D.c, SP 5.A, 5.E  
2 points

Derive an expression for  $\omega_f$ . Express your answer in terms of  $\omega_P$ ,  $I_P$ , and physical constants, as appropriate.

|                                                                  |  |         |
|------------------------------------------------------------------|--|---------|
| For using an expression for the conservation of angular momentum |  | 1 point |
| $L_1 = L_2 \therefore I_1\omega_1 = I_2\omega_2$                 |  |         |
| For correctly substituting into the above equation               |  | 1 point |
| $I\omega_P = (2I)\omega_f$                                       |  |         |
| $\omega_f = \frac{1}{2}\omega_P$                                 |  |         |

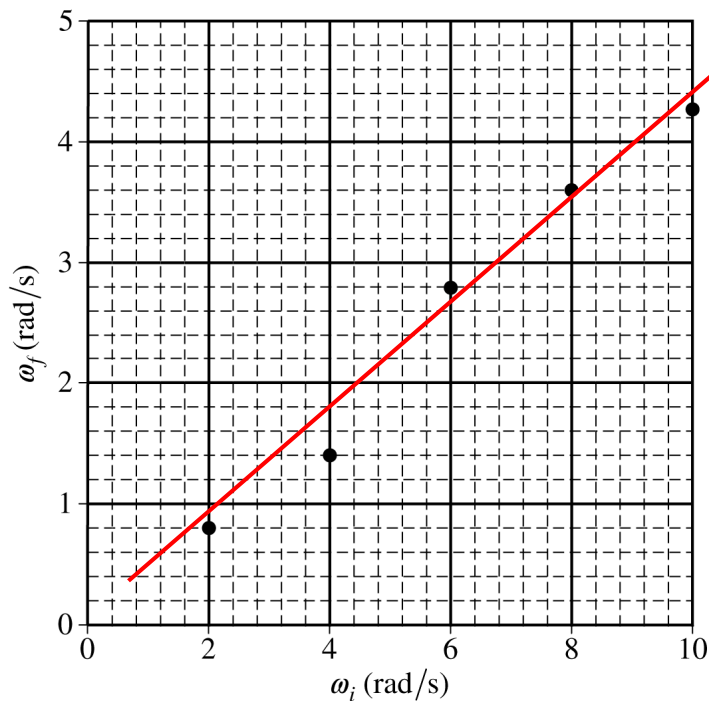
## 2019 SCORING GUIDELINES

## Question 3 (continued)

A student now uses the rotating platform ( $I_P = 3.1 \text{ kg} \cdot \text{m}^2$ ) to determine the rotational inertia  $I_U$  of an unknown object about a vertical axis that passes through the object's center of mass. The platform is rotating at an initial angular speed  $\omega_i$  when the unknown object is dropped with its center of mass directly above the center of the platform. The platform and object are observed to be rotating together at angular speed  $\omega_f$ . Trials are repeated for different values of  $\omega_i$ . A graph of  $\omega_f$  as a function of  $\omega_i$  is shown on the axes below.

- (e)
- i. LO CON-5.D.c, SP 4.C  
1 points

On the graph on the previous page, draw a best-fit line for the data.



|                                                      |         |
|------------------------------------------------------|---------|
| For an appropriate best-fit line for the graph above | 1 point |
|------------------------------------------------------|---------|

## 2019 SCORING GUIDELINES

## Question 3 (continued)

(e) continued

- ii. LO CON-5.D.c, SP 4.D, 6.C  
2 points

Using the straight line, calculate the rotational inertia of the unknown object  $I_U$  about a vertical axis passing through its center of mass.

|                                                                                                                                                                                      |         |
|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------|
| For using conservation of angular momentum to derive an expression that includes $I_U$                                                                                               | 1 point |
| $L_i = L_f \therefore I_P \omega_i = (I_P + I_U) \omega_f$                                                                                                                           |         |
| $I_U = I_P \left( \frac{\omega_i}{\omega_f} \right) - I_P$                                                                                                                           |         |
| For substituting points from the best-fit line into the expression above                                                                                                             | 1 point |
| $I_U = (3.1 \text{ kg}\cdot\text{m}^2) \left( \frac{(4.0 - 1.0) \text{ rad/s}}{(9.3 - 2.4) \text{ rad/s}} \right) - (3.1 \text{ kg}\cdot\text{m}^2) = 4.1 \text{ kg}\cdot\text{m}^2$ |         |
| <u>Note:</u> The point (0, 0) can be used implicitly if the best-fit line goes through the origin.                                                                                   |         |

- (f) LO CON-5.D.c, SP 7.A, 7.C  
2 points

The kinetic energy of the spinning platform before the object is dropped on it is  $K_i$ . The total kinetic energy of the platform-object system when it reaches angular speed  $\omega_f$  is  $K_f$ . Which of the following expressions is true?

\_\_\_  $K_f < K_i$       \_\_\_  $K_f = K_i$       \_\_\_  $K_f > K_i$

Justify your answer.

|                                                                                                                                                                          |         |
|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------|
| For selecting $K_f < K_i$ with an attempt at a relevant justification                                                                                                    | 1 point |
| For a correct justification                                                                                                                                              | 1 point |
| Example: Because the two disks will be rotating with the same final angular speed, this is an inelastic collision, and kinetic energy will be lost during the collision. |         |

## 2019 SCORING GUIDELINES

## Question 3 (continued)

- (g) LO INT-6.E, SP 7.A, 7.C  
2 points

One of the students observes that the center of mass of the object is not actually aligned with the axis of the platform. Is the experimental value of  $I_U$  obtained in part (e) greater than, less than, or equal to the actual value of the rotational inertia of the unknown object about a vertical axis that passes through its center of mass?

\_\_\_\_\_ Greater than      \_\_\_\_\_ Less than      \_\_\_\_\_ Equal to

Justify your answer.

|                                                                                                                                                                                                                                                                                      |         |
|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------|
| For selecting “Greater than” with an attempt at a relevant justification                                                                                                                                                                                                             | 1 point |
| For a correct justification                                                                                                                                                                                                                                                          | 1 point |
| Example: Because the center of mass of the object is off the axis of the platform, the parallel axis theorem would be used to calculate the total rotational inertia of the platform-object system. Using $I = I_{CM} + Mh^2$ , the experimental value will be increased by $Mh^2$ . |         |

## Learning Objectives

**INT-6.E:** Derive the moments of inertia of an extended rigid body for different rotational axes (parallel to an axis that goes through the object’s center of mass) if the moment of inertia is known about an axis through the object’s center of mass.

**CHA-4.A.b:** Calculate unknown quantities such as angular positions, displacement, angular speeds, or angular acceleration of a rigid body in uniformly accelerated motion, given initial conditions.

**INT-7.A.b:** Calculate unknown quantities such as net torque, angular acceleration, or moment of inertia for a rigid body undergoing rotational acceleration.

**INT-7.C:** Derive expressions for physical systems such as Atwood Machines, pulleys with rotational inertia, or strings connecting discs or strings connecting multiple pulleys that relate linear or translational motion characteristics to the angular motion characteristics of rigid bodies in the system that are: **(a)** rolling (or rotating on a fixed axis) without slipping. **(b)** rotating and sliding simultaneously.

**INT-7.D.a:** Calculate the rotational kinetic energy of a rotating rigid body.

**CON-5.D.c:** Calculate the changes of angular momentum of each disc in a rotating system of two rotating discs that collide with each other inelastically about a common rotational axis.

## Science Practices

**4.C:** Linearize data and/or determine a best-fit line or curve.

**4.D:** Select relevant features of a graph to describe a physical situation or solve problems.

**5.A:** Select an appropriate law, definition, or mathematical relationship or model to describe a physical situation.

**5.E:** Derive a symbolic expression from known quantities by selecting and following a logical algebraic pathway.

**6.C:** Calculate an unknown quantity with units from known quantities, by selecting and following a logical computational pathway.

**7.A:** Make a scientific claim.

**7.C:** Support a claim with evidence from physical representations.