

2015 SCORING GUIDELINES

Question 2

15 points total

Distribution
of points

(a)

i. 2 points

Using Ohm's law:

$$V = IR$$

For a correct application of Kirchhoff's loop rule

$$\mathcal{E} = Ir + IR$$

$$I = \frac{\mathcal{E}}{(r + R)}$$

For a correct expression for the measured voltage across the variable resistor

$$V = \frac{\mathcal{E}}{(r + R)} R$$

1 point

1 point

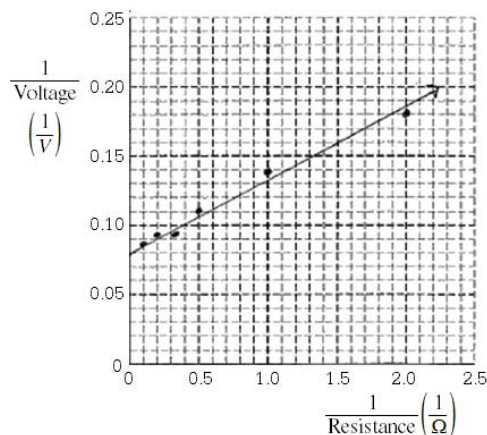
ii. 1 point

For an expression of $1/V$ as a function of $1/R$ consistent with answer from part (a)(i)

$$\frac{1}{V} = \left(\frac{r}{\mathcal{E}}\right) \frac{1}{R} + \frac{1}{\mathcal{E}}$$

1 point

(b) 4 points



For correctly labeling both axes with variables and units

1 point

For correctly scaling both axes with an acceptable and appropriate scale

1 point

For correctly plotting the data points

1 point

For correctly drawing a straight line that best represents the data

1 point

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Question 2 (continued)

Distribution
of points

(c)

i. 2 points

For using a value for the y-intercept consistent with the straight line drawn in part (b)

1 point

$$y = mx + b$$

$$b = 0.080 \text{ 1/V}$$

For a correct substitution into the equation from part (a)(ii)

1 point

$$\frac{1}{V} = \frac{(r + R)}{\mathcal{E}} \frac{1}{R}$$

$$\frac{1}{V} = \frac{r}{\mathcal{E}} \frac{1}{R} + \frac{1}{\mathcal{E}}$$

$$b = 1/\mathcal{E}$$

$$\mathcal{E} = 1/(0.080 \text{ 1/V})$$

$$\mathcal{E} = 12.5 \text{ V}$$

ii. 2 points

For calculating the slope using the straight line from part (b) and not data points

1 point

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{(0.151 - 0.100)}{(1.50 - 0.40)} = 0.0463 \text{ } \Omega/\text{V}$$

For a correct substitution into equation from part (a)(ii)

1 point

$$m = \frac{r}{\mathcal{E}}$$

$$r = m\mathcal{E}$$

$$r = (0.0463 \text{ } \Omega/\text{V})(12.5 \text{ V})$$

$$r = 0.58 \text{ } \Omega$$

(d) 2 points

For using Ohm's law

1 point

$$\mathcal{E} = Ir$$

For a correct substitution of values from part (c):

1 point

$$(12.5 \text{ V}) = I(0.58 \text{ } \Omega)$$

$$I = 21.6 \text{ A}$$

(e) 2 points

For selecting "The voltmeter with high resistance"

1 point

For a correct justification

1 point

Example: The voltmeter acts like a resistor in a circuit with the battery. It will measure the potential difference across its own internal resistance. The higher its internal resistance, the closer its potential difference will be to the emf of the battery.

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Question 3

15 points total

Distribution
of points

(a) 3 points

For properly using a correct equation to calculate the magnetic flux

$$\Phi_B = \int \vec{B} \cdot d\vec{A}$$

For correct substitution of the area and trigonometric function

$$\Phi_B = BA(\cos\theta) = B\pi r^2(\cos\theta)$$

For correct substitution into the above equation

$$\Phi_B = 4(1 - 0.2t)\pi(0.10\text{ m})^2(\cos 60^\circ)$$

$$\Phi_B = 0.063 - 0.013t \quad (\text{or in terms of } a \text{ and } b, \Phi_B = a(1 - bt)(0.016))$$

1 point

1 point

1 point

(b) 2 points

For using a correct equation to solve for the emf

$$\mathcal{E} = -\frac{d\Phi_B}{dt}$$

Substituting the expression from part (a):

$$\mathcal{E} = \frac{d}{dt}(0.063 - 0.013t)$$

For an answer consistent with part (a)

$$\mathcal{E} = 0.013\text{ V}$$

Note: Any sign on the answer is ignored.

1 point

1 point

(c) i. 1 point

For a substitution into Ohm's law consistent with the answer from part (b)

$$V = IR$$

$$I = \frac{(0.013\text{ V})}{(50\ \Omega)}$$

$$I = 2.6 \times 10^{-4}\text{ A}$$

1 point

ii. 2 points

The correct choice is "Counterclockwise".

For a justification that incorporates that the original magnetic field is changing

For a justification that correctly relates the induced current to the direction of a new magnetic field created by that current

Example: Looking down at the loop from P , the vertical component of the magnetic field of the loop is upward and decreasing. To oppose this change, the current in the loop must create a magnetic field that is directed upward at point P .

This requires a counterclockwise current in the loop.

1 point

1 point

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Question 3 (continued)

Distribution
of points

(d) 2 points

For using a correct equation to calculate the energy dissipated

$$E = Pt = I^2 R t \quad \text{or} \quad E = Pt = (\mathcal{E}^2 / R) t$$

For a substitution into either of the above equations with the answer from part (c)(i) or part (b)

$$E = (2.6 \times 10^{-4}\text{ A})^2 (50\ \Omega)(4.0\text{ s}) \quad \text{or} \quad E = \frac{(0.013\text{ V})^2}{(50\ \Omega)} (4.0\text{ s})$$

$$E = 1.4 \times 10^{-5}\text{ J}$$

1 point

1 point

(e) 4 points

For selecting both "Zero" for the net magnetic force and "Nonzero" for the Net magnetic torque

1 point

For indicating the forces on directly opposite sides of the loop are in opposite directions

1 point

For concluding that the forces cancel & net force is zero

1 point

For indicating that the torques add & net torque is nonzero

1 point

Example: Since the current changes direction relative to the magnetic field as you go around the loop, the magnetic field will exert force of equal magnitude but opposite direction on opposite sides of the loop. These forces all cancel out resulting in zero net force. However, since this force is up on one side of the loop and down on the other side of the loop, this will create torques that rotate the loop in the same direction. Therefore, the net torque is not zero.

Units 1 point

For correct units on at least two parts with a calculated numerical answer and no incorrect units

1 point