

8.6 Gauss's Law

Name: _____ Class: _____ Date: _____

Total: 10 marks

KEY WORDS gauss's law 高斯定律 • gaussian surface 高斯面 • electric field 电场
• electric flux 电通量 • conductor 导体

Objective

Build the skills to answer exam questions on **Gauss's law**.**You must be able to:**

- state **Gauss's law** 高斯定律, $\oint \vec{E} \cdot d\vec{A} = \frac{Q_{\text{enc}}}{\epsilon_0}$
- choose a **Gaussian surface** 高斯面 whose symmetry makes $\vec{E}$ constant and perpendicular
- apply Gauss's law to spherical, cylindrical, and planar distributions
- explain why $\vec{E} = 0$ inside a conductor in electrostatic equilibrium

1 Worked examples

Study these first. Each one shows the method for a question type used later.

■ Gauss's law

$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{\text{enc}}}{\epsilon_0}$: the net flux through a closed surface equals the enclosed charge divided by ϵ_0 .

■ Choose the symmetry

Pick a Gaussian surface (sphere, cylinder, box) on which E is constant and either perpendicular or parallel to the surface, so the integral becomes $E \times A$.

■ A point charge

For a sphere of radius r around charge q : $E(4\pi r^2) = \frac{q}{\epsilon_0}$, giving $E = \frac{kq}{r^2}$. Inside a conductor at equilibrium, no charge is enclosed, so $E = 0$.

2 Practice

2.1 State Gauss's law. [1]

2.2 State the electric field inside a conductor in electrostatic equilibrium. [1]

2.3 A charge of 5.0×10^{-9} C is enclosed by a closed surface ($\epsilon_0 = 8.85 \times 10^{-12}$). Find the flux through it. [2]

3 Exam-style questions

3.1 Gauss's law relates the flux through a closed surface to the [1]

- A** total field everywhere
- B** charge enclosed
- C** surface area
- D** current

3.2 Inside a charged conducting sphere in equilibrium, the electric field is [1]

- A** kq/r^2
- B** zero
- C** at its maximum
- D** infinite

3.3 A point charge $+8.0 \times 10^{-9}$ C sits at the centre of a spherical surface of radius 0.20 m ($\epsilon_0 = 8.85 \times 10^{-12}$, $k = 8.99 \times 10^9$).

(a) Find the flux through the sphere. [2]

(b) Find the field at the surface. [2]

Solutions

2.1 the net electric flux through a closed surface equals the enclosed charge divided by ϵ_0 .

2.2 zero.

$$\mathbf{2.3} \quad \Phi_E = \frac{Q_{\text{enc}}}{\epsilon_0} = \frac{5.0 \times 10^{-9}}{8.85 \times 10^{-12}} = 565 \text{ N m}^2 \text{ C}^{-1}.$$

3.1 B.

3.2 B.

$$\mathbf{3.3} \quad (\text{a}) \quad \Phi_E = \frac{Q}{\epsilon_0} = \frac{8.0 \times 10^{-9}}{8.85 \times 10^{-12}} = 904 \text{ N m}^2 \text{ C}^{-1}. \quad (\text{b}) \quad E = \frac{kq}{r^2} = \frac{8.99 \times 10^9 \times 8.0 \times 10^{-9}}{(0.20)^2} = 1.8 \times 10^3 \text{ N C}^{-1}.$$