Question 3: Quantitative/Qualitative Translation — 12 points

(a)(i)	For correctly determining the total resistance R_{total} of the circuit	**1 point**

Example Response

$$R_{\text{total}} = \frac{5R}{3}$$

For a multi-step derivation that includes correct substitutions of $\mathcal{E}$ and R_{total} into the equation that describes Ohm's law, consistent with the first point of part (a)(i) — **1 point**

Example Response

$$I_1 = \frac{3\mathcal{E}}{5R}$$

Example Solution

Determine the total resistance of the circuit.

The resistance of the right-most branch containing resistors connected in series:

$$R_s = \sum_i R_i$$
$$R_s = R + R$$
$$R_s = 2R$$

The resistance of parallel branches that contain resistors:

$$\frac{1}{R_p} = \sum_i \frac{1}{R_i}$$
$$\frac{1}{R_p} = \frac{1}{R} + \frac{1}{2R} = \frac{3}{2R}$$
$$R_p = \frac{2R}{3}$$

The total resistance of the circuit:

$$R_s = \sum_i R_i$$
$$R_{\text{total}} = R + \frac{2R}{3} = \frac{5R}{3}$$

The total current in the circuit:

$$I = \frac{\Delta V}{R} = \frac{3\mathcal{E}}{5R}$$

(a)(ii) For applying a result of Kirchhoff's law and/or Ohm's law that relates the current in R_3 to **one** of the following: **1 point**

- The current in or potential difference across R_1
- The current in or potential difference across R_2
- The potential difference across R_3

Example Responses

One-third of the total current in the circuit is in R_3 *:* $I_3 = \frac{I_1}{3}$

OR

$I_1 = I_2 + I_3$

OR

$\Delta V_2 = \Delta V_3 + \Delta V_4$

For a correct expression from a multi-step derivation that is consistent with the final expression in part (a)(i) **1 point**

Example Response

$I = \frac{\mathcal{E}}{5R}$

Example Solutions

$I_1 = I_2 + I_3$

$$\Delta V_2 = \Delta V_3 + \Delta V_4$$
$$I_2 R_2 = I_3(R_3 + R_4)$$
$$I_2 R = I_3(2R)$$
$$I_2 = 2I_3$$

$$I_1 = 2I_3 + I_3$$
$$I_3 = \frac{I_1}{3}$$

$$I_3 = \frac{\left(\frac{3\mathcal{E}}{5R}\right)}{3}$$
$$I_3 = \frac{\mathcal{E}}{5R}$$

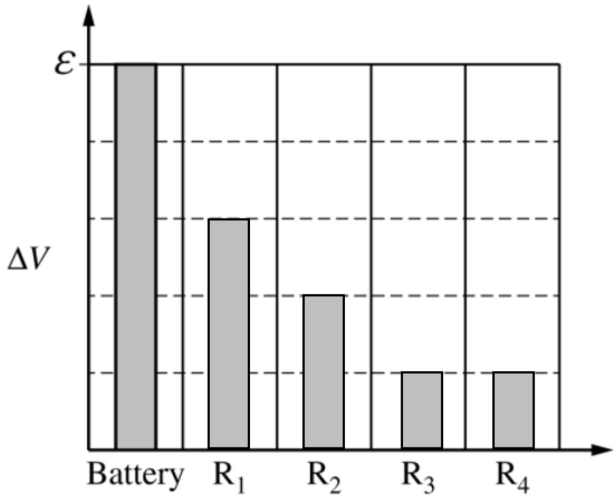
OR

One-third of the total current in the circuit is in R_3. *Therefore,* $I_3 = \frac{\mathcal{E}}{5R}$.

Total for part (a) 4 points

(b)	For drawing a bar that indicates that the potential difference across R_3 is nonzero and is equal to the potential difference across R_4	**1 point**
	For drawing a bar that indicates that the potential difference across R_2 is nonzero and is equal to the sum of the potential differences across R_3 and R_4	**1 point**
	For drawing all bars correctly	**1 point**

Example Response



Total for part (b) **3 points**

(c)	For indicating that the equation is correct or incorrect, consistent with the derivations in part (a) or the bar chart from part (b), with an attempt at a relevant justification	**1 point**
	For a justification that correctly relates P to at least **one** of the following: • The potential difference across the battery • The current in the battery • R_1, R_2, R_3, and R_4	**1 point**
	For a justification that relates the equation $P = \frac{3\mathcal{E}^2}{5R}$ to at least **one** of the following: • The bar chart from the response in part (b) • The derivations in the responses to parts (a)(i) and (a)(ii) **Scoring Note**: The justification must be consistent with the derivations in part (a) or the bar chart from part (b).	**1 point**

Example Solution

The equation is correct. The equation for P*, which is power, can be written as* $P = \frac{(\Delta V)^2}{R}$*. According to the bar chart in part (b), the potential difference across the battery is* $\mathcal{E}$*. The total resistance of the circuit is* $\frac{5R}{3}$*, according to the derivation from part (a)(i). Therefore,* $P = \frac{(\Delta V)^2}{R} = \frac{(\mathcal{E})^2}{\left(\frac{5R}{3}\right)} = \frac{3\mathcal{E}^2}{5R}$.

Total for part (c) 3 points

(d)	For selecting that $P_{\text{new}} < P_{\text{original}}$ with an attempt at a relevant justification	**1 point**
	For a correct justification that indicates at least **one** of the following: • The current in R_1 is less in the new circuit than in the original circuit • The potential difference across R_1 is less in the new circuit than in the original circuit	**1 point**

Example Response

$P_{\text{new}} < P_{\text{original}}$. *Since the* emf *of the battery is the same in the new circuit and the total resistance of the new circuit is greater, the current in* R_1 *is less in the new circuit. Therefore,* P_{new} *is less than* P_{original}.

Total for part (d) 2 points

Total for question 3 12 points

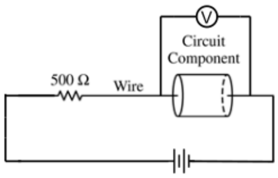
Question 2: Experimental Design — 12 points

(a)(i) For a diagram including a source of potential difference (e.g., battery, power supply) that is in a complete circuit that results in a current in the unknown circuit component — **1 point**

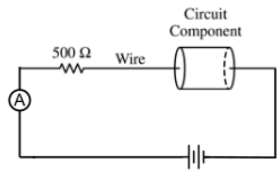
For a diagram including a measurement device that is appropriately connected in the circuit (e.g., voltmeter, ammeter) — **1 point**

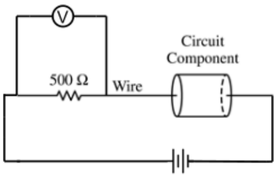
Scoring Note: A lightbulb that is connected in series with the circuit component is an acceptable alternative for an ammeter.

Example Responses

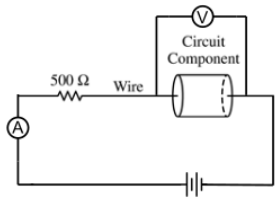


OR

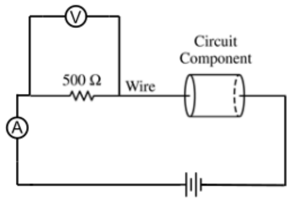




OR



OR



(a)(ii) For describing a procedure that includes a measurement of **one** of the following: — **1 point**

- The potential difference across the circuit component
- The current in the circuit
- The potential difference across the known resistor

For taking measurements at two different times after the circuit is closed or taking one measurement a long time after the circuit is closed, consistent with the procedure described — **1 point**

Example Responses

Measure the current in the ammeter immediately after the circuit is closed and a long time after the circuit is closed.

OR

Measure the potential difference across the circuit component immediately after the circuit is closed and a long time after the circuit is closed.

OR

Measure the potential difference across the circuit component a long time after the circuit is closed.

OR

Measure the potential difference across the $500\,\Omega$ *resistor immediately after the circuit is closed and a long time after the circuit is closed.*

(a)(iii) For describing a correct result of the experiment that indicates the current in the circuit decreases to zero over time or that the charge of the plates of the capacitor increases over time **1 point**

For describing a correct result of the experiment that indicates that the electric potential difference across the capacitor increases from zero over time **1 point**

Example Response

Immediately after the circuit has been closed, a current should be measured. A long time after the circuit has been closed, a current of zero should be measured. This is because the initially uncharged capacitor becomes fully charged. This results in a potential difference across the capacitor that is equal to the potential difference across the battery a long time after the circuit has been closed. Therefore, according to Kirchhoff's loop rule, a potential difference will not be measured across any other circuit components.

Total for part (a) 6 points

(b)(i) For an equation that correctly applies the loop rule **1 point**

Example Response

$0 = +\varepsilon - Ir - IR_{\text{var}}$

(b)(ii) For indicating appropriate quantities that, when graphed, result in a linear graph that allow students to determine emf ε **1 point**

Example Responses

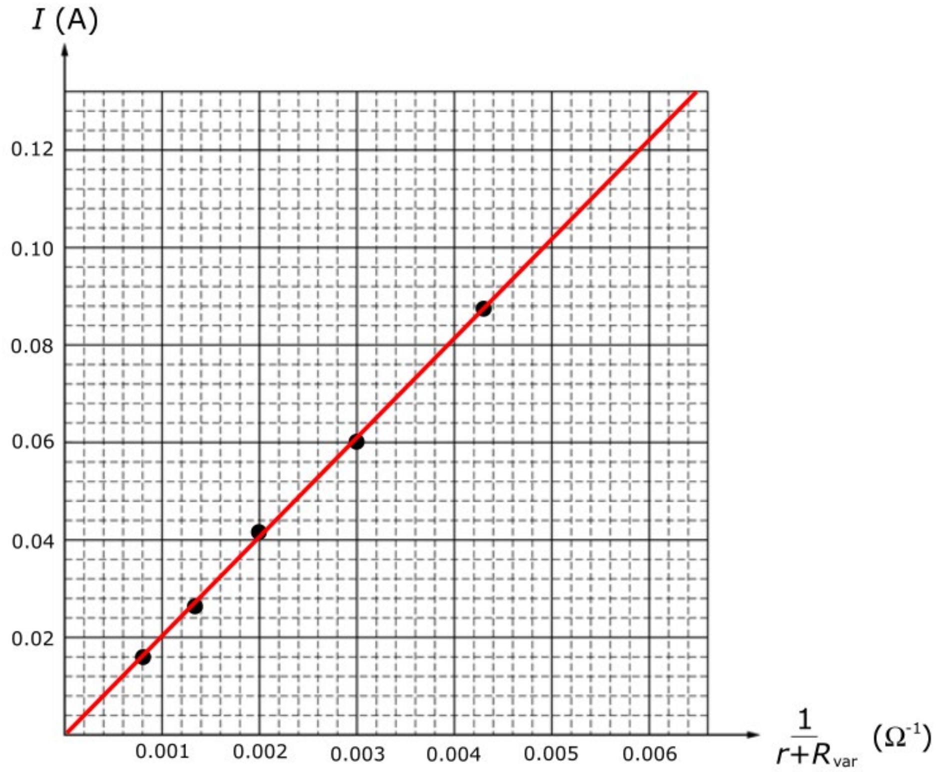
- $\dfrac{1}{r + R_{\text{var}}}$ *vs.* I
- I *vs.* IR_{var}
- R_{var} *vs.* $\dfrac{1}{I}$

(b)(iii) For including numerical values on both axes with a linear scale and labeling the axes with appropriate labels and units **1 point**

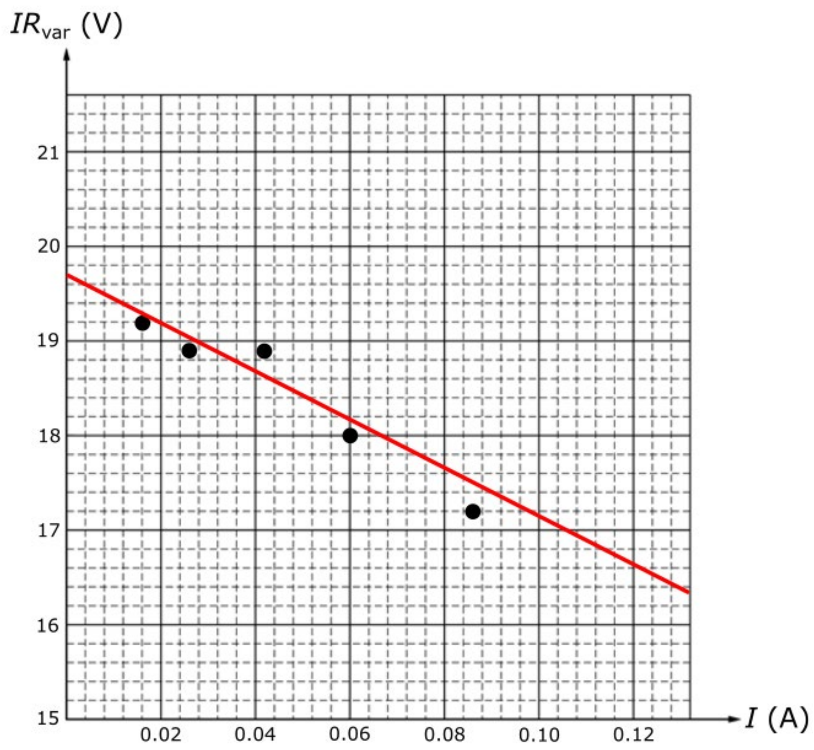
For a graph in which data are plotted within at least half of the grid area **1 point**

For drawing a best-fit line that approximates the trend of the data **1 point**

Example Responses



OR



(b)(iv) For correctly using the graph to determine an experimental value for emf ε, including correct units, between 18.0 V and 22.0 V **1 point**

Example Solutions

I as a function of $\dfrac{1}{r + R_{\text{var}}}$

$\varepsilon - Ir - IR_{\text{var}} = 0$
$\varepsilon - I(r + R_{\text{var}}) = 0$
$I(r + R_{\text{var}}) = \varepsilon$
$I = \varepsilon\left(\dfrac{1}{r + R_{\text{var}}}\right)$
$I = \varepsilon\left(\dfrac{1}{30\,\Omega + R_{\text{var}}}\right)$
$\text{Slope} = \varepsilon$
$\dfrac{\Delta y}{\Delta x} = \varepsilon$
$\dfrac{(0.08\text{ A} - 0.04\text{ A})}{\left(0.004\,\Omega^{-1} - 0.002\,\Omega^{-1}\right)} \approx \varepsilon$
$\varepsilon \approx 20\text{ V}$

OR

IR_{var} as a function of I

$\varepsilon - Ir - IR_{\text{var}} = 0$
$\varepsilon - Ir = IR_{\text{var}}$
$IR_{\text{var}} = -Ir + \varepsilon$
$y\text{-intercept} = \varepsilon$
$\varepsilon \approx 20\text{ V}$

Total for part (b) 6 points

Total for question 2 12 points

Question 2: Experimental Design — 12 points

(a) For a correct ranking — **1 point**

__1__ ΔV_A __1__ ΔV_B __3__ ΔV_C __2__ ΔV_D

For indicating that the resistors in parallel will have the same potential difference — **1 point**

For a justification that indicates $\Delta V_D > \Delta V_C$ because $R_D = 2R_C$ — **1 point**

Total for part (a) — 3 points

(b)(i) For calculating the correct value of the charge on the $200\,\mu\text{F}$ capacitor, including units — **1 point**

Example Response

$$\Delta V = \frac{Q}{C}$$

$$Q = C\Delta V = (200\,\mu\text{F})(0.91\text{ V})$$

$$Q = 1.82 \times 10^{-4}\text{ C}$$

(b)(ii) For indicating one of the following as evidence that the capacitors are in series: — **1 point**

- the potential differences across the capacitors are different
- the sum of the potential differences across the capacitors is constant
- the sum of the potential differences across the capacitors is approximately equal to the potential difference across the battery

(b)(iii) For an explanation that correctly addresses one of the following: — **1 point**

- that the potential differences across the known and unknown capacitor will always be the same
- that the charge on the unknown capacitor cannot be determined

Example Response

Both charge and potential difference across the capacitor are needed to determine C. Arranging the capacitors in parallel will mean both capacitors will have the same potential difference. However, capacitors in parallel will have differing amounts of charge, making it impossible to determine the charge, and, therefore, the capacitance of the unknown capacitor.

Total for part (b) — 3 points

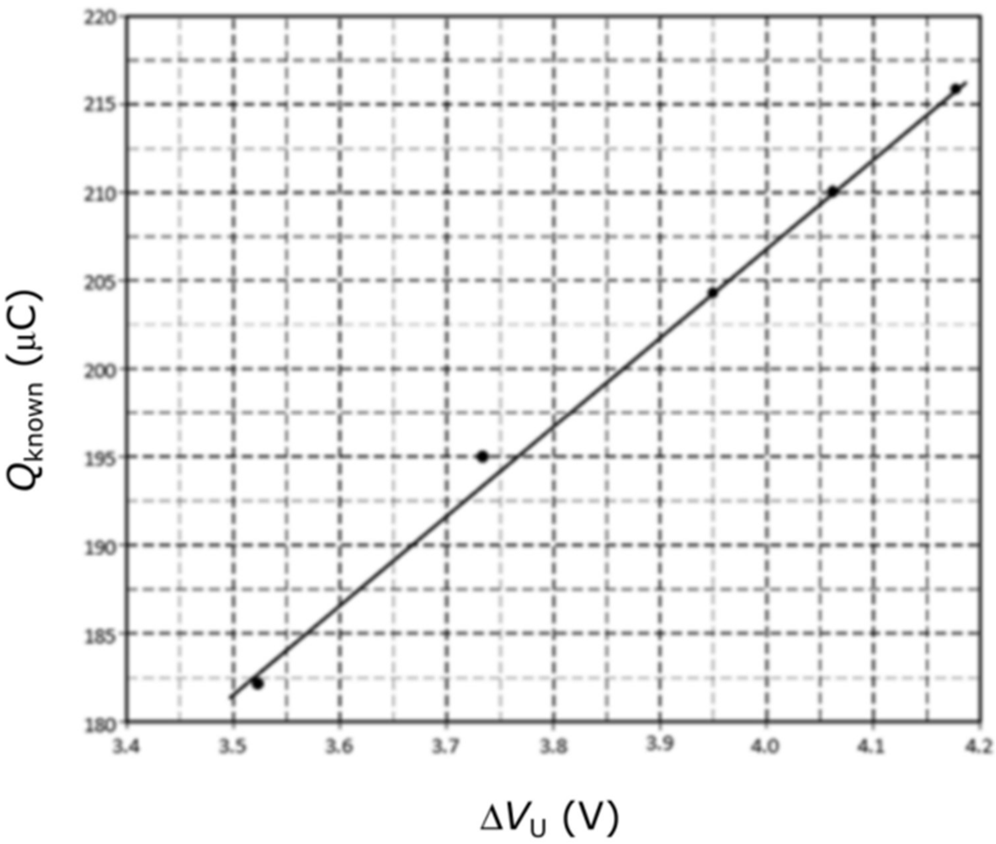
(c)(i)	For choosing two quantities that will produce a linear plot that can be used to find C_U	**1 point**

Example Responses

- Q_{known} $(C_{known}\Delta V_{known})$ and ΔV_U
- Q_U and ΔV_U
- C_{known} and $\dfrac{\Delta V_U}{\Delta V_{known}}$

(c)(ii)	For labeling the axes and including appropriate units consistent with Part (c)(i)	**1 point**
	For correctly plotting points (with valid scaling consistent with units) so that the plotted points cover at least half of the grid's width and height	**1 point**
	For drawing an appropriate linear best-fit line	**1 point**

Example Response



(c)(iii)	For using points on the best-fit line to calculate the slope of the line	**1 point**
	For correctly determining the capacitance from the slope of the line	**1 point**

Example Response

Capacitance is equal to slope

$$C_U = \frac{212\ \mu C - 190\ \mu C}{4.10\ V - 3.67\ V}$$
$$C_U = 51.2\ \mu F$$

Total for part (c) 6 points

Total for question 2 12 points

2019

AP® CollegeBoard

AP® Physics 2: Algebra-Based

Scoring Guidelines

2019 SCORING GUIDELINES

General Notes About 2019 AP Physics Scoring Guidelines

1. The solutions contain the most common method of solving the free-response questions and the allocation of points for this solution. Some also contain a common alternate solution. Other methods of solution also receive appropriate credit for correct work.

2. The requirements that have been established for the paragraph-length response in Physics 1 and Physics 2 can be found on AP Central at https://secure-media.collegeboard.org/digitalServices/pdf/ap/paragraph-length-response.pdf.

3. Generally, double penalty for errors is avoided. For example, if an incorrect answer to part (a) is correctly substituted into an otherwise correct solution to part (b), full credit will usually be awarded. One exception to this may be cases when the numerical answer to a later part should be easily recognized as wrong, e.g., a speed faster than the speed of light in vacuum.

4. Implicit statements of concepts normally receive credit. For example, if use of the equation expressing a particular concept is worth 1 point, and a student's solution embeds the application of that equation to the problem in other work, the point is still awarded. However, when students are asked to derive an expression, it is normally expected that they will begin by writing one or more fundamental equations, such as those given on the exam equation sheet. For a description of the use of such terms as "derive" and "calculate" on the exams, and what is expected for each, see "The Free-Response Sections — Student Presentation" in the *AP Physics; Physics C: Mechanics, Physics C: Electricity and Magnetism Course Description* or "Terms Defined" in the *AP Physics 1: Algebra-Based Course and Exam Description* and the *AP Physics 2: Algebra-Based Course and Exam Description*.

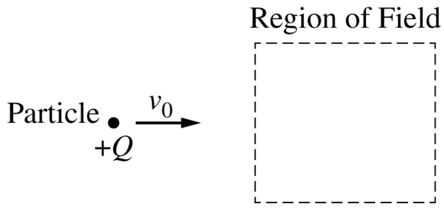
5. The scoring guidelines typically show numerical results using the value $g = 9.8 \text{ m/s}^2$, but the use of 10 m/s^2 is of course also acceptable. Solutions usually show numerical answers using both values when they are significantly different.

6. Strict rules regarding significant digits are usually not applied to numerical answers. However, in some cases answers containing too many digits may be penalized. In general, two to four significant digits are acceptable. Numerical answers that differ from the published answer due to differences in rounding throughout the question typically receive full credit. Exceptions to these guidelines usually occur when rounding makes a difference in obtaining a reasonable answer. For example, suppose a solution requires subtracting two numbers that should have five significant figures and that differ starting with the fourth digit (e.g., 20.295 and 20.278). Rounding to three digits will lose the accuracy required to determine the difference in the numbers, and some credit may be lost.

2019 SCORING GUIDELINES

Question 1

10 points

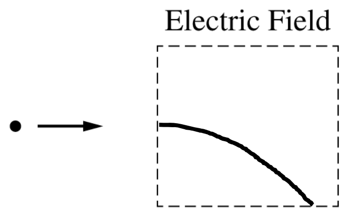


The figure above shows a particle with positive charge $+Q$ traveling with a constant speed v_0 to the right and in the plane of the page. The particle is approaching a region, shown by the dashed box, that contains a constant uniform field. The effects of gravity are negligible.

(a)

i. LO 2.C.1.1, SP 6.4
2 points

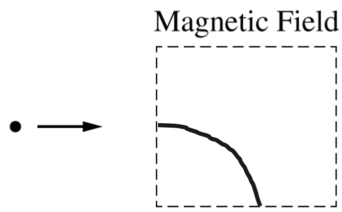
On the figure below, draw a possible path of the particle in the region if the region contains only an electric field directed toward the bottom of the page.



For a curved path that is initially horizontal and does not have a component of velocity toward the left		1 point
For a path that deflects toward the bottom of the page and reaches an edge of the region		1 point

ii. LO 3.C.3.1, SP 1.4
2 points

On the figure below, draw a possible path of the particle in the region if the region contains only a magnetic field directed out of the page.



For a curved path that is initially horizontal, is not more than a semicircle, and reaches an edge of the region		1 point
For a path that deflects toward the bottom of the page		1 point

2019 SCORING GUIDELINES

Question 1 (continued)

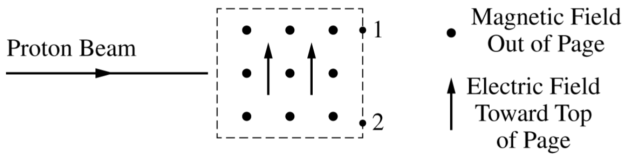
(a) (continued)

iii. LO 2.C.5.3, SP 1.1, 7.1
1 point

For which of the previous situations is the motion more similar to that of a projectile in only a gravitational field near Earth's surface, and why?

For indicating that the motion in the electric field is more similar to a projectile because the force or acceleration is always down or constant, or the shape is parabolic		1 point

(b) LO 2.D.1.1, SP 2.2; LO 3.A.3.4, SP 6.1, 6.4; LO 3.B.1.4, SP 6.4, 7.2; LO 3.B.2.1, SP 1.1, 1.4, 2.2
5 points



Another region of space contains an electric field directed toward the top of the page and a magnetic field directed out of the page. Both fields are constant and uniform. A horizontal beam of protons with a variety of speeds enters the region, as shown above. Protons exit the region at a variety of locations, including points 1 and 2 shown on the figure. In a coherent, paragraph-length response, explain why some protons exit the region at point 1 and others exit at point 2. Use physics principles to explain your reasoning.

For indicating that initially the electric and magnetic forces act in opposite directions		1 point
For indicating or implying that the magnetic force is affected by speed, but the electric force is not		1 point
For indicating that different paths occur as a result of the addition of forces		1 point
For indicating that slower protons exit higher than faster protons (i.e., slower protons exit at point 1 and faster protons exit at point 2)		1 point
For a logical, relevant, and internally consistent argument that addresses the question asked and follows the guidelines described in the published requirements for the paragraph-length response		1 point
Example: For a charged particle to travel through the region undeflected, the net force on it must be zero. This means that the upward electric force and the downward magnetic force must be equal and opposite to each other. This occurs for a particular speed. The electric force is independent of the particle's velocity, but the magnetic force will be larger for greater velocities and less for smaller velocities. If a particle is moving faster than the particular speed, it will experience a greater magnetic force and be deflected downward. If it is moving more slowly than the particular speed, it will be deflected upward.		

2019 SCORING GUIDELINES

Question 1 (continued)

(b) (continued)

Claim: Slower protons exit higher than faster protons (i.e., slower protons exit at point 1 and faster protons exit at point 2). Evidence: The electric and magnetic forces act in opposite directions. The magnetic force is affected by speed, but the electric force is not. Reasoning: Different paths occur as a result of the addition of forces.		

Learning Objectives

LO 2.C.1.1: The student is able to predict the direction, and the magnitude of the force exerted on an object with an electric charge q placed in an electric field E using the mathematical model of the relation between an electric force and an electric field: $\vec{F} = q\vec{E}$; a vector relation. [See Science Practices 6.4, 7.2]

LO 2.C.5.3: The student is able to represent the motion of an electrically-charged particle in the uniform field between two oppositely charged plates and express the connection of this motion to projectile motion of an object with mass in Earth's gravitational field. [See Science Practices 1.1, 2.2, 7.1]

LO 2.D.1.1: The student is able to apply mathematical routines to express the force exerted on a moving charged object by a magnetic field. [See Science Practices 2.2]

LO 3.A.3.4: The student is able to make claims about the force on an object due to the presence of other objects with the same property: mass, electric charge. [See Science Practices 6.1, 6.4]

LO 3.B.1.4: The student is able to predict the motion of an object subject to forces exerted by several objects using an application of Newton's second law in a variety of physical situations. [See Science Practices 6.4, 7.2]

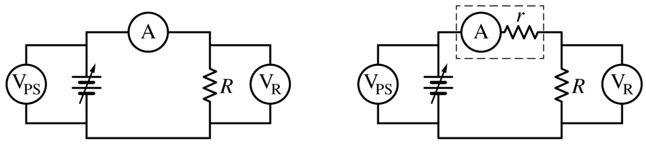
LO 3.B.2.1: The student is able to create and use free-body diagrams to analyze physical situations to solve problems with motion qualitatively and quantitatively. [See Science Practices 1.1, 1.4, 2.2]

LO 3.C.3.1: The student is able to use right-hand rules to analyze a situation involving a current-carrying conductor and a moving electrically charged object to determine the direction of the magnetic force exerted on the charged object due to the magnetic field created by the current-carrying conductor. [See Science Practices 1.4]

2019 SCORING GUIDELINES

Question 2

12 points



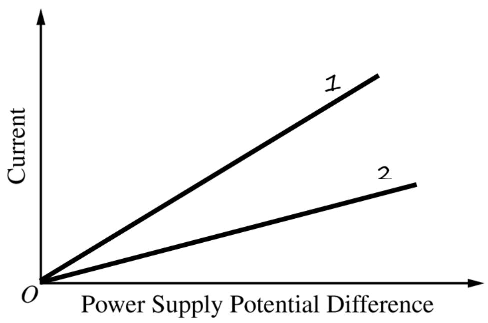
Circuit 1 Circuit 2

The two circuits shown above contain an ideal variable power supply, an ohmic resistor of resistance R, an ammeter A, and two voltmeters V_{PS} and V_R . In circuit 1 the ammeter has negligible resistance, and in circuit 2 the ammeter has significant internal ohmic resistance r. The potential difference of the power supply is varied, and measurements of current and potential difference are recorded.

(a) LO 4.E.5.1, SP 6.4
2 points

The axes below can be used to graph the current measured by the ammeter as a function of the potential difference measured across the power supply. On the axes, do the following.

- Sketch a possible graph for circuit 1 and label it 1.
- Sketch a possible graph for circuit 2 and label it 2.



For graph 1 a straight line with a positive slope through origin		1 point
For graph 2 a straight line with a positive slope through origin with a smaller slope than line 1		1 point

(b) LO 5.B.9.6, SP 2.2; LO 5.C.3.4, SP 6.4
2 points

Let ΔV_{PS} be the potential difference measured by voltmeter V_{PS} across the power supply, and let I be the current measured by the ammeter A. For each circuit, write an equation that satisfies conservation of energy, in terms of ΔV_{PS} , I, R, and r, as appropriate.

<u>Circuit 1</u> <u>Circuit 2</u>

For a correct equation for circuit 1		1 point
$\Delta V_{PS} - IR = 0$		
For a correct equation for circuit 2		1 point
$\Delta V_{PS} - I(R + r) = 0$		

2019 SCORING GUIDELINES

Question 2 (continued)

(c) LO 5.B.9.8, SP 1.5
2 points

Explain how your equations in part (b) account for any differences between graphs 1 and 2 in part (a).

For indicating that the slope is inversely proportional to the resistance		1 point
For explaining that the equations in part (b) show that a larger total resistance corresponds to a smaller slope or smaller current		1 point
Example: Claim: The equations in part (b) account for the differences between graphs 1 and 2 in part (a). Evidence: The graphs show a linear relationship between current and potential difference. The equations are linear functions, which when graphed would have a slope that is the inverse of the total resistance. Reasoning: The difference between the equations is the value of the total resistance, so the equations account for the difference in slopes. The larger the total resistance, the smaller the slope.		

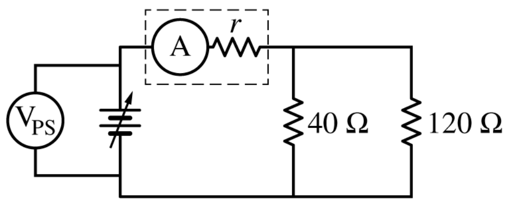
(d) LO 5.B.9.6, SP 2.2; LO 5.C.3.4, SP 6.4, 7.2
2 points

In circuit 2, $R = 40\ \Omega$. When voltmeter V_{PS} reads 3.0 V, voltmeter V_R reads 2.5 V. Calculate the internal resistance r of the ammeter.

Ohm's law solution:		
For correctly calculating the current in the circuit		1 point
$I = \Delta V_R / R = 2.5\ \text{V}/40\ \Omega = 0.0625\ \text{A}$		
For using Ohm's law with the calculated current and correct potential difference		1 point
$r = \Delta V_r / I = (3\ \text{V} - 2.5\ \text{V})/0.0625\ \text{A}$		
$r = 8\ \Omega$		

(e)

Voltmeter V_R in circuit 2 is replaced by a resistor with resistance $120\ \Omega$ to create circuit 3 shown below. Voltmeter V_{PS} still reads 3.0 V.



Circuit 3

Question 2 (continued)

(e) (continued)

i. LO 4.E.5.1, SP 2.2
2 points

Calculate the equivalent resistance R_{eq} of the circuit.

For calculating the equivalent resistance of the parallel branches		1 point
$\frac{1}{40\ \Omega} + \frac{1}{120\ \Omega} = \frac{4}{120\ \Omega}$		
$R_{\parallel} = 30\ \Omega$		
For adding the value of r from part (d) to $R_{\parallel}$		1 point
$R_{eq} = 30\ \Omega + 8\ \Omega = 38\ \Omega$		

ii. LO 5.B.9.6, SP 2.2
2 points

Calculate the current in each of the resistors that are in parallel.

For substituting the correct potential difference and the resistance from part (e)(i) into Ohm's law to determine the current through the battery		1 point
$I_{tot} = 3\ \text{V}/38\ \Omega = 0.079\ \text{A}$		
For calculating two currents that are in the correct ratio ($I_{40\ \Omega} = 3I_{120\ \Omega}$)		1 point
$\Delta V_{\text{parallel}} = (3\ \text{V}) - (8\ \Omega)(0.079\ \text{A}) = 2.36\ \text{V}$ $I_{40\ \Omega} = \frac{2.36\ \text{V}}{40\ \Omega} = 0.059\ \text{A}$ $I_{120\ \Omega} = \frac{2.36\ \text{V}}{120\ \Omega} = 0.020\ \text{A}$		

Learning Objectives

LO 4.E.5.1: The student is able to make and justify a quantitative prediction of the effect of a change in values or arrangements of one or two circuit elements on the currents and potential differences in a circuit containing a small number of sources of emf, resistors, capacitors, and switches in series and/or parallel. [See Science Practices 2.2, 6.4]

LO 5.B.9.6: The student is able to mathematically express the changes in electric potential energy of a loop in a multiloop electrical circuit and justify this expression using the principle of the conservation of energy. [See Science Practices 2.1, 2.2]

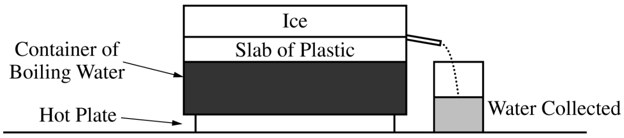
LO 5.B.9.8: The student is able to translate between graphical and symbolic representations of experimental data describing relationships among power, current, and potential difference across a resistor. [See Science Practices 1.5]

LO 5.C.3.4: The student is able to predict or describe current values in series and parallel arrangements of resistors and other branching circuits using Kirchhoff's junction rule and explain the relationship of the rule to the law of charge conservation. [See Science Practices 6.4, 7.2]

2019 SCORING GUIDELINES

Question 3

12 points



A group of students use the apparatus shown above to determine the thermal conductivity of a certain type of plastic. A hot plate is used to keep water in a container boiling at a temperature of $100°C$. They place a slab of the plastic with area $0.025\ m^2$ and thickness 0.010 m above the container so that the bottom surface of the slab is at a temperature of $100°C$. They put a large block of ice with temperature $0°C$ on top of the plastic slab. Some of the ice melts, and the students measure the amount of water collected during a time Δt. The students correctly calculate the amount of energy Q delivered to the ice and thus determine $Q/\Delta t$. They repeat this experiment several times, each time adding an identical slab to increase the total thickness L of plastic. Their results are shown in the table below.

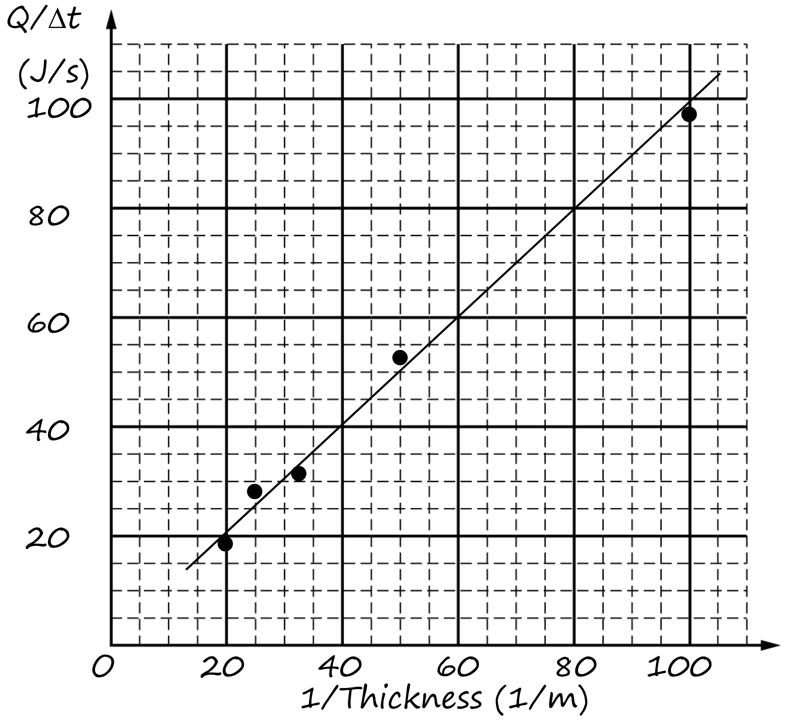
Table with sample entries for part (a)(ii)

Energy Flow Rate $Q/\Delta t$ (J/s)	97	53	31	27	18
Total Thickness of Plastic (m)	0.01	0.02	0.03	0.04	0.05
1/Thickness (1/m)	100	50	33.3	25	20

(a)

The students want to create a graph to yield a straight line whose slope could be used to calculate the thermal conductivity of the plastic.

Sample graph using above data



2019 SCORING GUIDELINES

Question 3 (continued)

(a) (continued)

i. LO 1.E.3.1, SP 4.1, 5.1
1 point

Label the axes below to indicate a pair of quantities that could be graphed to yield a straight line. Include units for the quantities.

$\dfrac{Q}{\Delta t} = \dfrac{kA\,\Delta T}{L}$		
For labeling the axes with two quantities that would produce a linear graph, including units		1 point
Example: $Q/\Delta t$ and $1/\text{thickness}$		

ii. LO 1.E.3.1, SP 4.1, 5.1
3 points

On the grid on the previous page, create a linear graph using the values for the quantities indicated in part (a)(i). Be sure to do the following:

- Add to the data table the values of any quantities to be plotted that are not already given.
- Scale the axes.
- Plot the data from the table.
- Draw a line that best represents the data.

For scaling the axes linearly so the data extends over at least half of each axis		1 point
For accurately plotting the data		1 point
For a best-fit curve or line that fits the trend in the data		1 point

iii. LO 1.E.3.1, 5.1
2 points

Use the graph to calculate the thermal conductivity of the plastic.

For a correct method for calculating the slope using points on the best-fit line		1 point
For the graph above, $\text{slope} = \dfrac{(80-20)(\text{J/s})}{(80-20)(1/\text{m})} = 1.0\ \text{J}\bullet\text{m/s}$		
For determining the thermal conductivity k, with or without units using the slope found above		1 point
$\dfrac{Q}{\Delta t} = \dfrac{kA\,\Delta T}{L}$ so $\text{slope} = kA\,\Delta T$		
Using slope above: $k = \text{slope}/A\Delta T = 1(\text{J}\bullet\text{m/s})\Big/\left(0.025\ \text{m}^2\right)(100°\ \text{C}) = 0.40\ \text{J/s}\bullet\text{m}°\text{C}$		

Question 3 (continued)

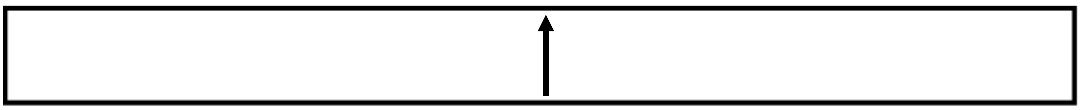
(b) LO 5.B.6.1, SP1.2
2 points

Indicate one potential problem with the setup that could lead to an experimental value for the thermal conductivity that is different from the actual value. Use physics principles to explain the effect this problem could have on the experimental value.

For any valid indication of an additional thermal interaction with the environment		1 point
For a reasonable explanation of how additional energy added or lost could change the experimental value of conductivity		1 point
Example 1: The given setup allows energy to be transferred to the ice from the air around it. This means the values of $Q/\Delta t$ contain energy that did not go through the plastic slab, resulting in a value of k that is too large.		
Example 2: The given setup allows energy to be lost out the sides of the plastic slab. This means the values of $Q/\Delta t$ do not contain all the energy that went through the plastic slab, resulting in a value of k that is too small.		
Claim: The problem leads to a value of k that is too small/large. Evidence: The problem allows energy transfer into/out of the system that is not accounted for. Reasoning: The values of $Q/\Delta t$ contain less/more energy than went through the plastic slab, resulting in a value of k that is too small/large.		

(c) LO 4.C.3.1, SP 6.4
1 point

The rectangle below represents a side view of the plastic slab. Draw a single arrow on the diagram representing the direction of the net flow of energy through the plastic.



For drawing an arrow toward the top of the page		1 point

(d) LO 4.C.3.1, SP 6.4; LO 5.B.6.1, SP 1.2; LO 5.D.1.6, SP 6.4
2 points

Describe what occurs in the plastic at the microscopic level that explains the energy flow you indicated in part (c).

For indicating that particles at the bottom (or a location consistent with part (c)) have a higher temperature or kinetic energy, so they vibrate faster		1 point
For indicating that particles collide with neighboring particles, transferring energy from faster to slower particles in the process		1 point
Example: Energy absorbed at the lower surface makes particles jiggle faster, they jiggle particles above them, and so forth until energy reaches the other side.		

Question 3 (continued)

(e) LO 1.E.3.1, SP 4.1, 4.2
1 point

An extra plastic slab sits on a wood surface, with both the plastic slab and the wood surface at room temperature. A student touches each and finds that the plastic slab feels cooler than the wood surface. Explain what causes this observation.

For indicating that the slab and wood have different thermal conductivities or that energy is transferred into the plastic and wood at different rates, with no incorrect statements		1 point

Learning Objectives

LO 1.E.3.1: The student is able to design an experiment and analyze data from it to examine thermal conductivity. [See Science Practices 4.1, 4.2, 5.1]

LO 4.C.3.1: The student is able to make predictions about the direction of energy transfer due to temperature differences based on interactions at the microscopic level. [See Science Practices 6.4]

LO 5.B.6.1: The student is able to describe the models that represent processes by which energy can be transferred between a system and its environment because of differences in temperature: conduction, convection, and radiation. [See Science Practices 1.2]

LO 5.D.1.6: The student is able to make predictions of the dynamical properties of a system undergoing a collision by application of the principle of linear momentum conservation and the principle of the conservation of energy in situations in which an elastic collision may also be assumed. [See Science Practices 6.4]

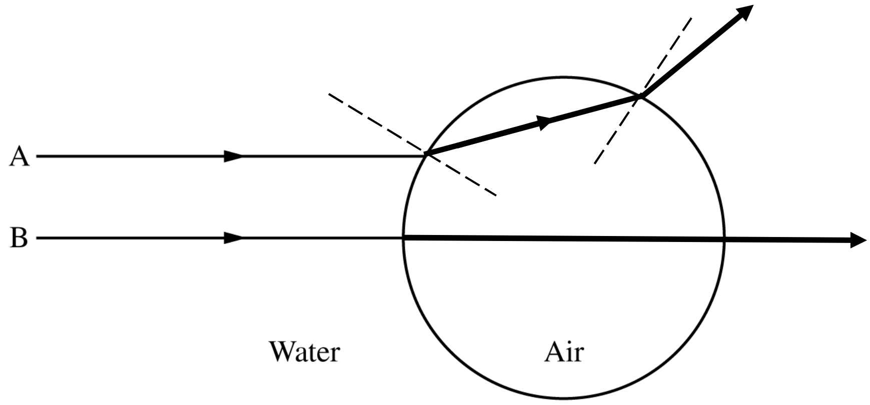
Question 4

10 points

A student notices many air bubbles rising through the water in a large fish tank at an aquarium.

(a) LO 6.E.3.1, SP 1.1, 1.4
3 points

In the figure below, the circle represents one such air bubble, and two incoming rays of light, A and B, are shown. Ray B points toward the center of the circle. On the diagram, draw the paths of rays A and B as they go through the bubble and back into the water. Your diagram should clearly show what happens to the rays at each interface.



For ray B going straight through		1 point
For ray A bending away from the normal as it enters the air from the water		1 point
For ray A bending the opposite direction in relationship to the normal as it exits the air and enters the water compared to the refraction entering the air from the water		1 point
Note: The normals need not be shown.		

(b) LO 5.B.4.1, SP 6.4, 7.2; LO 5.B.4.2, SP 1.4, 7.2; LO 5.B.5.4, SP 6.4, 2.2; LO 5.B.5.5, SP 2.2, 6.4
3 points

The bubble has a volume V_1, the air inside it has density ρ_A, and the water around it has density ρ_W. The bubble starts at rest and has a speed v_f when it has risen a height h. Assume that the change in the bubble's volume is negligible. Derive an expression for the mechanical energy dissipated by drag forces as the bubble rises this distance. Express your answer in terms of the given quantities and fundamental constants, as appropriate.

For a valid application of the work-energy theorem		1 point
$\Delta K = W_{\text{net}} = \lvert W_b \rvert - \lvert W_g \rvert - \lvert W_{\text{diss}} \rvert$		
For finding the work done by the buoyant force		1 point
$W_b = \rho_w V_1 g h$		
For correct substitutions into an equation with consistent relative signs for the terms		1 point
$\frac{1}{2}\rho_A V_1 v_f^2 = \rho_W V_1 g h - \rho_A V_1 g h - \lvert W_{\text{diss}} \rvert$		
$\lvert W_{\text{diss}} \rvert = \rho_W V_1 g h - \rho_A V_1 g h - \frac{1}{2}\rho_A V_1 v_f^2$		

Question 4 (continued)

(c)

At a particular instant, one bubble is 4.5 m below the water's surface. The surface of the water is at sea level, and the density of the water is 1000 kg/m^3.

i. LO 5.B.10.1, SP 2.2
1 point

Determine the absolute pressure in the bubble at this location.

$P_{4.5\text{m}} = P_{atm} + \rho_w g d$		
$P_{4.5\text{m}} = (1.0 \times 10^5 \text{Pa}) + (1000 \text{ kg/m}^3)(9.8 \text{ m/s}^2)(4.5 \text{ m})$		
For a correct answer with units		1 point
$P_{4.5\text{m}} = 1.44 \times 10^5 \text{ Pa}$ (or $1.45 \times 10^5 \text{ Pa}$ using $g = 10 \text{ m/s}^2$)		

ii. LO 7.A.3.3, SP 5.1
2 points

The bubble has a volume V_1 when it is 4.5 m below the water's surface. Assume that the temperature of the air in the bubble remains constant as it rises. In terms of V_1, calculate the volume of the bubble when it is just below the surface of the water.

For applying the ideal gas law at two locations in an attempt to determine the new bubble volume		1 point
$P_{4.5\text{m}} V_1 = P_{atm} V_{surface}$		
$V_{surface} = P_{4.5\text{m}} V_1 / P_{atm}$		
For substituting pressures consistent with part (i)		1 point
$V_{surface} = (1.44 \times 10^5 \text{ Pa}) V_1 / (1 \times 10^5 \text{ Pa})$		
$V_{surface} = 1.44 V_1$ (or $1.45 V_1$ using $g = 10 \text{ m/s}^2$)		

iii. LO 7.A.3.3, SP 5.1
1 point

If the air in the bubble cooled as it rose, the volume of the bubble would be less than the value calculated in part (c)(ii). Use physics principles to briefly explain why.

For a correct explanation		1 point
<u>Note:</u> The explanation may be qualitative or quantitative. The explanation may also be macroscopic or microscopic.		

Question 4 (continued)

(c) (continued)
iii. (continued)

Example 1: By the ideal gas law, $P_{4.5\text{m}}V_1/T_1 = P_{atm}V_{surface}/T_{surface}$, so $V_{surface} = P_{4.5\text{m}}V_1T_{surface}/P_{atm}T_1$. The two pressures still have their previous values. $T_{surface} < T_1$, so the volume at the surface will be smaller.		
Example 2: As the bubble cools, the air molecules move slower. Slower molecules exert less force on the inner surface of the bubble. The unbalanced force, due to the difference in the forces on the inside and outside of the bubble, causes the bubble to expand less than it did in the constant temperature situation or contract.		
Claim (given): The volume of the bubble will decrease Example 1 evidence: $P_{4.5\text{m}}V_1/T_1 = P_{atm}V_{surface}/T_{surface}$, so $V_{surface} = P_{4.5\text{m}}V_1T_{surface}/P_{atm}T_1$ Example 1 reasoning: The two pressures still have their previous values. $T_{surface} < T_1$, so the volume at the surface will be smaller. Example 2 evidence: As the bubble cools, the air molecules move slower. Slower molecules exert less force on the inner surface of the bubble. Example 2 reasoning: The unbalanced force, due to the difference in the forces on the inside and outside of the bubble, causes the bubble to contract.		

Learning Objectives:

LO 5.B.4.1: The student is able to describe and make predictions about the internal energy of systems. [See Science Practices 6.4, 7.2]

LO 5.B.4.2: The student is able to calculate changes in kinetic energy and potential energy of a system using information from representations of that system. [See Science Practices 1.4, 2.1, 2.2]

LO 5.B.5.4: The student is able to make claims about the interaction between a system and its environment in which the environment exerts a force on the system, thus doing work on the system and changing the energy of the system (kinetic energy plus potential energy). [See Science Practices 6.4, 7.2]

LO 5.B.5.5: The student is able to predict and calculate the energy transfer to (i.e., the work done on) an object or system from information about a force exerted on the object or system through a distance. [See Science Practices 2.2, 6.4]

LO 5.B.10.1: The student is able to make calculations related to a moving fluid using Bernoulli's equation. [See Science Practices 2.2]

LO 6.E.3.1: The student is able to describe models of light traveling across a boundary from one transparent material to another when the speed of propagation changes, causing a change in the path of the light ray at the boundary of the two media. [See Science Practices 1.1, 1.4]

LO 7.A.3.3: The student is able to analyze graphical representations of macroscopic variables for an ideal gas to determine the relationships between these variables and to ultimately determine the ideal gas law $PV = nRT$. [See Science Practices 5.1]

2017

AP Physics 2: Algebra-Based

Scoring Guidelines

AP® PHYSICS
2017 SCORING GUIDELINES

General Notes About 2017 AP Physics Scoring Guidelines

1. The solutions contain the most common method of solving the free-response questions and the allocation of points for this solution. Some also contain a common alternate solution. Other methods of solution also receive appropriate credit for correct work.

2. The requirements that have been established for the paragraph length response in Physics 1 and Physics 2 can be found on AP Central at https://secure-media.collegeboard.org/digitalServices/pdf/ap/paragraph-length-response.pdf.

3. Generally, double penalty for errors is avoided. For example, if an incorrect answer to part (a) is correctly substituted into an otherwise correct solution to part (b), full credit will usually be awarded. One exception to this may be cases when the numerical answer to a later part should be easily recognized as wrong, e.g., a speed faster than the speed of light in vacuum.

4. Implicit statements of concepts normally receive credit. For example, if use of the equation expressing a particular concept is worth one point, and a student's solution embeds the application of that equation to the problem in other work, the point is still awarded. However, when students are asked to derive an expression it is normally expected that they will begin by writing one or more fundamental equations, such as those given on the exam equation sheet. For a description of the use of such terms as "derive" and "calculate" on the exams, and what is expected for each, see "The Free-Response Sections—Student Presentation" in the *AP Physics; Physics C: Mechanics, Physics C: Electricity and Magnetism Course Description* or "Terms Defined" in the *AP Physics 1: Algebra-Based and AP Physics 2: Algebra-Based Course and Exam Description*.

5. The scoring guidelines typically show numerical results using the value $g = 9.8 \text{ m/s}^2$, but use of 10 m/s^2 is of course also acceptable. Solutions usually show numerical answers using both values when they are significantly different.

6. Strict rules regarding significant digits are usually not applied to numerical answers. However, in some cases answers containing too many digits may be penalized. In general, two to four significant digits are acceptable. Numerical answers that differ from the published answer due to differences in rounding throughout the question typically receive full credit. Exceptions to these guidelines usually occur when rounding makes a difference in obtaining a reasonable answer. For example, suppose a solution requires subtracting two numbers that should have five significant figures and that differ starting with the fourth digit (e.g., 20.295 and 20.278). Rounding to three digits will lose the accuracy required to determine the difference in the numbers, and some credit may be lost.

2017 SCORING GUIDELINES

Question 1

10 points total | **Distribution of points**

(a)

i. 1 point

For indicating that student Y is correct in stating that the water moves faster at point *B*, and not indicating any other aspect — 1 point

ii. 2 points

Student Y's statement that P_B is greater than P_A is not correct.

For a correct indication of how height affects pressure using the Bernoulli equation (i.e., conservation of energy principles) — 1 point

For correct indication of how the speed affects pressure using the Bernoulli equation (i.e., conservation of energy principles) — 1 point

Example: The pressure at point *B* is not greater. Because the water at *B* is moving faster and is higher than at point *A*, the kinetic energy and the gravitational potential energy terms in Bernoulli's equation are both greater. Because the sum of pressure and these energy terms is a constant, the pressure must be less.

iii. 1 point

For indicating one of the following: — 1 point

- Student Z is correct in stating that the potential energy of the water-Earth system has increased.
- Student Z is correct in stating that conservation of energy applies.
- Stating that nothing is correct or giving no response, with a justification in (iv).

iv. 1 point

For indicating that student Z is incorrect in stating that the speed is less at point *B*, not indicating any other aspect, and using continuity or the Bernoulli equation (i.e., conservation of energy principles) to show that it is greater — 1 point

OR

if third bullet for (iii) applies, indicating that work is done on the water due to the pressure difference, so the energy is not constant

2017 SCORING GUIDELINES

Question 1 (continued)

Distribution of points

(b)

i. 2 points

For a correct application of the continuity equation including substitutions — 1 point

$A_A v_A = A_B v_B$

$v_B = A_A v_A / A_B = r_A^2 v_A / r_B^2 = (2.5\text{ cm})^2 (0.5\text{ m/s}) / (1.5\text{ cm})^2$

For a correct answer with units — 1 point

$v_B = 1.4\text{ m/s}$

ii. 1 point

For an application of Bernoulli's equation to this situation and substitutions consistent with (b)(i) — 1 point

$$P_A + \rho g y_A + \frac{1}{2}\rho v_A^2 = P_B + \rho g y_B + \frac{1}{2}\rho v_B^2$$

$$P_B = P_A + \rho g(y_A - y_B) + \frac{1}{2}\rho\left(v_A^2 - v_B^2\right)$$

$$P_B = 2\times 10^5 + (1000)(10)(-5) + \frac{1}{2}(1000)\left(0.5^2 - 1.4^2\right) = 2\times 10^5 - 50000 - 855$$

$$P_B = 1.5\times 10^5\text{ Pa}$$

(c)

i. 1 point

For substituting correctly in an appropriate equation for determining the pressure — 1 point

$P = P_0 + \rho g h_A = 1\times 10^5\text{ Pa} + \left(1000\text{ kg/m}^3\right)\left(10\text{ m/s}^2\right)(6\text{ m})$

$P = 1.6\times 10^5\text{ Pa}$

ii. 1 point

For indicating that the buoyant force is toward the top of the page and gravity is toward the bottom of the page, with the buoyant force longer — 1 point

Student can draw lots of pressure forces around the dot instead of one buoyant force, as long as there is no buoyant force labeled and they add up to a net buoyant force that is longer than the gravitational force.

2017 SCORING GUIDELINES

Question 2

12 points total | **Distribution of points**

(a)

i. 5 points

For drawing a circuit with the battery, rod, and ammeter in series (rods can be drawn to look like rods, or schematically as resistors)	1 point
For drawing the voltmeter parallel to the rod, or indicating that the setting on the power supply will be used	1 point
For measuring potential difference and current for a rod	1 point
For measuring the length and diameter of a rod	1 point
For including multiple trials with appropriate controls Examples: 1) Use one rod and apply different potential differences 2) Use different rods	1 point

ii. 2 points

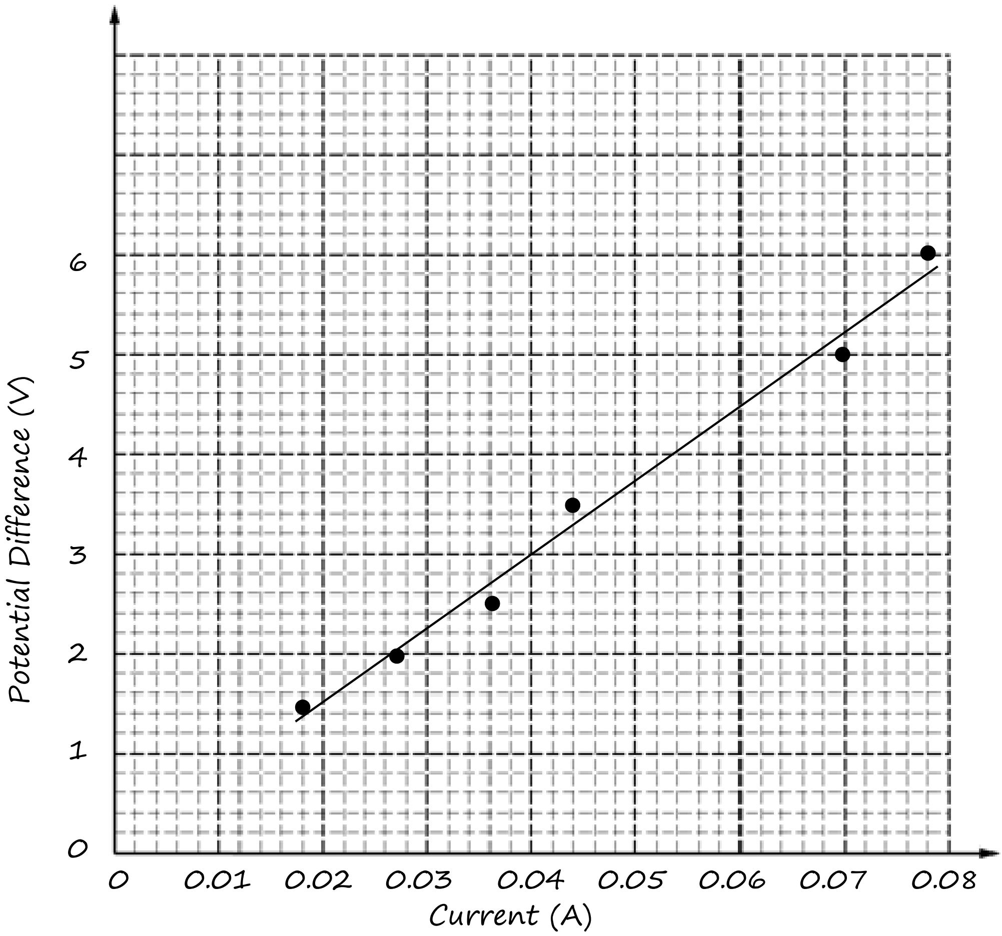
For graphing appropriate quantities whose slope can be used to calculate resistance directly or indirectly	1 point
For correctly stating how the slope relates to the resistivity	1 point

2017 SCORING GUIDELINES

Question 2 (continued)

Distribution of points

(b) 3 points



For plotting the data on the graph with potential difference on one axis and current on the other, labeled with units, using a reasonable scale — 1 point

For a clearly shown calculation of slope from a reasonable best-fit line — 1 point

For a correct answer with units — 1 point

Acceptable range is $70 - 79\ \Omega$.

For a graph of *I* as a function of *V*, the slope should end up near $0.013\ \Omega^{-1}$ and the resistance is the inverse

For a graph of *V* as a function of *I*, the slope should end up near $74\ \Omega$ and equals the resistance

For the example shown above

$$\text{slope} = \frac{(5.8 - 2.4)\ \text{V}}{(0.078 - 0.032)\ \text{A}} = 73.9\ \Omega$$

2017 SCORING GUIDELINES

Question 2 (continued)

Distribution of points

(c)

i. 1 point

For indicating that the internal resistance of the power supply will not affect the data acquired, with correct reasoning — 1 point

Example: Because potential difference is measured across each rod, $\Delta V/I$ is not affected by the internal resistance of the battery.

ii. 1 point

For indicating either: — 1 point

The students should be concerned because a change in temperature causes a change in the resistance or resistivity.

OR

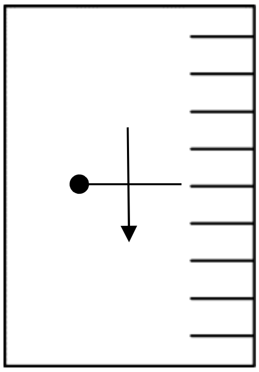
The students should not be concerned because any change in resistivity as the temperature increases is small compared to measurement error.

2017 SCORING GUIDELINES

Question 3

12 points total | **Distribution of points**

(a) 2 points



For the arrow drawn upside down relative to the object — 1 point

For bar/circle drawn left-to-right reversed relative to the object or consistent with an (incorrect) upright arrow — 1 point

(b)

i. 1 point

For correctly showing a calculation of the focal length and a correct answer with units — 1 point

$$\frac{1}{f} = \frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{20\text{ cm}} + \frac{1}{30\text{ cm}}$$

$f = 12$ cm

ii. 1 point

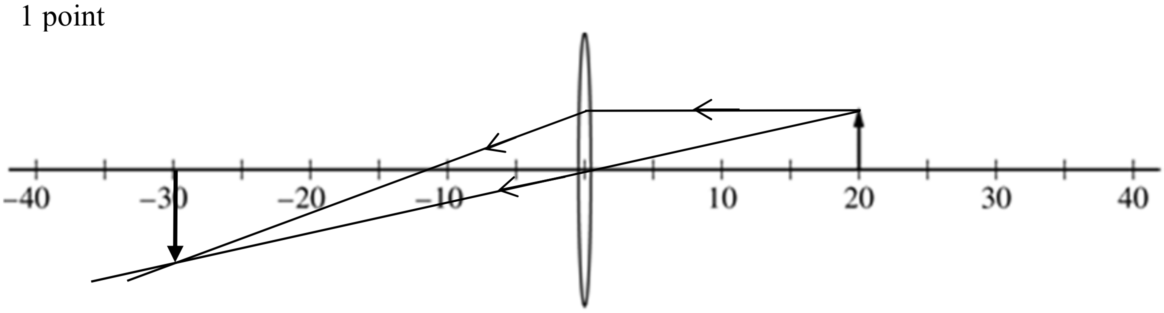
For correctly showing a calculation of the magnitude of the magnification (with or without sign) and a correct answer — 1 point

$M = d_i/d_o = 30\text{ cm}/20\text{ cm}$

$M = 1.5$

(c)

i. 1 point



For two reasonably correctly drawn rays consistent with the calculated focal length, and inclusion of an inverted image — 1 point

2017 SCORING GUIDELINES

Question 3 (continued)

Distribution of points

(c) (continued)

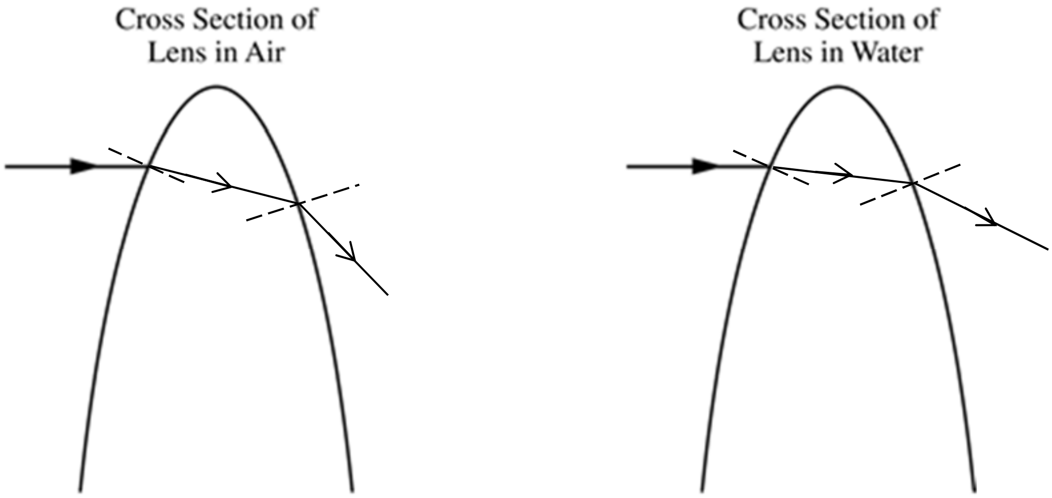
ii. 2 points

For a correct explanation of how the rays drawn relate to the focal length	1 point
For a correct explanation of how the image relates to the magnification	1 point

Example: The horizontal ray from the object bends to cross the axis at 12 cm from the middle of the lens, which is the focal length. The image arrow is about 1.5 times the height of the object, which is the magnification.

(d)

i. 2 points



For showing the downward refraction of the rays at each surface of the lens in air (i.e., toward the normal entering the lens and away from the normal leaving the lens)	1 point
For the rays refracted by the lens in water at greater angles to the normal than the corresponding angles for the lens in air — i.e., less bending (can be earned even if first point was not, scoring is relative to whatever is drawn for the lens in air)	1 point

ii. 3 points

For describing a greater focal length when the lens is in water or a comparison consistent with part (d)(i)	1 point
For describing a larger image distance and image size or a comparison consistent with part (d)(i)	1 point
For describing how the rays drawn in (d)(i) support the descriptions	1 point

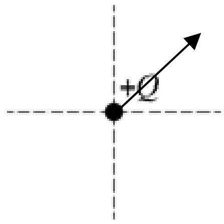
Example: The rays do not bend as much as they pass from water to glass as when they pass from air to glass (and vice versa). This means parallel rays coming into the lens will converge at a farther distance, so the focal length is longer. Rays from an object also will converge farther from the lens, so the new image is farther and larger.

2017 SCORING GUIDELINES

Question 4

10 points total | **Distribution of points**

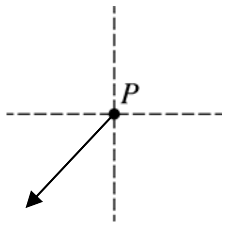
(a) 1 point



For an arrow pointing outward from the object, along a diagonal of the square and away from the object with charge $-2Q$, with no other arrows — 1 point

(b)

i. 3 points



For correctly determining magnitudes of the field from individual objects — 1 point

The fields from the $+2Q$ objects cancel. This can be implicit or explicit in the calculations.

For the $-2Q$ object, $E = 2kQ/d^2$

For the $+Q$ object, $E = kQ/d^2$

For correctly adding the individual fields — 1 point

$E = 3kQ/d^2$

For showing the correct direction on the diagram, along a diagonal of the square and toward the object with charge $-2Q$ — 1 point

ii. 1 point

For showing a correct scalar potential summation — 1 point

A final answer is not required; however, no credit is given if an incorrect final answer is included.

$V = (k/d)(+2Q + Q + 2Q - 2Q) = 3kQ/d$

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Question 4 (continued)

	Distribution of points
(c) 5 points	
For indicating that electric potential energy is the energy stored in a configuration of charged objects	1 point
For indicating that the change in potential energy is equal to the work done by an external force to create a particular configuration	1 point
For indicating that moving the object with $+2Q$ charge results in an increase in energy and indicating that moving the object with $+Q$ charge results in a decrease in energy (i.e., for showing understanding that moving charges of the same sign closer together increases the energy and/or moving charges of opposite sign closer together decreases the energy, with some support such as $U = kqQ/r$ or a description of doing work against forces)	1 point
For indicating that the net result is an increase in the energy with some explanation	1 point
For a logical, relevant, and internally consistent response that addresses the required argument or question asked, and follows the guidelines described in the published requirements for the paragraph-length response	1 point