

## 6.6 Motion of Orbiting Satellites

Name: \_\_\_\_\_ Class: \_\_\_\_\_ Date: \_\_\_\_\_

Total: 9 marks

KEY WORDS satellite 卫星 • orbital speed 轨道速度

### Objective

Build the skills to answer exam questions on **the motion of orbiting satellites**.

You must be able to:

- explain how **gravity** provides the centripetal force that keeps a satellite in orbit
- relate the **orbital speed** 轨道速度 to the radius with  $\frac{GMm}{r^2} = \frac{mv^2}{r}$
- describe the energy of a satellite as kinetic plus gravitational potential energy

### 1 Worked examples

Study these first. Each one shows the method for a question type used later.

#### ■ Gravity is the centripetal force

Setting the gravitational force equal to the required centripetal force:

$$\frac{GMm}{r^2} = \frac{mv^2}{r} \Rightarrow v = \sqrt{\frac{GM}{r}}.$$

#### ■ Closer orbits are faster

Because  $v \propto 1/\sqrt{r}$ , a satellite in a **lower** orbit moves **faster**.

#### ■ Energy

A satellite has kinetic energy  $\frac{1}{2}mv^2$  and (negative) gravitational potential energy; the two together give its total orbital energy.

### 2 Practice

2.1 State what provides the centripetal force on an orbiting satellite. [1]

2.2 State how the orbital speed changes if the orbital radius increases. [1]

2.3 Write the equation obtained by setting the gravitational force equal to the centripetal force. [1]

### 3 Exam-style questions

3.1 The centripetal force on a satellite in orbit is provided by [1]

|   |   |
|---|---|
| A | B |
| C | D |

- A its engine  
B gravity  
C air resistance  
D the normal force

3.2 As the orbital radius increases, the orbital speed [1]

|   |   |
|---|---|
| A | B |
| C | D |

- A increases  
B decreases  
C stays constant  
D becomes zero

3.3 A satellite orbits Earth ( $M = 6.0 \times 10^{24}$  kg,  $G = 6.67 \times 10^{-11}$  N m<sup>2</sup> kg<sup>-2</sup>) at radius  $r = 7.0 \times 10^6$  m.(a) Write the expression  $v = \sqrt{GM/r}$ . [1]

(b) Find the orbital speed. [3]