

# 1.4 Reference Frames and Relative Motion

Name: \_\_\_\_\_ Class: \_\_\_\_\_ Date: \_\_\_\_\_

Total: 10 marks

## Objective

Build the skills to answer exam questions on **reference frames and relative motion**.

You must be able to:

- define a **reference frame** 参考系 as the coordinate system an observer measures from
- explain that **displacement** and **velocity** depend on the observer's reference frame
- use **vector addition** to find a velocity relative to a different frame
- explain that **acceleration** is the same in all **inertial reference frames** 惯性参考系

## 1 Worked examples

Study these first. Each one shows the method for a question type used later.

### ■ Relative velocity in one dimension

The velocity of A relative to C is  $v_{A/C} = v_{A/B} + v_{B/C}$ . A passenger walks at  $+2 \text{ m s}^{-1}$  on a train moving at  $+30 \text{ m s}^{-1}$ : relative to the ground the passenger moves at  $+32 \text{ m s}^{-1}$ .

### ■ Reversing a subscript

$v_{A/B} = -v_{B/A}$ . If the train moves at  $+30 \text{ m s}^{-1}$  relative to the ground, the ground moves at  $-30 \text{ m s}^{-1}$  relative to the train.

### ■ The same acceleration in every inertial frame

Two observers moving at constant velocity relative to each other measure **different velocities** but the **same acceleration** — a constant relative velocity adds a constant, and the rate of change of a constant is zero.

## 2 Practice

**2.1** A boat moves at  $+4.0 \text{ m s}^{-1}$  relative to the water; the water flows at  $+1.0 \text{ m s}^{-1}$  relative to the bank. Find the boat's velocity relative to the bank. [1]

**2.2** A car moves at  $+20 \text{ m s}^{-1}$  relative to the road. Find the road's velocity relative to the car. [1]

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**2.3** Two cars drive directly toward each other, each at  $15 \text{ m s}^{-1}$  relative to the road. Find the velocity of one car relative to the other. [2]

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**2.4** Explain why two observers in different inertial frames measure the same acceleration for one object. [2]

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### 3 Exam-style questions

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**3.1** Quantities that depend on the reference frame include [1]

- **A** velocity but not acceleration
  - **B** acceleration but not velocity
  - **C** both velocity and acceleration
  - **D** neither velocity nor acceleration
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**3.2** A person walks at  $1.5 \text{ m s}^{-1}$  toward the back of a bus moving forward at  $12 \text{ m s}^{-1}$ . The person's velocity relative to the ground is [1]

- **A**  $13.5 \text{ m s}^{-1}$  forward
  - **B**  $10.5 \text{ m s}^{-1}$  forward
  - **C**  $1.5 \text{ m s}^{-1}$  backward
  - **D**  $12 \text{ m s}^{-1}$  forward
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**3.3** A plane flies at  $200 \text{ m s}^{-1}$  east relative to the air. A wind blows relative to the ground.

(a) Find the plane's ground velocity if the wind blows at  $30 \text{ m s}^{-1}$  east. [1]

(b) State its ground velocity if the wind instead blows  $30 \text{ m s}^{-1}$  west.

[1]

#### 4 Go further

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- work through the **1.4 Reference Frames and Relative Motion** lesson on the **Learn** page;
- read the **Kinematics** section of the AP Physics 1 handout on the **Know** page.

## Solutions

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**2.1**  $+4.0 + 1.0 = +5.0 \text{ m s}^{-1}$ .

**2.2**  $-20 \text{ m s}^{-1}$ .

**2.3** Take one car as  $+15$  and the other as  $-15$ ; relative velocity =  $(+15) - (-15) = 30 \text{ m s}^{-1}$ , closing.

**2.4** Their relative velocity is constant, so their measured velocities differ by a constant amount; the rate of change of velocity —the acceleration —is therefore the same.

**3.1 A.**

**3.2 B**  $-12 + (-1.5) = 10.5 \text{ m s}^{-1}$  forward.

**3.3** (a)  $200 + 30 = 230 \text{ m s}^{-1}$  east. (b)  $200 - 30 = 170 \text{ m s}^{-1}$  east.