

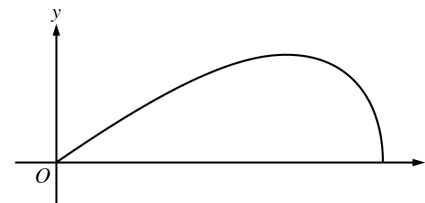
5. The graphs of the functions f and g are shown in the figure for $0 \leq x \leq 3$. It is known that $g(x) = \frac{12}{3+x}$

for $x \geq 0$. The twice-differentiable function f , which is not explicitly given, satisfies $f(3) = 2$ and

$$\int_0^3 f(x) \, dx = 10.$$

- Find the area of the shaded region enclosed by the graphs of f and g .
- Evaluate the improper integral $\int_0^\infty (g(x))^2 \, dx$, or show that the integral diverges.
- Let h be the function defined by $h(x) = x \cdot f'(x)$. Find the value of $\int_0^3 h(x) \, dx$.

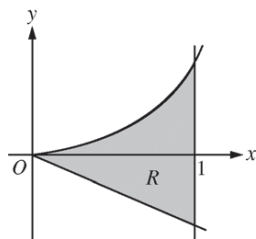
Write your responses to this question only on the designated pages in the separate Free Response booklet. Write your solution to each part in the space provided for that part.



A company designs spinning toys using the family of functions $y = cx\sqrt{4-x^2}$, where c is a positive constant. The figure above shows the region in the first quadrant bounded by the x -axis and the graph of $y = cx\sqrt{4-x^2}$, for some c . Each spinning toy is in the shape of the solid generated when such a region is revolved about the x -axis. Both x and y are measured in inches.

- Find the area of the region in the first quadrant bounded by the x -axis and the graph of $y = cx\sqrt{4-x^2}$ for $c = 6$.
- It is known that, for $y = cx\sqrt{4-x^2}$, $\frac{dy}{dx} = \frac{c(4-2x^2)}{\sqrt{4-x^2}}$. For a particular spinning toy, the radius of the largest cross-sectional circular slice is 1.2 inches. What is the value of c for this spinning toy?
- For another spinning toy, the volume is 2π cubic inches. What is the value of c for this spinning toy?

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5. Let R be the shaded region bounded by the graph of $y = xe^{x^2}$, the line $y = -2x$, and the vertical line $x = 1$, as shown in the figure above.
- (a) Find the area of R .
 - (b) Write, but do not evaluate, an integral expression that gives the volume of the solid generated when R is rotated about the horizontal line $y = -2$.
 - (c) Write, but do not evaluate, an expression involving one or more integrals that gives the perimeter of R .