

4.1 Interpreting the Meaning of the Derivative in Context

Name: _____ Class: _____ Date: _____ Total: 9 marks

KEY WORDS units 单位

Objective

Build the skills to answer exam questions on **interpreting the meaning of the derivative in context**.

You must be able to:

- give the **units** 单位 of a derivative
- interpret its sign and value in a real context

1 Worked examples

Study these first. Each one shows the method for a question type used later.

■ The derivative in context

A derivative is a **rate of change** with units: if $V(t)$ is a volume in cm^3 at time t (s), then $V'(t)$ is in cm^3/s .

- $f'(t) > 0$: the quantity is increasing;
- $f'(t) < 0$: it is decreasing.

2 Practice

2.1 State the units of $f'(t)$ if f is in metres and t in seconds. [1]

2.2 State what a positive derivative means. [1]

2.3 If $P(t)$ is a population and $P'(5) = 200$, interpret this. [2]

3 Exam-style questions

3.1 If $h(t)$ is a height in m and t in s, then $h'(t)$ has units [1]

- | | |
|---|---|
| A | B |
| C | D |
- A m
B m/s
C s/m
D m · s

3.2 A positive $f'(t)$ means the quantity is [1]

- | | |
|---|---|
| A | B |
| C | D |
- A decreasing
B increasing
C constant
D zero

3.3 $W(t)$ is water in litres at time t (min), and $W'(3) = -4$.

(a) State the units. [1]

(b) State what the sign means. [1]

(c) Interpret $W'(3) = -4$. [1]