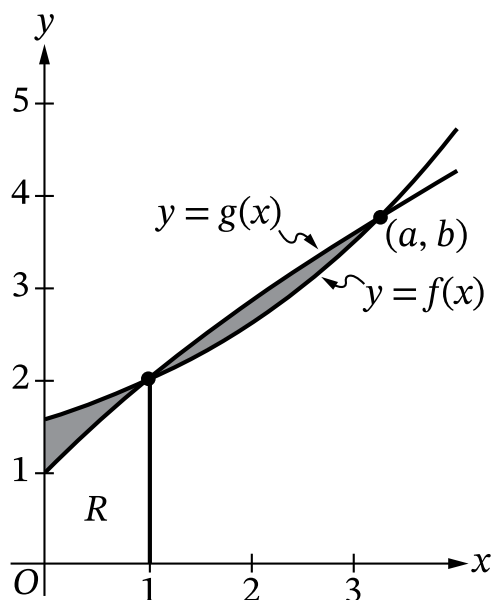


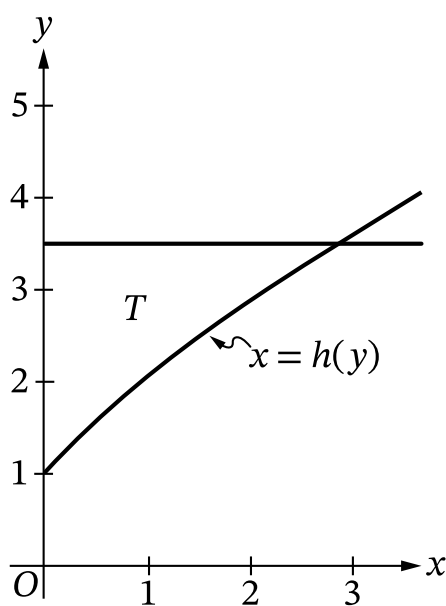
2. The function f is defined by $f(x) = 1.43^x + 0.57$, and the function g is defined by $g(x) = \frac{14x + 12}{x + 12}$. The graphs of f and g intersect at the points $(1, 2)$ and (a, b) , as shown in Figure 1.

Figure 1



For $x \geq 0$, the equation $y = g(x)$ can be rewritten as $x = h(y) = \frac{12y - 12}{14 - y}$, where h is a function of y . The graph of $x = h(y)$ and the horizontal line $y = 3.5$ are shown in Figure 2.

Figure 2



Part A

Let R be the region bounded by the graph of g , the x -axis, the y -axis, and the vertical line $x = 1$, as shown in Figure 1. Find the area of region R . Show the setup for your calculations.

Part B

Region R , described in part A, is the base of a solid. For this solid, each cross section perpendicular to the x -axis is a rectangle whose height is $\frac{1}{3}$ times the length of its base in region R . Write, but do not evaluate, an integral expression that gives the volume of the solid.

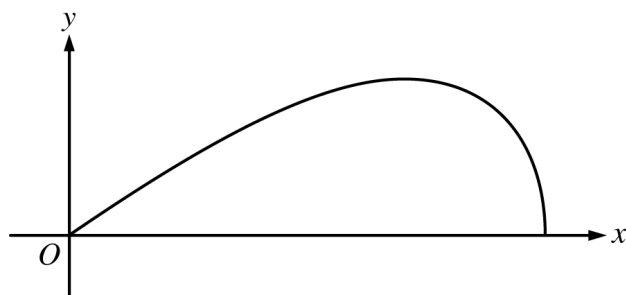
Part C

The shaded region in Figure 1 is bounded by the graphs of f and g on the interval from $x = 0$ to $x = a$. Find the area of the shaded region. Show the setup for your calculations.

Part D

Let T be the region bounded by the graph of $x = h(y)$, the y -axis, and the horizontal line $y = 3.5$, as shown in Figure 2. Write, but do not evaluate, an integral expression that gives the volume of the solid generated when region T is revolved about the y -axis.

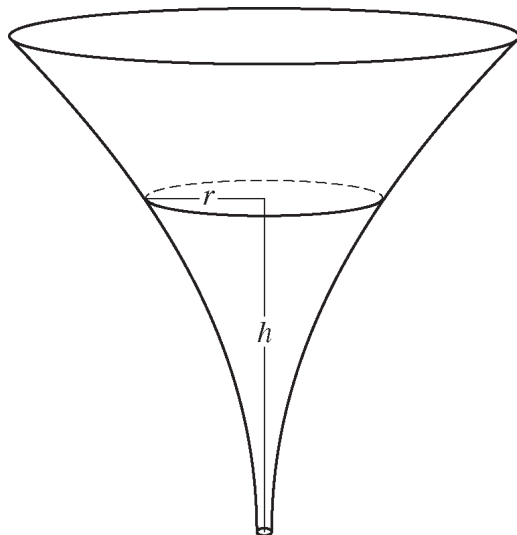
END OF PART A



A company designs spinning toys using the family of functions $y = cx\sqrt{4 - x^2}$, where c is a positive constant. The figure above shows the region in the first quadrant bounded by the x -axis and the graph of $y = cx\sqrt{4 - x^2}$, for some c . Each spinning toy is in the shape of the solid generated when such a region is revolved about the x -axis. Both x and y are measured in inches.

- (a) Find the area of the region in the first quadrant bounded by the x -axis and the graph of $y = cx\sqrt{4 - x^2}$ for $c = 6$.
- (b) It is known that, for $y = cx\sqrt{4 - x^2}$, $\frac{dy}{dx} = \frac{c(4 - 2x^2)}{\sqrt{4 - x^2}}$. For a particular spinning toy, the radius of the largest cross-sectional circular slice is 1.2 inches. What is the value of c for this spinning toy?
- (c) For another spinning toy, the volume is 2π cubic inches. What is the value of c for this spinning toy?

Write your responses to this question only on the designated pages in the separate Free Response booklet. Write your solution to each part in the space provided for that part.



5. The inside of a funnel of height 10 inches has circular cross sections, as shown in the figure above. At height h , the radius of the funnel is given by $r = \frac{1}{20}(3 + h^2)$, where $0 \leq h \leq 10$. The units of r and h are inches.
- (a) Find the average value of the radius of the funnel.
 - (b) Find the volume of the funnel.
 - (c) The funnel contains liquid that is draining from the bottom. At the instant when the height of the liquid is $h = 3$ inches, the radius of the surface of the liquid is decreasing at a rate of $\frac{1}{5}$ inch per second. At this instant, what is the rate of change of the height of the liquid with respect to time?
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