

| $x$ | $f(x)$ | $f'(x)$ | $g(x)$ | $g'(x)$ |
|-----|--------|---------|--------|---------|
| 1   | -6     | 3       | 2      | 8       |
| 2   | 2      | -2      | -3     | 0       |
| 3   | 8      | 7       | 6      | 2       |
| 6   | 4      | 5       | 3      | -1      |

6. The functions  $f$  and  $g$  have continuous second derivatives. The table above gives values of the functions and their derivatives at selected values of  $x$ .

(a) Let  $k(x) = f(g(x))$ . Write an equation for the line tangent to the graph of  $k$  at  $x = 3$ .

(b) Let  $h(x) = \frac{g(x)}{f(x)}$ . Find  $h'(1)$ .

(c) Evaluate  $\int_1^3 f''(2x) dx$ .

**STOP**

**END OF EXAM**

| $x$     | -2 | $-2 < x < -1$ | -1            | $-1 < x < 1$ | 1 | $1 < x < 3$ | 3             |
|---------|----|---------------|---------------|--------------|---|-------------|---------------|
| $f(x)$  | 12 | Positive      | 8             | Positive     | 2 | Positive    | 7             |
| $f'(x)$ | -5 | Negative      | 0             | Negative     | 0 | Positive    | $\frac{1}{2}$ |
| $g(x)$  | -1 | Negative      | 0             | Positive     | 3 | Positive    | 1             |
| $g'(x)$ | 2  | Positive      | $\frac{3}{2}$ | Positive     | 0 | Negative    | -2            |

5. The twice-differentiable functions  $f$  and  $g$  are defined for all real numbers  $x$ . Values of  $f$ ,  $f'$ ,  $g$ , and  $g'$  for various values of  $x$  are given in the table above.

(a) Find the  $x$ -coordinate of each relative minimum of  $f$  on the interval  $[-2, 3]$ . Justify your answers.

(b) Explain why there must be a value  $c$ , for  $-1 < c < 1$ , such that  $f''(c) = 0$ .

(c) The function  $h$  is defined by  $h(x) = \ln(f(x))$ . Find  $h'(3)$ . Show the computations that lead to your answer.

(d) Evaluate  $\int_{-2}^3 f'(g(x))g'(x) dx$ .