

5.4 The First Derivative Test

Name: _____ Class: _____ Date: _____ Total: 9 marks

KEY WORDS local minimum 极小值 • local maximum 极大值 • local extremum 局部极值
• critical point 临界点

Objective

Build the skills to answer exam questions on the **First Derivative Test**.

You must be able to:

- use the sign change of f' to classify a **local extremum** 局部极值

1 Worked examples

Study these first. Each one shows the method for a question type used later.

■ First Derivative Test

At a critical point, look at how f' changes:

- + to – → local **maximum**;
- – to + → local **minimum**;
- no sign change → neither.

■ Example

$f'(x) = 2x - 4$ at $x = 2$: f' goes – (for $x < 2$) to + (for $x > 2$), so $x = 2$ is a local minimum.

2 Practice

2.1 State the sign change for a local maximum. [1]

2.2 State the sign change for a local minimum. [1]

2.3 For $f'(x) = 2x - 4$, classify $x = 2$. [2]

3 Exam-style questions

3.1 A local maximum occurs where f' changes [1]

- | | |
|---|---|
| A | B |
| C | D |
- A – to +
B + to –
C stays +
D stays –

3.2 A local minimum occurs where f' changes [1]

- | | |
|---|---|
| A | B |
| C | D |
- A + to –
B – to +
C stays 0
D never

3.3 $f'(x) = 2x - 4$, critical at $x = 2$.

(a) State the sign of f' for $x < 2$. [1]

(b) State the sign for $x > 2$. [1]

(c) Classify $x = 2$. [1]