

1.10 Exploring Types of Discontinuities

Name: _____ Class: _____ Date: _____ **Total: 9 marks**

KEY WORDS discontinuity 不连续点 • infinite discontinuity 无穷间断
• jump discontinuity 跳跃间断 • removable discontinuity 可去间断 • jump 跳跃

Objective

Build the skills to answer exam questions on **types of discontinuities**.

You must be able to:

- classify a **discontinuity** 不连续点 as removable, jump, or infinite

1 Worked examples

Study these first. Each one shows the method for a question type used later.

■ Three types of discontinuity

- **removable** (a **hole**): the limit exists but $\neq f(a)$, or $f(a)$ is undefined;
- **jump**: the left and right limits differ;
- **infinite**: a vertical asymptote (the function blows up).

2 Practice

2.1 Name the three types of discontinuity. [1]

2.2 State which type is a “hole”. [1]

2.3 State which type occurs at a vertical asymptote. [2]

3 Exam-style questions

3.1 A discontinuity where the left and right limits differ is a [1]

A	B
C	D

- A removable discontinuity
- B jump discontinuity
- C infinite discontinuity
- D point of continuity

3.2 A hole in a graph is a [1]

A	B
C	D

- A jump discontinuity
- B removable discontinuity
- C infinite discontinuity
- D point of continuity

3.3 Classify each.

(a) A vertical asymptote. [1]

(b) A single missing point. [1]

(c) A step where the graph jumps. [1]