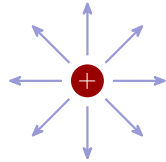


## Electric Fields

A2 Physics ■ Topic 18

A-Level Physics



Electric Fields

### What we will cover

- 1 Fields & field lines
- 2 Uniform fields:  $E = V/d$
- 3 Coulomb's law
- 4 The field of a point charge
- 5 Electric potential
- 6 Recap



# 1 Fields and field lines

## Electric field strength



An **electric field** 电场 is a region where a charge feels a force. Its **field strength** 电场强度 is the force per unit **positive** charge:

$$E = \frac{F}{q} \Rightarrow F = qE, \quad [E] = \text{N C}^{-1}$$

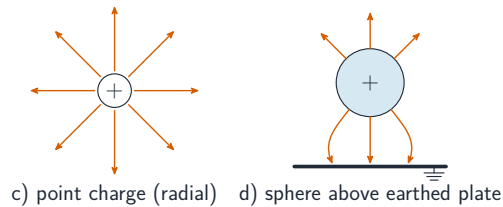
Defined on a **positive** test charge – so a **negative** charge feels a force **against** the field.

## Field-line patterns

a) parallel plates (uniform field) b) dipole (+ and -)



- they run **from + to -** (or off to infinity)
- they **never cross**
- **closer lines** = stronger field



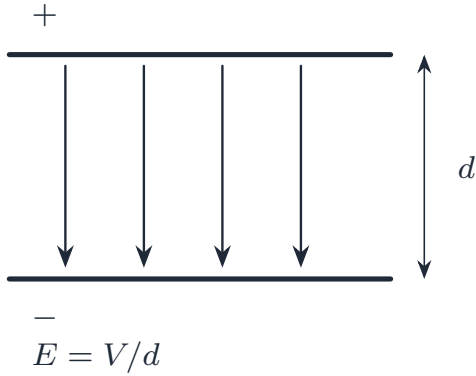
c) point charge (radial) d) sphere above earthed plate

Two crossing lines would give the force at that point **two** directions at once – impossible, which is why it never happens.

## 2

## Uniform fields

## The uniform field between plates



Plates a distance  $d$  apart with p.d.  $V$  across them:

$$E = \frac{V}{d}$$

pointing from the **high**-potential plate to the low.

This is where  $\text{V m}^{-1}$  comes from – and it is the **same unit** as  $\text{N C}^{-1}$ .

## Worked example – plates and an electron

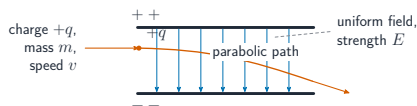
**Plates 5.0 mm apart carry a p.d. of 200 V. Find  $E$ , and the force on an electron between them. ( $e = 1.6 \times 10^{-19} \text{ C}$ )**

$$E = \frac{V}{d} = \frac{200}{5.0 \times 10^{-3}} = 4.0 \times 10^4 \text{ V m}^{-1}$$

$$F = qE = (1.6 \times 10^{-19})(4.0 \times 10^4) = 6.4 \times 10^{-15} \text{ N}$$

Convert **mm** to **m** first – forgetting it scales  $E$  by a thousand. The force is the **same everywhere** in the gap: that is what uniform means.

## A charge crossing a uniform field



Constant force  $\Rightarrow$  constant acceleration  
 $a = qE/m$ :

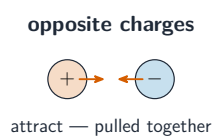
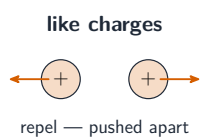
- released **at rest**: speeds up along the field, gaining KE
- entering **at right angles**: a **parabolic** 抛物线 path

Exactly a **projectile** 抛体 problem – steady velocity across, uniform acceleration down. This is how a **cathode-ray tube** 阴极射线管 steered its beam.

# 3 Coulomb's law

Electric Fields  
└ Coulomb's law

## Coulomb's law



$$F = \frac{Q_1 Q_2}{4\pi\epsilon_0 r^2}$$

with  $\epsilon_0 = 8.85 \times 10^{-12} \text{ F m}^{-1}$   
and  $\frac{1}{4\pi\epsilon_0} \approx 9.0 \times 10^9 \text{ N m}^2 \text{ C}^{-2}$ .

Inverse square, along the joining line – **like repels**, **opposite attracts**. That sign choice is the one thing gravity cannot do.

Electric Fields  
└ Coulomb's law

## Worked example – two point charges

**Find the force between  $+2.0 \text{ nC}$  and  $+3.0 \text{ nC}$  set  $4.0 \text{ cm}$  apart.**

$$F = \frac{(9.0 \times 10^9)(2.0 \times 10^{-9})(3.0 \times 10^{-9})}{(0.040)^2}$$
$$\approx 3.4 \times 10^{-5} \text{ N, and repulsive (both +)}$$

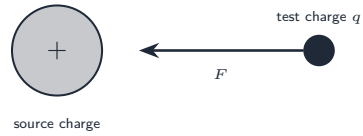
State the **direction** as well as the size – “repulsive” is part of the answer. And  $r$  goes in as **metres**, squared.

## Spheres as point charges

A charged spherical **conductor** 导体 of total charge  $Q$ :

- **outside**: identical to a point charge  $Q$  at its centre (measure  $r$  from the centre)
- **inside** a hollow one: the field is **zero**

Zero field inside makes the whole conductor one **equipotential** 等势面 – and is why a car shields you from lightning.



$$E = F/q \quad (\text{NC}^{-1})$$

# 4 Field of a point charge

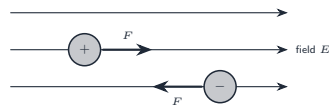
## The field of a point charge

Coulomb's law gives the force between **two** charges. Divide by the test charge and only the **source** is left:

$$E = \frac{F}{q} = \frac{Q}{4\pi\epsilon_0 r^2}$$

Out of a positive  $Q$ , into a negative one, falling as  $1/r^2$ .

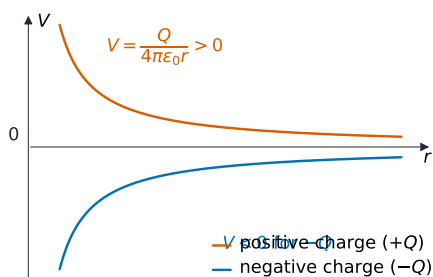
The same shape as  $g = GM/r^2$  – but charges can **cancel**, so for several of them add the fields as a **vector** sum.



# 5 Electric potential

Electric Fields  
└ Electric potential

## Electric potential



**Potential** 电势 is the work done per unit **positive** charge bringing a test charge in from **infinity** 无穷远:

$$V = \frac{W}{q} = \frac{Q}{4\pi\epsilon_0 r}$$

Note  $1/r$ , not  $1/r^2$ .  $V$  is a **scalar** and takes the sign of  $Q$  – so several charges just **add**, signs and all, with no directions to resolve.

Electric Fields  
└ Electric potential

## Worked example – potential near a charge

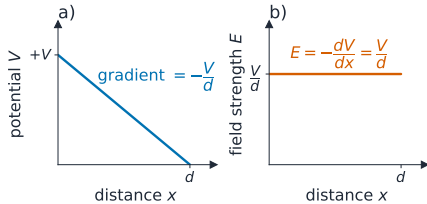
**Find  $V$  at 4.0 cm from a point charge of +3.0 nC.**

$$V = \frac{Q}{4\pi\epsilon_0 r} = \frac{(9.0 \times 10^9)(3.0 \times 10^{-9})}{0.040} \approx 6.8 \times 10^2 \text{ V}$$

Same charge, same distance as the Coulomb example – but  $r$  appears to the **first** power here. Mixing up  $1/r$  and  $1/r^2$  is the standard slip.

## Field is the potential gradient

$$E = -\frac{dV}{dx}$$



■ between plates  $V$  falls evenly  $\Rightarrow$   
 $E = V/d$ , constant

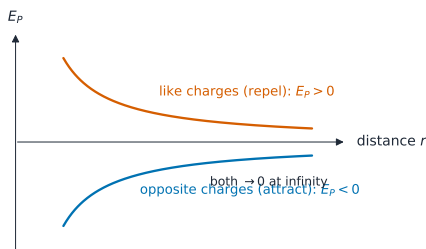
■ for a point charge  
 $-\frac{dV}{dr} = \frac{Q}{4\pi\epsilon_0 r^2} = E$

The minus sign says the field points **downhill** in potential – from high  $V$  to low.

## Electric potential energy

A charge  $q$  where the potential is  $V$  has  
 $E_P = qV$ ; for two point charges

$$E_P = \frac{Qq}{4\pi\epsilon_0 r}$$



■ **like:**  $E_P > 0$  – energy released if they fly apart

■ **opposite:**  $E_P < 0$  – a **bound** 束缚 well

Both tend to **zero** as  $r \rightarrow \infty$  – that is the choice of zero, exactly as for gravity.

## Gravitational vs electric

| Quantity       | Gravitational       | Electric                     |
|----------------|---------------------|------------------------------|
| Source         | mass $M$ (always +) | charge $Q$ (either sign)     |
| Field strength | $g = GM/r^2$        | $E = Q/(4\pi\epsilon_0 r^2)$ |
| Force          | $F = mg$            | $F = qE$                     |
| Potential      | $\phi = -GM/r$      | $V = Q/(4\pi\epsilon_0 r)$   |
| PE of two      | $-GMm/r$            | $Qq/(4\pi\epsilon_0 r)$      |
| Nature         | always attractive   | attract <i>or</i> repel      |

Identical machinery, one difference: gravity's minus sign is **permanent** (mass only attracts), while the electric sign is inherited from the **charge**.

# 6

## Recap

Electric Fields  
↳ Recap

### Topic 18 – key takeaways

#### 1 Coulomb

$F = Q_1 Q_2 / 4\pi\epsilon_0 r^2$  – attract or repel

#### 2 Two fields

uniform  $E = V/d$ ; radial  $E = Q / 4\pi\epsilon_0 r^2$

#### 3 Potential

$V = Q / 4\pi\epsilon_0 r$  – scalar, signed,  $1/r$

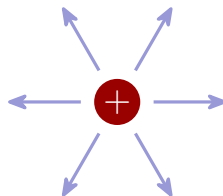
#### 4 The link

$E = -dV/dx$  – the field points downhill in  $V$

Electric Fields  
↳ Recap

### Check yourself

- 1 Which way does a field line point?
- 2 Halve the plate gap at fixed  $V$  – what happens to  $E$ ?
- 3 Is potential a vector or a scalar?
- 4 What is the field inside a hollow charged sphere?



**Answers** 1. the force on a + charge 2. doubles 3. scalar 4. zero