

4.1 Turning effects of forces

Name: _____ Class: _____ Date: _____

Total: 27 marks

KEY WORDS force 力 • moment 力矩 • weight 重力 • couple 力偶 • torque 力偶矩

Objective

Build the skills to answer exam questions on the **turning effects of forces** — centre of gravity, moments, couples and torque.

You must be able to:

- use the **centre of gravity** 重心 when drawing weight
- define and calculate the **moment** 力矩 of a force
- define a **couple** and calculate its **torque** 力偶矩
- locate the **centre of gravity** of a hanging object, and use a torque to find how far it lies from the pivot

1 Worked examples

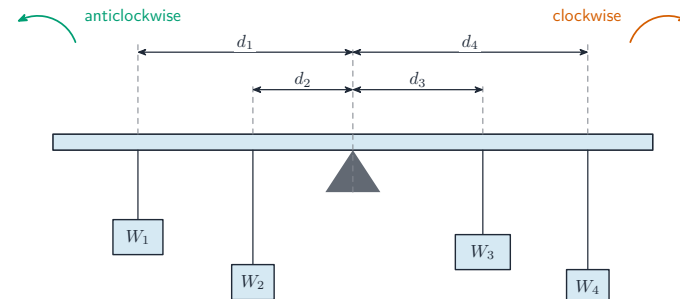
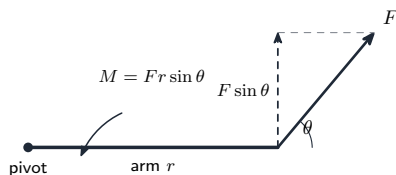
Study these first. Each one shows the method for a question type used later — follow the steps and you can do the Practice and Exam-style questions yourself.

■ Centre of gravity and moment

The whole **weight** acts at the **centre of gravity** (the middle of a uniform shape). The **moment** of a force about a point is

$$M = F \times d,$$

where d is the **perpendicular distance** from the point to the force's line of action. If the force acts at angle θ to a lever arm of length r , then $M = Fr \sin \theta$ — only the part **perpendicular** to the arm turns it:



The principle of moments balances turning effects

Worked example. 50 N at the end of a 0.40 m spanner, at 30° to it:

$$M = 50 \times 0.40 \times \sin 30^\circ = 10 \text{ N m.}$$

■ Finding a centre of gravity

For a **non-uniform** object the centre of gravity is not at the middle, and the exam asks you to find it two ways.

Hang it up. An object free to swing settles with its centre of gravity **vertically below** the point it hangs from. So the centre of gravity lies **somewhere on that vertical line** — hang it from a second point and the two lines cross at it.

Hold it still. If the object is held so that its centre of gravity is a horizontal distance d from the pivot, the weight has a moment mgd about the pivot, and the torque you must apply is equal and opposite:

$$\tau = mgd \Rightarrow d = \frac{\tau}{mg}$$

Worked example. Holding a 2.0 kg non-uniform plate on a rod takes a torque of 1.6 N m:

$$d = \frac{1.6}{2.0 \times 9.81} = 0.082 \text{ m}$$

The direction tells you which side: if the centre of gravity is to the **right** of the rod, the weight turns the plate **clockwise**, so the applied torque must be **anticlockwise**.

■ Couple and torque

A **couple** is two forces that are **equal, opposite**, and a perpendicular distance apart — it produces **turning only** (zero resultant force). Its **torque** is

$$\tau = F \times d,$$

where d is the distance between the two lines of action. (*Two equal forces in the **same** direction are **not** a couple.*)

2 Practice

Now apply the methods above.

2.1 Define the **moment** of a force. [1]

2.2 A 20 N force acts at right angles to a lever, 0.30 m from the pivot. Find its **moment**. [2]

2.3 State the **two** conditions a pair of forces must meet to be a **couple**. [2]

2.4 State where the **weight** of a uniform rod acts. [1]

3 Exam-style questions

3.1 The **moment** of a force is measured in: [1]

- A N
- B N m
- C N m⁻¹
- D J

3.2 A force of 50 N is applied at the end of a 0.40 m spanner, at 30° to the spanner. Calculate the **moment** about the nut. [2]

3.3 Two parallel forces, each 8.0 N, act in opposite directions 0.25 m apart, forming a couple. Calculate the **torque**. [2]

3.4 Explain why two **equal** forces acting in the **same** direction do **not** form a couple. [2]

3.5 A square aluminium sheet of **non-uniform** density has a mass of 1.6 kg and a uniform thickness of 3.0 mm. A thin rod of negligible mass is fixed through the centre of the sheet, and the sheet hangs vertically from the rod. To hold the sheet still, with one corner directly above the rod, a torque of 1.9 N m must be applied. In that position the centre of gravity of the sheet lies to the **right** of the rod.

(a) Define the **torque of a couple**. [2]

(b) Explain what is meant by the **centre of gravity** of the sheet. [1]

(c) **Show that** the centre of gravity of the sheet is a horizontal distance of about 0.12 m from the rod. [2]

- the centre of gravity is to the right of the rod, so the weight turns the sheet **clockwise**; the applied torque must oppose it

(e) $V = m/\rho$

$$V = \frac{1.6 \text{ kg}}{2700 \text{ kg m}^{-3}} = 5.93 \times 10^{-4} \text{ m}^3$$

- square sheet: $V = L^2 t$

$$L^2 = \frac{5.93 \times 10^{-4} \text{ m}^3}{3.0 \times 10^{-3} \text{ m}} = 0.198 \text{ m}^2 \Rightarrow L = \mathbf{0.44 \text{ m}}$$

(f) directly **below** that corner, on the vertical line through it

(g)

$$V = L^2 t = (0.44 \text{ m})^2 (5.0 \times 10^{-3} \text{ m}) = 9.68 \times 10^{-4} \text{ m}^3$$

$$m = \rho V = (2700 \text{ kg m}^{-3})(9.68 \times 10^{-4} \text{ m}^3) = 2.61 \text{ kg}$$

$$W = mg = (2.61 \text{ kg})(9.81 \text{ m s}^{-2}) = \mathbf{26 \text{ N}}$$