

1.4 Scalars and vectors

Name: _____ Class: _____ Date: _____

Total: 20 marks

Objective

Build the skills to answer the real exam questions on **scalars and vectors**. In the exam, 1.4 is tested by **multiple-choice** questions and by short parts inside longer questions: classify a quantity, find a **resultant**, or **resolve** a vector into components.

You must be able to:

- tell a **scalar** 标量 from a **vector** 矢量 and complete a classification table
- find the **resultant** 合矢量 of two **perpendicular** 垂直 vectors (size and direction)
- give the direction of $\vec{X} + \vec{Y}$ and $\vec{X} - \vec{Y}$
- find the resultant of **two equal forces** at an angle
- **resolve** 分解 any vector (a force *or* a velocity) into two perpendicular **components** 分量

1 Worked examples

Study these first. Each one shows the method for an exam question type used below — read them and you can do the Practice and Exam-style questions yourself.

■ A —Scalar or vector?

A scalar has size only; a vector has size **and** direction. **Quick test:** if "in which direction?" makes sense, it is a vector. In the exam you often tick a table:

Quantity	Scalar	Vector
speed		
acceleration		
energy		
momentum		

(Common scalars: mass, time, temperature, energy, distance, speed. Common vectors: displacement, velocity, acceleration, force, momentum.)

■ B —Add two perpendicular vectors

Draw them **tip to tail**; the resultant closes the triangle. For two vectors at 90° the size is $|\vec{R}| = \sqrt{X^2 + Y^2}$ and the direction is $\tan \theta = Y/X$.

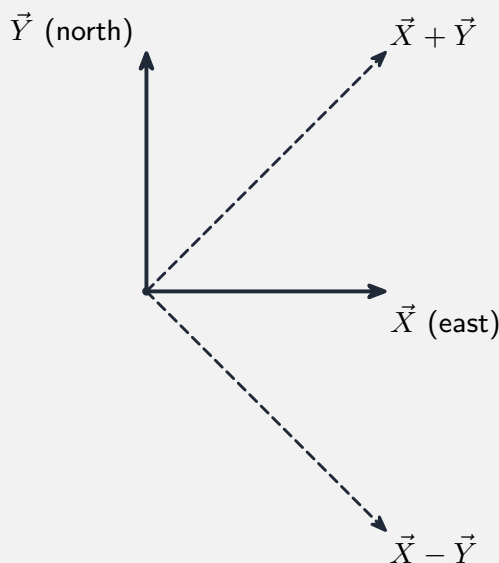
Worked example. A swimmer heads north at 1.2 m s^{-1} ; the river flows east at

0.5 m s^{-1} :

$$|\vec{R}| = \sqrt{1.2^2 + 0.5^2} = 1.3 \text{ m s}^{-1}, \quad \tan \theta = \frac{0.5}{1.2} \Rightarrow \theta \approx 23^\circ \text{ east of north.}$$

■ **C —Direction of $\vec{X} + \vec{Y}$ and $\vec{X} - \vec{Y}$**

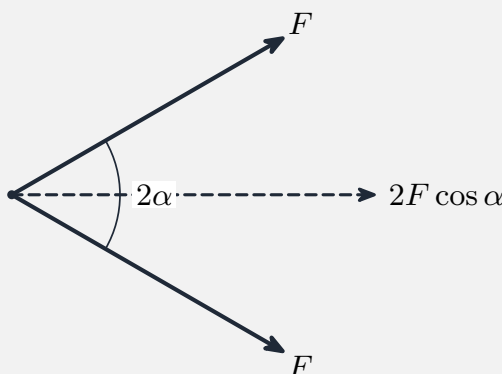
To **add**, place the arrows tip to tail. To **subtract**, reverse the second arrow first: $\vec{X} - \vec{Y} = \vec{X} + (-\vec{Y})$, where $-\vec{Y}$ is the same size as $\vec{Y}$ but points the opposite way.



With $\vec{X}$ east and $\vec{Y}$ north: $\vec{X} + \vec{Y}$ points **north-east**, and $\vec{X} - \vec{Y}$ points **south-east**.

■ **D —Two equal forces at an angle**

Two equal forces of size F with an angle 2α between them have a resultant of size $2F \cos \alpha$, along the line that **cuts the angle in half**.

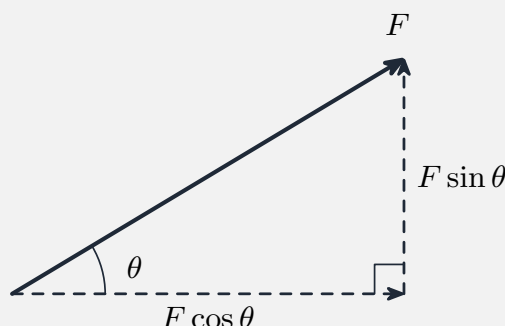


Worked example. Two 6.0 N forces act with 60° between them. Here $2\alpha = 60^\circ$, so $\alpha = 30^\circ$:

$$R = 2F \cos \alpha = 2(6.0) \cos 30^\circ = 10.4 \text{ N.}$$

■ E —Resolve a vector into components

Any vector $\vec{v}$ at angle θ to the horizontal splits into a horizontal part $v \cos \theta$ and a vertical part $v \sin \theta$ —this works for a force **or** a velocity 速度.



Force example. A 50 N force at 30° : horizontal = $50 \cos 30^\circ = 43$ N, vertical = $50 \sin 30^\circ = 25$ N.

Velocity example. A ball kicked at 28 m s^{-1} , 34° above the horizontal: $v_H = 28 \cos 34^\circ = 23 \text{ m s}^{-1}$, $v_V = 28 \sin 34^\circ = 16 \text{ m s}^{-1}$.

On a slope of angle θ , the weight splits into $W \sin \theta$ **along** the slope and $W \cos \theta$ **into** the slope.

2 Practice

Now apply the methods above.

2.1 Complete the table by ticking **scalar** or **vector** for each quantity.

[3]

Quantity	Scalar	Vector
distance		
force		
temperature		
velocity		
power		
acceleration		

2.2 Forces of 3.0 N east and 4.0 N north act at a point. Find the **magnitude** 大小 of the resultant.

[2]

2.3 Resolve a 50 N force acting at 30° to the horizontal into its horizontal and vertical

components.

[2]

2.4 A ball leaves the ground at 20 m s^{-1} at 60° above the horizontal. Find the **horizontal** and **vertical** components of its velocity.

[2]

2.5 Two forces, each 5.0 N , act at a point with 90° between them. Find the **magnitude** of the resultant.

[2]

3 Exam-style questions

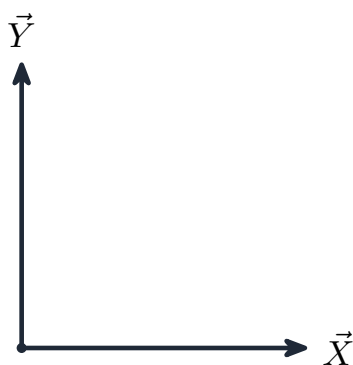
3.1 Which of these is a **vector** quantity?

[1]

- **A** energy
- **B** power
- **C** displacement
- **D** temperature

3.2 Two vectors $\vec{X}$ and $\vec{Y}$ are shown: $\vec{X}$ points east and $\vec{Y}$ points north. What are the directions of $\vec{X} + \vec{Y}$ and $\vec{X} - \vec{Y}$?

[1]



- **A** $\vec{X} + \vec{Y}$ north-east; $\vec{X} - \vec{Y}$ south-east
- **B** $\vec{X} + \vec{Y}$ north-east; $\vec{X} - \vec{Y}$ north-west
- **C** $\vec{X} + \vec{Y}$ south-west; $\vec{X} - \vec{Y}$ south-east
- **D** $\vec{X} + \vec{Y}$ south-east; $\vec{X} - \vec{Y}$ north-east

3.3 Two forces of 6.0 N and 8.0 N act at a point at right angles to each other. What is the magnitude of the resultant force? [1]

- **A** 2.0 N
- **B** 10 N
- **C** 14 N
- **D** 48 N

3.4 A stone is thrown with a velocity of 15 m s^{-1} at 40° above the horizontal.

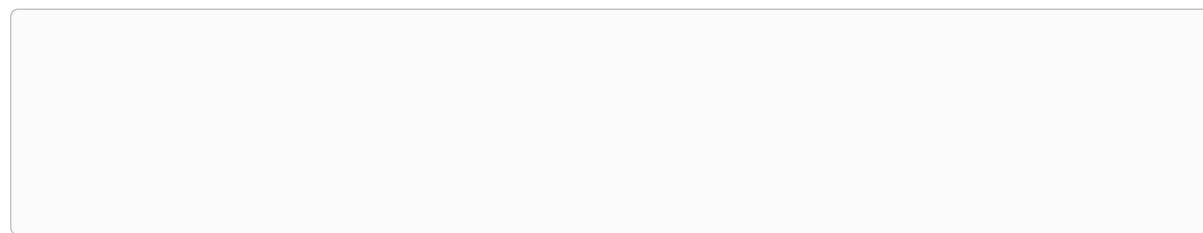
(a) Find the **horizontal** and **vertical** components of this velocity. [2]

(b) Air resistance is negligible. State which component stays **constant** during the flight, and why. [2]

3.5 Two forces, each 7.0 N, act at a point with 80° between them. Find the **magnitude**

of the resultant.

[2]



4 Go further

You are now ready for the real exam questions on this subtopic. Open the **1.4 Scalars and vectors** past-paper sheet in the Library, or try these in **Practice mode**:

- 9702/11 N25 —Q1 (which quantity is a vector?)
- 9702/11 N25 —Q4 (direction of a vector sum and difference)
- 9702/24 N25 —Q1 (resolve a velocity into components —part a)
- 9702/22 J25 —Q1 (classify quantities as scalar or vector —part a)

Solutions

2.1 distance scalar; force vector; temperature scalar; velocity vector; power scalar; acceleration vector.

2.2 $|\vec{R}| = \sqrt{3.0^2 + 4.0^2} = \sqrt{25} = 5.0 \text{ N}.$

2.3 Horizontal = $50 \cos 30^\circ = 43 \text{ N}$; vertical = $50 \sin 30^\circ = 25 \text{ N}.$

2.4 $v_H = 20 \cos 60^\circ = 10 \text{ m s}^{-1}$; $v_V = 20 \sin 60^\circ = 17 \text{ m s}^{-1}.$

2.5 $R = \sqrt{5.0^2 + 5.0^2} = 7.1 \text{ N}$ (or $2F \cos 45^\circ = 2(5.0)(0.707) = 7.1 \text{ N}$).

3.1 C —displacement.

3.2 A — $\vec{X} + \vec{Y}$ points north-east; reversing $\vec{Y}$ (now south) gives $\vec{X} - \vec{Y}$ pointing south-east.

3.3 B — $\sqrt{6.0^2 + 8.0^2} = \sqrt{100} = 10 \text{ N}.$

3.4 (a) Horizontal = $15 \cos 40^\circ = 11 \text{ m s}^{-1}$; vertical = $15 \sin 40^\circ = 9.6 \text{ m s}^{-1}.$

(b) The **horizontal** component stays constant, because with no air resistance there is no horizontal force, so no horizontal acceleration.

3.5 $2\alpha = 80^\circ$, so $\alpha = 40^\circ$: $R = 2F \cos \alpha = 2(7.0) \cos 40^\circ = 10.7 \text{ N}.$