

1.1 Physical quantities

Name: _____ Class: _____ Date: _____ **Total: 11 marks**

KEY WORDS physical quantities 物理量 • magnitude 大小 • unit 单位
• order of magnitude 数量级 • derived quantity 导出量

Objective

Build the skills to answer exam questions on **physical quantities** 物理量 — magnitude and unit, and making sensible estimates.

You must be able to:

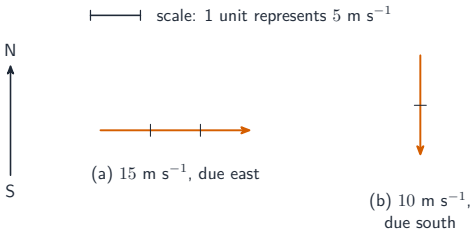
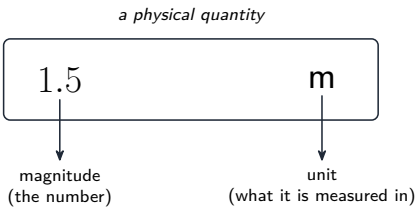
- state that every physical quantity has a **magnitude** 大小 and a **unit** 单位
- make reasonable **estimates** 估算 of common quantities
- give an answer to the right **order of magnitude** 数量级 (power of ten)

1 Worked examples

Study these first. Each one shows the method for a question type used later — follow the steps and you can do the Practice and Exam-style questions yourself.

■ Magnitude and unit

A physical quantity needs **both** a number and a unit. “The length is 1.5” means nothing; “the length is 1.5 m” is complete:



Quantities are scalars or vectors

■ Making estimates

Learn these rough values so you can check whether an answer is sensible:

quantity	estimate
mass of an adult	~ 70 kg
height of an adult	~ 1.7 m
mass of an apple	~ 0.1 kg (weight ≈ 1 N)
speed of sound in air	~ 340 m s ⁻¹
speed of light (vacuum)	3.0 × 10 ⁸ m s ⁻¹
free-fall acceleration	g ≈ 9.81 m s ⁻²

■ Order of magnitude

The **order of magnitude** is the nearest power of ten. A good estimate has the right power of ten: an adult’s mass is ~ 10² kg (70 kg), **not** 10¹ kg (7 kg). To estimate the seconds in a day, keep the units so they cancel:

$$24 \text{ h} \times \frac{60 \text{ min}}{1 \text{ h}} \times \frac{60 \text{ s}}{1 \text{ min}} = 86\,400 \text{ s} \approx 9 \times 10^4 \text{ s},$$

so the order of magnitude is 10⁵ s.

■ Estimating a derived quantity

Combine sensible estimates. The **pressure** a standing person exerts on the floor: weight ≈ 700 N, area of two feet ≈ 0.02 m². Substitute with the units still attached:

$$p = \frac{F}{A} \approx \frac{700 \text{ N}}{0.02 \text{ m}^2} = 3.5 \times 10^4 \text{ N m}^{-2} = 3.5 \times 10^4 \text{ Pa}.$$

2 Practice

Now apply the methods above.

2.1 A student writes “the mass is 60”. State what is **missing** to make it a physical quantity. [1]

2.2 Estimate the **mass of an apple**, giving a unit. [1]

2.3 State the **order of magnitude** of the speed of light in a vacuum, in m s^{-1} . [1]

2.4 Estimate the **height of a typical room** (floor to ceiling), giving a unit. [1]

3 Exam-style questions

3.1 What must all physical quantities have? [1]

- **A** a direction and a magnitude
- **B** a direction and a unit
- **C** a magnitude and a prefix
- **D** a magnitude and a unit

3.2 Which is the best estimate of the **mass of an adult human**? [1]

- **A** 7 kg
- **B** 70 kg
- **C** 700 kg
- **D** 7000 kg

3.3 Estimate the number of **seconds in one day**. Give your answer to an **order of magnitude**. [2]

3.4 A car travels at about 30 m s^{-1} . Estimate the time it takes to travel 1 km, and state the **order of magnitude** of that time in seconds. [2]

3.5 A person of weight 700 N stands on both feet, total contact area about 0.02 m^2 . Which is the best estimate of the pressure on the floor? [1]

- **A** $1.4 \times 10^4 \text{ Pa}$
- **B** $3.5 \times 10^4 \text{ Pa}$
- **C** $3.5 \times 10^6 \text{ Pa}$
- **D** $1.4 \times 10^7 \text{ Pa}$

Solutions

Each answer shows the steps, then the **result**.

2.1

- “the mass is 60” gives a magnitude only
- a physical quantity also needs a **unit** — e.g. 60 kg

2.2

- an apple is about 100 g (from the estimate table)
- $1\text{ g} = 10^{-3}\text{ kg}$, so $100\text{ g} = 100 \times 10^{-3}\text{ kg} = \mathbf{0.1\text{ kg}}$
- any value $\sim 0.05\text{--}0.2\text{ kg}$ with a unit is accepted

2.3

- speed of light $= 3.0 \times 10^8\text{ m s}^{-1}$
- write as $a \times 10^n$ with $1 \leq a < 10$: here $3.0 \times 10^8\text{ m s}^{-1}$
- coefficient 3.0 is nearer 1 than 10, so the order of magnitude is $\mathbf{10^8\text{ m s}^{-1}}$

2.4

- an adult is about 1.7 m tall, so a room is a little taller: $\mathbf{2.5\text{ m}}$
- any value $\sim 2\text{--}3\text{ m}$ with a unit is accepted

3.1 D

- every physical quantity has a **magnitude** and a **unit**
- “1.5” is not a length; “1.5 m” is
- **A** and **B** add a direction — that describes a *vector*, not every quantity
- **C** a prefix (k, m, μ) is not a unit

3.2 B

- the estimate table gives an adult’s mass $\sim 70\text{ kg}$
- **A** 7 kg is a cat; **C** 700 kg a horse; **D** 7000 kg a truck

3.3

- 1 day $= 24\text{ h}$; keep the units so they cancel

$$24\text{ h} \times \frac{60\text{ min}}{1\text{ h}} \times \frac{60\text{ s}}{1\text{ min}} = 86\,400\text{ s}$$

- $86\,400\text{ s} = 8.64 \times 10^4\text{ s} \approx 9 \times 10^4\text{ s}$ (1 s.f.)
- leading digit $9 \geq 5$, so round up: order of magnitude $\mathbf{10^5\text{ s}}$

3.4

- $s = 1\text{ km} = 1000\text{ m}$, $v = 30\text{ m s}^{-1}$

$$t = \frac{s}{v} = \frac{1000\text{ m}}{30\text{ m s}^{-1}} \approx 33\text{ s}$$

- $33\text{ s} = 3.3 \times 10^1\text{ s} \approx 3 \times 10^1\text{ s}$ (1 s.f.)
- leading digit $3 < 5$, so order of magnitude $\mathbf{10^1\text{ s}}$

3.5 B

$$p = \frac{F}{A} = \frac{700\text{ N}}{0.02\text{ m}^2} = 3.5 \times 10^4\text{ N m}^{-2} = \mathbf{3.5 \times 10^4\text{ Pa}}$$

- **A** is too small (wrong A , or $F \times A$)
- **C** and **D** are far too large (area probably left in cm^2)