

Exercise walk-through

8.4

The diffraction grating

A-Level Physics

8.4 The diffraction grating

Name: _____ Class: _____ Date: _____ **Total: 23 marks**

KEY WORDS diffraction grating • wavelength • diffraction • normal
• order

Objective

Build the skills to answer exam questions on the **diffraction grating** .

You must be able to:

- use $d \sin \theta = n\lambda$ in **both** directions (find an angle; find the grating)
- find the slit spacing from **lines per mm** and the **highest order**
- describe using a grating to measure **wavelength**

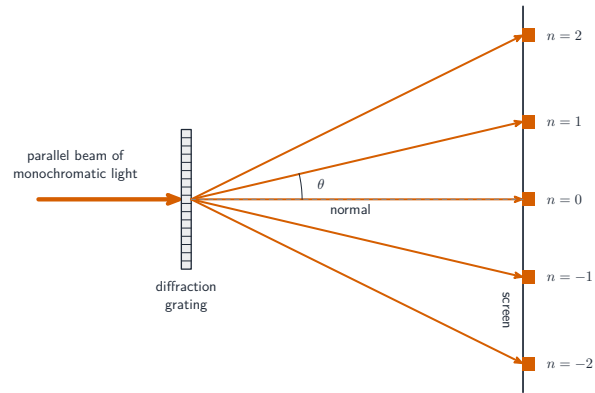
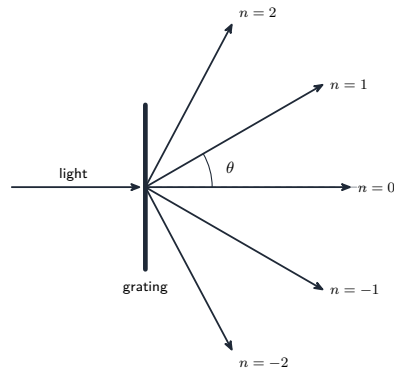
1 Key knowledge and worked examples

Study these first. Each one shows the method for a question type used later – follow the steps and you can do the Practice and Exam-style questions yourself.

■ The grating equation

A grating has many equally spaced slits, slit spacing d . Bright maxima (orders n) appear where

$$d \sin \theta = n\lambda.$$



A diffraction grating spreads the orders

Worked example (find the angle). 500 lines/mm, $\lambda = 600$ nm, first order:

- line spacing: $d = \frac{1}{N} = \frac{1}{500} \text{ mm} = 2.0 \times 10^{-6} \text{ m}$
- angle: $\sin \theta = \frac{n\lambda}{d} = \frac{600 \times 10^{-9}}{2.0 \times 10^{-6}} = 0.30$, so $\theta \approx 17^\circ$

■ Working backwards – find the grating

Exam questions often **give** an order's angle and ask for the grating. Rearrange to

$$d = \frac{n\lambda}{\sin \theta}, \text{ then } \mathbf{\text{lines per mm}} = \frac{1}{d \text{ (in mm)}}.$$

Worked example. The **second-order** ($n = 2$) maximum for $\lambda = 730 \text{ nm}$ is at $\theta = 35^\circ$.

- spacing: $d = \frac{n\lambda}{\sin \theta} = \frac{2 \times 730 \times 10^{-9}}{\sin 35^\circ} = 2.55 \times 10^{-6} \text{ m} = 2.55 \times 10^{-3} \text{ mm}$
- **lines per mm:** $N = \frac{1}{d} = \frac{1}{2.55 \times 10^{-3} \text{ mm}} \approx 390$

■ Slit spacing and highest order

N lines per mm $\rightarrow d = 10^{-3}/N \text{ m}$. Since $\sin \theta \leq 1$, the **highest order** is $n_{\max} = \lfloor d/\lambda \rfloor$.

■ Finding wavelength

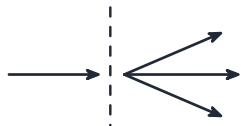
Shine parallel light normally on the grating, measure θ_1 for the first order, then $\lambda = d \sin \theta_1$. A grating gives **sharper** maxima than a double slit (many slits add).

■ Key knowledge: paired orders, overlap and graphs

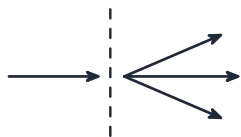
- Angle between the $+n$ and $-n$ beams is $2\theta_n$. Halve it before using $d \sin \theta_n = n\lambda$.
- Orders of different wavelengths overlap when $n_1\lambda_1 = n_2\lambda_2$.
- A graph of $\sin \theta$ against n has gradient $G = \lambda/d$, so $d = \lambda/G$. Convert spacing to metres before finding lines/mm: $N = 10^3/d$.
- For a screen perpendicular to the central ray at distance L , an order at displacement y has $\tan \theta = y/L$; do not use the double-slit fringe-spacing formula for a grating.

Exercises 2.1·2.2

2.1 State what d represents in $d \sin \theta = n\lambda$. [1]



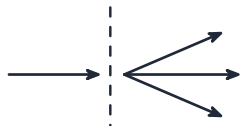
2.2 A grating has 500 lines per mm. Find the slit spacing d in metres. [2]



500 lines mm^{-1}

Exercises 2.1·2.2

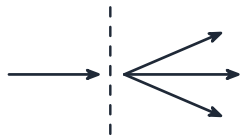
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2.1

- the **slit spacing** – the centre-to-centre distance between adjacent slits

2.2 A grating has 500 lines per mm. Find the slit spacing d in metres. [2]



500 lines mm^{-1}

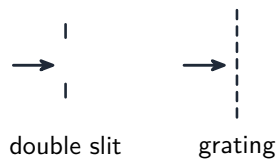
2.2

- $d = 1/N$ per millimetre

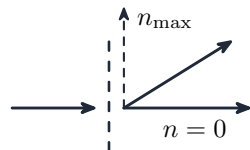
$$d = \frac{1}{N} = \frac{1.0 \times 10^{-3} \text{ m}}{500} = \mathbf{2.0 \times 10^{-6} \text{ m}}$$

Exercises 2.3·2.4

2.3 State **one** reason a grating gives **sharper** maxima than a double slit. [1]

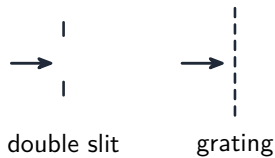


2.4 Write the formula for the **highest order** observable. [1]



Exercises 2.3·2.4

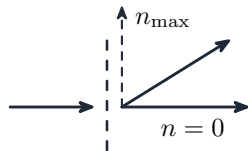
2.3 State **one** reason a grating gives **sharper** maxima than a double slit. [1]



2.3

- many slits contribute, so the maxima are **sharper** / **brighter** and other directions are more completely cancelled

2.4 Write the formula for the **highest order** observable. [1]



2.4

- $n_{\max} = \lfloor d/\lambda \rfloor$ – the largest integer with $\sin \theta \leq 1$

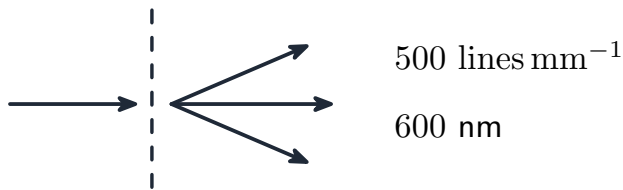
Exercise 3.1

3.1 A grating with 500 lines per mm is illuminated normally by light of wavelength 600 nm. Calculate the angle of the **first-order** maximum. [3]



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3.1

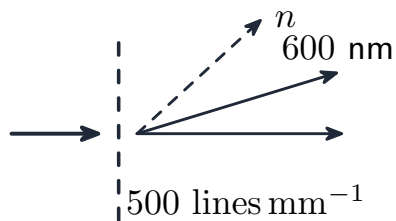
- $d = 2.0 \times 10^{-6} \text{ m}$

$$\sin \theta = \frac{n\lambda}{d} = \frac{(1)(600 \times 10^{-9} \text{ m})}{2.0 \times 10^{-6} \text{ m}} = 0.30$$

- $\theta = 17^\circ$

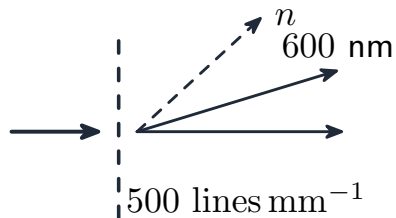
Exercise 3.2

3.2 For the same grating and wavelength, calculate the **highest order** that can be seen. [2]



Exercise 3.2

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3.2

$$\frac{d}{\lambda} = \frac{2.0 \times 10^{-6} \text{ m}}{600 \times 10^{-9} \text{ m}} = 3.33$$

- highest order $n = \mathbf{3}$ ($n = 4$ needs $\sin \theta > 1$)

Exercise 3.3

3.3 A grating has 600 lines per mm. Light of wavelength 590 nm is incident normally on it. **Determine** the highest order of maximum that can be observed, and **explain** what limits it. [4]



Exercise 3.3

3.3 A grating has 600 lines per mm. Light of wavelength 590 nm is incident normally on it. **Determine** the highest order of maximum that can be observed, and **explain** what limits it. [4]



3.3

$$d = \frac{1}{N} = \frac{1.0 \times 10^{-3} \text{ m}}{600} = 1.67 \times 10^{-6} \text{ m}$$

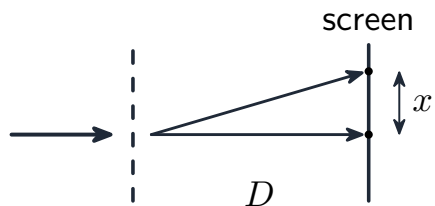
- largest angle is 90° , where $\sin \theta = 1$

$$n_{\max} = \frac{d}{\lambda} = \frac{1.67 \times 10^{-6} \text{ m}}{590 \times 10^{-9} \text{ m}} = 2.8$$

- an order must be a whole number and $\sin \theta$ cannot exceed 1, so the highest observed is the **2nd order**

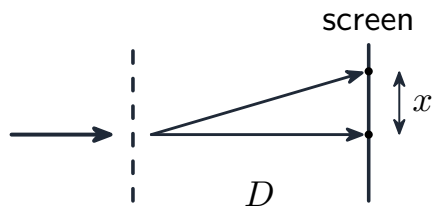
Exercise 3.4

3.4 Describe how a diffraction grating can be used to **measure the wavelength** of light. [3]



Exercise 3.4

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3.4

- shine **parallel monochromatic** light normally on the grating
- measure the **angle** θ of a known order n from the straight-through beam
- calculate $\lambda = d \sin \theta / n$

Exercise 3.5

3.5 A grating with **more** lines per mm (smaller d) is used. The diffraction angles become: [1]

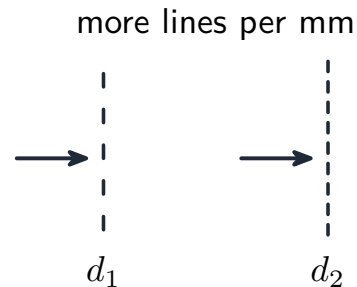
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A smaller

B larger

C unchanged

D zero



Exercise 3.5

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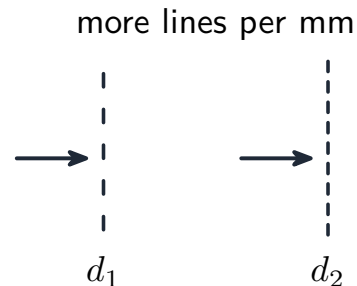
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A smaller

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D zero

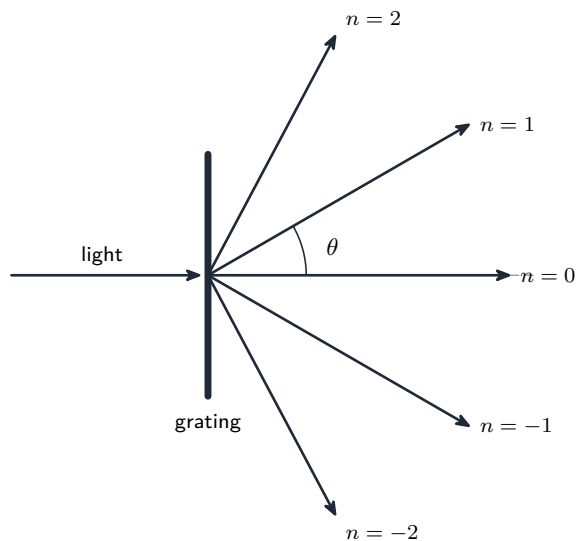


3.5 B

- more lines per mm $\Rightarrow$ smaller $d \Rightarrow$ larger $\sin \theta$ for each order $\Rightarrow$ **larger** angle

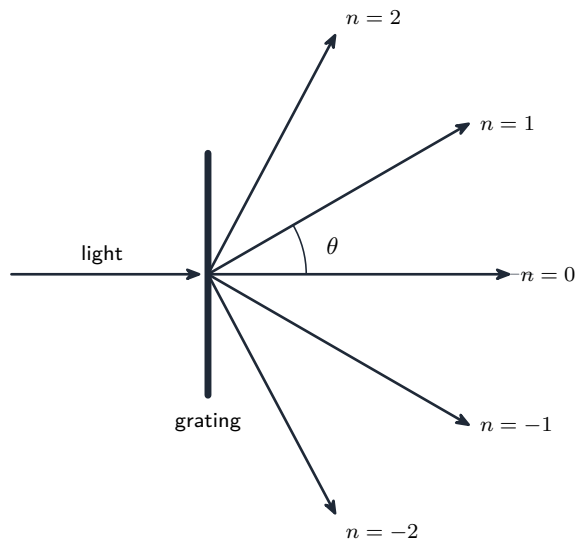
Exercise 3.6

3.6 A grating gives second-order beams separated by 60° for 600 nm light. Find the slit spacing and lines per mm. At the same angle, what order is produced by 400 nm light?[5]



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3.6

- $\theta = 60^\circ / 2 = 30^\circ$.
- $d = n\lambda / \sin \theta = 2 \times 600 \times 10^{-9} / \sin 30^\circ = 2.40 \times 10^{-6} \text{ m}$.

Full solution on next slide

Full solution 3.6

3.6

- $\theta = 60^\circ/2 = 30^\circ$.
- $d = n\lambda/\sin\theta = 2 \times 600 \times 10^{-9}/\sin 30^\circ = 2.40 \times 10^{-6} \text{ m}$.
- $N = 10^{-3}/d = 10^{-3}/(2.40 \times 10^{-6}) = 417 \text{ lines/mm}$.
- $n_2 = n_1\lambda_1/\lambda_2 = 2 \times 600/400 = 3$: third order.