

1(a)

$$4k + k + 4k + 9k = 1, k = \frac{1}{18}$$

x	-2	1	2	3
$P(X = x)$	$\frac{4}{18}$	$\frac{1}{18}$	$\frac{4}{18}$	$\frac{9}{18}$

1(b)

$$[E(X) = 28k =] \frac{14}{9}, 1.56$$

1(c)

$$P(X \neq 2 | X > 0) = \frac{\frac{10}{18}}{\frac{14}{18}}$$

$$= \frac{5}{7}, 0.714$$

2(a)	$\left[\frac{1}{6} \left(\frac{5}{6} \right)^7 = \right] 0.0465$
2(b)	$\left(\frac{5}{6} \right)^4 \left(\frac{1}{6} \right)^3 \times {}^6C_2$
	0.0335
3(a)	Median = [\$]32400
	[IQR = \$]33500 – [\$]31300
	= [\$]2200

3(b)

$$[\text{Mean} =] \frac{878.3 + 896.5}{54} [= 32.867]$$

so [\$]32900

$$[\text{Variance} =] \left[\frac{28616.09 + 29815.63}{54} - \left(\frac{1774.8}{54} \right)^2 = \right]$$

$$\frac{58431.72}{54} - \left(\frac{1774.8}{54} \right)^2$$

$$= 1.8511$$

$$\sigma = 1.36, \text{ so } \sigma = [\text{\$}]1360$$

6(a)

$$P\left(\frac{148-155}{6} < Z < \frac{160-155}{6}\right)$$

$$\begin{aligned} & [= P(-1.1667 < Z < 0.8333) \\ & = \Phi(1.1667) + \Phi(0.8333) - 1] \\ & = 0.7975 + 0.8784 - 1 \\ & \text{Or } (0.7975 - 0.5) + (0.8784 - 0.5) \\ & \text{Or } 0.2975 + 0.3784 \end{aligned}$$

$$= 0.6759$$

$$[\text{Expected number} = 0.6759 \times 350 = 236.565]$$

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6(b)

$$\frac{114 - \mu}{\sigma} = 1.406$$

$$\frac{99.5 - \mu}{\sigma} = -0.842$$

Solve, obtaining values for μ and σ

$$\mu = 105, \sigma = 6.45$$

7(a)

$$\left[\frac{10!}{2!2!3!} = \right] 151200$$

7(b)

Method 1[SC_ S _ _ _ _ _]

$$\frac{7!}{2!3!} \times 2 \times 7$$

$$= 5880$$

Method 2 Considering each case separately [SC-S, S-CS]

$$\text{With Y } \frac{6!}{2!3!} \times 2 \times 7 = 840$$

$$\text{With H } \frac{6!}{2!3!} \times 2 \times 7 = 840$$

$$\text{With E } \frac{6!}{2!2!} \times 2 \times 7 = 2520$$

$$\text{With L } \frac{6!}{3!} \times 2 \times 7 = 1680$$

$$840 + 840 + 2520 + 1680$$

$$= 5880$$

7(b)	Method 3 Considering each case separately [SC-S, S-CS]
	$\text{SCYS } \frac{7!}{2!3!} \times 2 = 840$ $\text{SCHS } \frac{7!}{2!3!} \times 2 = 840$ $\text{SCES } \frac{7!}{2!2!} \times 2 = 2520$ $\text{SCLS } \frac{7!}{3!} \times 2 = 1680$
	$840 + 840 + 2520 + 1680$
	$= 5880$
7(c)	Method 1 Total arrangements with Ss at ends – arrangements with
	$\frac{8!}{2!3!} - \frac{6!}{2!}$ $[= 3360 - 360]$
	$= 3000$

7(d)

Method 1[Number of ways with 3 Es =] ${}^7C_2 (= 21)$ [Total number of ways is] ${}^{10}C_5 (= 252)$ [Probability =] $\frac{21}{252}, \frac{1}{12}$ **Method 2**

$$\frac{3}{11} \times \frac{2}{6} \times \frac{3}{11} \times {}^5C_2$$

[Probability =] $\frac{21}{252}, \frac{1}{12}$