

6(a)

$$P\left(\frac{148-155}{6} < Z < \frac{160-155}{6}\right)$$

$$\begin{aligned} & [= P(-1.1667 < Z < 0.8333) \\ & = \Phi(1.1667) + \Phi(0.8333) - 1] \\ & = 0.7975 + 0.8784 - 1 \\ & \text{Or } (0.7975 - 0.5) + (0.8784 - 0.5) \\ & \text{Or } 0.2975 + 0.3784 \end{aligned}$$

$$= 0.6759$$

$$[\text{Expected number} = 0.6759 \times 350 = 236.565]$$

236

6(b)

$$\frac{114 - \mu}{\sigma} = 1.406$$

$$\frac{99.5 - \mu}{\sigma} = -0.842$$

Solve, obtaining values for μ and σ

$$\mu = 105, \sigma = 6.45$$

3(a)

$$P\left(\frac{182.4 - 187.4}{6.4} < Z < \frac{192.4 - 187.4}{6.4}\right)$$

$$[= P(-0.78125 < Z < 0.78125) = 2\Phi(0.7813) - 1]$$

$$= 2 \times 0.7826 - 1$$

$$\text{Or } 0.7826 - (1 - 0.7826)$$

$$\text{Or } 0.7826 - 0.2174$$

$$\text{Or } (0.7826 - 0.5) + (0.7826 - 0.5)$$

$$\text{Or } 2 \times 0.2826$$

$$0.5652$$

$$[\text{Expected number} = 124 \times 0.5652 = 70.08,]$$

$$70$$

3(b)

$$[P(X < 170.3) = 0.23, \quad P(Z > \frac{170.3 - 172.7}{\sigma}) = 0.77]$$

$$\frac{170.3 - 172.7}{\sigma} = -0.739$$

or

$$\frac{172.7 - 170.3}{\sigma} = 0.739$$

$$\sigma = 3.25$$

6(a)

$$[\left(\frac{5}{7}\right)^{10} =] 0.0346, \frac{9765625}{282475249}$$

6(b)

Method 1

$$[P(0, 1, 2) =] {}^{10}C_2 \left(\frac{6}{7}\right)^8 \left(\frac{1}{7}\right)^2 + {}^{10}C_1 \left(\frac{6}{7}\right)^9 \left(\frac{1}{7}\right) + \left(\frac{6}{7}\right)^{10}$$

$$[= 0.2675729 + 0.3567639 + 0.2140583 =]$$

0.838

$$[P(0,1,2) =] 1 - \left\{ \left(\frac{1}{7}\right)^{10} + {}^{10}C_9 \left(\frac{6}{7}\right) \left(\frac{1}{7}\right)^9 + {}^{10}C_1 \left(\frac{6}{7}\right)^2 \left(\frac{1}{7}\right)^8 + {}^{10}C_1$$

$$\left(\frac{6}{7}\right)^3 \left(\frac{1}{7}\right)^7 + {}^{10}C_1 \left(\frac{6}{7}\right)^4 \left(\frac{1}{7}\right)^6 + {}^{10}C_1 \left(\frac{6}{7}\right)^5 \left(\frac{1}{7}\right)^5 + {}^{10}C_1$$

$$\left(\frac{6}{7}\right)^4 \left(\frac{1}{7}\right)^6 + {}^{10}C_1 \left(\frac{6}{7}\right)^3 \left(\frac{1}{7}\right)^7 \right\}$$

0.838

6(c)

$$[\text{Mean} = 392 \times \frac{1}{7} =] 56$$

$$[\text{Variance} = 392 \times \frac{1}{7} \times \frac{6}{7} =] 48$$

$$[P(X > 65) = P(Z > \frac{65.5 - 56}{\sqrt{48}})]$$

$$[= 1 - \Phi(1.3712)]$$

$$= 1 - 0.9149$$

$$= 0.0851 \text{ final answer}$$

1	$P\left(Z < \frac{1.48 - \mu}{0.14}\right) = 0.22$
	$\frac{1.48 - \mu}{0.14} = -0.772$
	$\mu = 1.59$