

7(a)

$$\left[\frac{10!}{2!2!3!} = \right] 151200$$

7(b)

Method 1[SC_ S _ _ _ _ _]

$$\frac{7!}{2!3!} \times 2 \times 7$$

$$= 5880$$

Method 2 Considering each case separately [SC-S, S-CS]

$$\text{With Y } \frac{6!}{2!3!} \times 2 \times 7 = 840$$

$$\text{With H } \frac{6!}{2!3!} \times 2 \times 7 = 840$$

$$\text{With E } \frac{6!}{2!2!} \times 2 \times 7 = 2520$$

$$\text{With L } \frac{6!}{3!} \times 2 \times 7 = 1680$$

$$840 + 840 + 2520 + 1680$$

$$= 5880$$

7(b)	Method 3 Considering each case separately [SC-S, S-CS]
	$\text{SCYS } \frac{7!}{2!3!} \times 2 = 840$ $\text{SCHS } \frac{7!}{2!3!} \times 2 = 840$ $\text{SCES } \frac{7!}{2!2!} \times 2 = 2520$ $\text{SCLS } \frac{7!}{3!} \times 2 = 1680$
	$840 + 840 + 2520 + 1680$
	$= 5880$
7(c)	Method 1 Total arrangements with Ss at ends – arrangements with
	$\frac{8!}{2!3!} - \frac{6!}{2!}$ $[= 3360 - 360]$
	$= 3000$

7(d)

Method 1[Number of ways with 3 Es =] ${}^7C_2 (= 21)$ [Total number of ways is] ${}^{10}C_5 (= 252)$ [Probability =] $\frac{21}{252}, \frac{1}{12}$ **Method 2**

$$\frac{3}{11} \times \frac{2}{6} \times \frac{3}{11} \times {}^5C_2$$

[Probability =] $\frac{21}{252}, \frac{1}{12}$

7(a)

Method 1 Total arrangements with 3 Os together – total arrangem

$$\frac{8!}{2!} - 7!$$

$$= 15120$$

Method 2 ^ ^ OOO ^ ^ ^ , Arrangements with OOOs together an

$$6! \times \frac{7 \times 6}{2}$$

$$= 15120$$

7(b)

Method 1 L _ _ _ _ _ L _ _ _ _

$$\frac{8!}{3!} \times 4$$

26880

Method 2

$${}^8P_5 \times \frac{4!}{3!}$$

26880

7(c)

Method 1 $1 - P(2 \text{ letters the same})$

$$1 - \left(\frac{3}{10} \times \frac{2}{9} + \frac{2}{10} \times \frac{1}{9} \right)$$

$$= \frac{41}{45}, 0.911$$

Method 2 $P(O \bar{O}) + P(L \bar{L}) + P(\bar{O} \bar{L})$

$$\frac{3}{10} \times \frac{7}{9} + \frac{2}{10} \times \frac{8}{9} + \frac{5}{10} \times \frac{9}{9}$$

$$= \frac{41}{45}, 0.911$$

7(c)

Method 3 Combination approach using OO and LL

$$[\text{Probability} =] 1 - \frac{{}^3C_2 + {}^2C_2}{{}^{10}C_2}$$

$$= \frac{41}{45}, 0.911$$

Method 4 Combinations with scenarios OL, OL̄, OL̄, OL̄

O and L	${}^3C_1 \times {}^2C_1$	[6]
O and not L	${}^3C_1 \times {}^5C_1$	[15]
Not O and L	${}^5C_1 \times {}^2C_1$	[10]
Not O and not L	5C_2	[10]

$$[\text{Probability} =] \frac{6 + 15 + 10 + 10}{{}^{10}C_2}$$

$$= \frac{41}{45}, 0.911$$

2(a)	Method 1 total arrangements with As together – arrangements with
	$\frac{7!}{2!} - 6!$
	$n - 6!$
	1800
	Method 2 arrangements of other 6 letters with the As together and th
	$5! \times \frac{6 \times 5}{2}$
	1800

2(b)	Method 1
	$[P(X < 6) =] 1 - \left(\frac{3}{4}\right)^5 [$
	$= 0.763, \frac{781}{1024}$
	Method 2
	$[P(X < 6) =] \frac{1}{4} + \left(\frac{1}{4}\right)\left(\frac{3}{4}\right) + \left(\frac{1}{4}\right)\left(\frac{3}{4}\right)^2 + \left(\frac{1}{4}\right)\left(\frac{3}{4}\right)^3 + \left(\frac{1}{4}\right)\left(\frac{3}{4}\right)^4$
2(c)	$= 0.763, \frac{781}{1024}$
2(c)	$\left(\frac{1}{4}\right)^2 \left(\frac{3}{4}\right)^4 \times 5 = \frac{405}{4096}$
	$= 0.0989$

5(a)	$3G\ 2P\ 1D: {}^9C_3 \times {}^6C_2 \times {}^5C_1 = 6300$ $4G\ 1P\ 1D: {}^9C_4 \times {}^6C_1 \times {}^5C_1 = 3780$ $5G\ 0P\ 1D: {}^9C_5 [\times {}^6C_0] \times {}^5C_1 = 630$ Condone ${}^5C_1 = 5$ and ${}^6C_1 = 6$
	Total: 10710
5(b)	Ways of selecting 1 st band: ${}^9C_3 \times {}^6C_1 \times {}^5C_1 = 2520$ Ways of selecting 2 nd band: ${}^6C_3 \times {}^5C_1 \times {}^4C_1 = 400$ Ways of selecting 3 rd band: $1 \times {}^4C_1 \times {}^3C_1 = 12$ [Total number of ways =] $2520 \times 400 \times 12 =$
	12096000