

7(a)	$v = \frac{1}{3}(2t^2 - 11t + 12) \Rightarrow \frac{dv}{dt} = \frac{1}{3}(4t - 11)$
	$\frac{1}{3}(4 \times 2 - 11) = -1 \text{ m s}^{-2}$
7(b)	Attempt to integrate
	$s = \frac{1}{3} \left(\frac{2t^3}{3} - \frac{11t^2}{2} + 12t \right) (+c)$
	[P changes direction when] $t = 1.5$
	Attempt to evaluate their $\frac{1}{3} \left(\frac{2t^3}{3} - \frac{11t^2}{2} + 12t \right)$ for $t = 0$ to $t = 1.5$ and $t = 1.5$ to $t = 3$
	Total distance is $\left[2.625 + -1.125 = \right] 3.75 \text{ m}$

7(c)

Attempt to evaluate their s for $t = 0$ to $t = 4$

$$\int_0^4 v \, dt = \frac{8}{9} > 0 \text{ so, no } P \text{ does not return to } O$$

1	Any method to find x , or a or getting an equation relating x and a For example: $\frac{x}{2} = 40$ or $x = 2 \times 40$ or $x = 40 \times 2 + \frac{1}{2}(0)2^2$ or $\frac{x-0}{4-6} = -40$ or $x = \frac{1}{2} \times a \times 4^2$
	$x = 80$
	$a = 10$
3(a)	$175 = \frac{1}{2}(15 + 20)t$
	Time = 10 s

3(b)(i)

$$\text{Change in KE} = \pm \left(\frac{1}{2} \times 1400 \times 20^2 - \frac{1}{2} \times 1400 \times 15^2 \right)$$

$$[= \pm (280000 - 157500) = \pm 122500]$$

$$\text{OR Work done against resistance} = \pm 800 \times 175 [= \pm 140000]$$

$$\text{Work done by engine} = \frac{1}{2} \times 1400 \times 20^2 - \frac{1}{2} \times 1400 \times 15^2 + 800 \times 175$$

$$\text{Av power} \times (\text{their } 10) = \frac{1}{2} \times 1400 \times 20^2 - \frac{1}{2} \times 1400 \times 15^2 + 800 \times 175$$

$$\text{Average power} = 26250 \text{ W}$$

Special case for using N2L Maximum 2 marks

$$20^2 = 15^2 + 2 \times a \times 175 \Rightarrow a = 0.5;$$

$$DF - 800 = 1400 \times 0.5 \Rightarrow DF = 1500$$

$$DF \times 175 = \text{Average power} \times (\text{their } 10) \Rightarrow \text{Average power} = 26250 \text{ W}$$

$$\text{OR } P = 1500 \times 15 = 22500 \text{ and } P = 1500 \times 20 = 30000 \text{ so}$$

$$\text{Average power} = \frac{1}{2} (22500 + 30000) = 26250 \text{ W}$$

3(b)(ii)

$$\text{their } 26250 = 800v$$

$$\text{Speed} = 32.8125 \text{ or } \frac{525}{16} \text{ m s}^{-1}$$

4(a)

$$[\text{Height gained by } P (s_P) =] 30t - \frac{1}{2}gt^2$$

$$[\text{Height lost by } Q (s_Q) =] 10t - \frac{1}{2}gt^2$$

$$\text{Meet when } 30t - \frac{1}{2}gt^2 = 10t - \frac{1}{2}gt^2 + 15$$

$$t = \frac{3}{4} \text{ or } 0.75$$

$$\text{Height} = 19.6875 \text{ m or } \frac{315}{16} \text{ m}$$

4(b)

$$[v_P =] \pm \left(30 - \frac{3}{4}g \right) [= \pm 22.5] \quad [v_Q =] \pm \left(10 - \frac{3}{4}g \right) [= \pm 2.5]$$

OR $[v_P =] \pm \sqrt{30^2 - 2g \times 19.6875} [= \pm 22.5]$

$$[v_Q =] \pm \sqrt{10^2 - 2g \times (19.6875 - 15)} [= \pm 2.5]$$

$$0.1 \times 22.5 + 0.4 \times 2.5 = (0.1 + 0.4) \times v_{PQ}$$

$$v_{PQ} = 6.5$$

$$v^2 = \text{their } 6.5^2 + 2g \times \text{their } 19.6875$$

OR

$$0 = \text{their } 6.5^2 + 2(-g)s \Rightarrow s = 2.1125,$$

$$\text{height above ground} = 2.1125 + 19.6875 = 21.8$$

$$\text{hence } v^2 = 0^2 + 2g \times 21.8$$

$$\text{Speed} = 20.9 \text{ ms}^{-1} \text{ or } 2\sqrt{109} \text{ ms}^{-1}$$

6

$$\text{Acceleration} = 0 \text{ when } \left[2(t+1)^{-\frac{1}{2}} - 1 = 0 \Rightarrow (t+1)^{\frac{1}{2}} = 2 \right] t = 3$$

For attempt at integration of $(a=)2(t+1)^{-\frac{1}{2}} - 1$

$$[v=] \frac{2}{-\frac{1}{2}+1} (t+1)^{-\frac{1}{2}+1} - t[+c] = 4(t+1)^{\frac{1}{2}} - t[+c]$$

$$v=0 \text{ at } t=0 \Rightarrow c=-4 \left[\Rightarrow v = 4(t+1)^{\frac{1}{2}} - t - 4 \right]$$

Attempt to integrate *their* v , which has come from integration

$$[s=] \frac{4}{\frac{1}{2}+1} (t+1)^{\frac{1}{2}+1} - \frac{1}{1+1} t^{1+1} - 4t[+k] = \frac{8}{3} (t+1)^{\frac{3}{2}} - \frac{1}{2} t^2 - 4t[+k]$$

$$= \left(\frac{8}{3} \times 4^{\frac{3}{2}} - \frac{1}{2} \times 3^2 - 4 \times 3 \right) - \left(\frac{8}{3} - 0 - 0 \right)$$

OR evaluate k from using $s=0$ when $t=0$ **AND** substitute $t = \text{their } 3$

6

$$\text{Distance} = \frac{13}{6} \text{m or } 2.17 \text{m}$$

3(a)	Velocity at $t = 10$ is $8 \text{ [m s}^{-1}\text{]}$
	$\frac{1}{2} \times 8(T - 40) = 80$ OR $\frac{1}{2} \times 8 \times t = 80 \quad [\Rightarrow t = 20] \text{ and } T = \textit{their } t + 40$
	Total time = 60s
3(b)	Distance after 10s = 55m
	Distance after 40s = 295m

7(a)

For an attempt at differentiation

$$v = \frac{9}{2}t^{\frac{1}{2}} - 6$$

$$v = 0 \Rightarrow t = \frac{16}{9}$$

$$\left(3 \times 16^{\frac{3}{2}} - 6 \times 16 \right) - \left(3 \times \left(\frac{16}{9} \right)^{\frac{3}{2}} - 6 \times \frac{16}{9} \right) \left[= \frac{896}{9} \right]$$

$$\text{Or } \left(3 \times \left(\frac{16}{9} \right)^{\frac{3}{2}} - 6 \times \frac{16}{9} \right) - 0 \left[= -\frac{32}{9} \right]$$

$$\text{For both i.e. } F(16) - F\left(\text{their } \frac{16}{9}\right) - \left[F\left(\text{their } \frac{16}{9}\right) - [F(0)] \right]$$

$$\text{OR } F(16) - F\left(\text{their } \frac{16}{9}\right) + \left| F\left(\text{their } \frac{16}{9}\right) - [F(0)] \right|$$

$$\text{OR } F(16) - 2 \times F\left(\text{their } \frac{16}{9}\right)$$

$$\frac{928}{9} \text{ m}$$

7(b)	For integration
	$v = 0.8t - 0.3t^2 + 7.5$
	$v = -9.6 \Rightarrow 0.3t^2 - 0.8t - 17.1 = 0$
	$t = 9 \left[\text{or } -\frac{19}{3} \right]$
	$s = 0.4t^2 - 0.1t^3 + 7.5t (+c)$
	At $t = 9 s_X = 3 \times 9^{\frac{3}{2}} - 6 \times 9 = 27$
	At $t = 9 s_Y = 0.4 \times 9^2 - 0.1 \times 9^3 + 7.5 \times 9 = 27$