

4	Use correct product rule: $p \sin 4xe^{\sin 2x} + q \cos 2x \cos 4xe^{\sin 2x}$
	Obtain derivative $-4 \sin 4xe^{\sin 2x} + 2 \cos 2x \cos 4xe^{\sin 2x}$
	Equate derivative to zero and obtain an equation in one trig function
	Obtain $2 \sin^2 2x + 4 \sin 2x - 1 = 0$
	Obtain $x = 0.113$ and no other root

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State $\frac{dx}{dt} = 2t - \frac{2}{2t+1}$

Use correct quotient rule or correct product rule

Obtain $\frac{dy}{dt} = \frac{(2t+1) \cdot 1 - t(2)}{(2t+1)^2}$ oe

Use $\frac{dy}{dx} = \frac{dy}{dt} \div \frac{dx}{dt}$

Obtain answer $\frac{1}{2(2t+1)(2t-1)(t+1)}$

Obtain $x = \left(\frac{y}{1-2y}\right)^2 - \ln\left(\frac{2y}{1-2y} + 1\right)$

Use correct quotient rule to differentiate

Obtain $\frac{dx}{dy} = \left(\frac{2y}{1-2y}\right) \left(\frac{(1-2y) + 2y}{(1-2y)^2}\right) - \frac{2}{1-2y}$

$\frac{dy}{dx} = \frac{\left(1 - \frac{2t}{2t+1}\right)^3}{-2\left(1 - \frac{4t}{2t+1}\right)\left(1 - \frac{t}{2t+1}\right)} = \frac{1}{-2(2t+1)(1-2t)(t+1)}$

Obtain answer $\frac{1}{2(2t+1)(2t-1)(t+1)}$

4	At $(e, 3)$, $\tan t = 1$ or $t = \frac{\pi}{4}$
	$\frac{dx}{dt} = \sec^2 t \times e^{\tan t}$
	$\frac{dy}{dt} = 6 \tan t \times \sec^2 t$
	$\frac{dy}{dx} = \frac{6 \tan t \times \sec^2 t}{\sec^2 t \times e^{\tan t}} \left(= 6 \tan t \times e^{-\tan t} \right)$
	$y - 3 = \frac{6}{e}(x - e)$
	$y = \frac{6}{e}x - 3$
	Alternative Method for Question 4
	Correct cartesian form, e.g. $x = e^{\sqrt{\frac{y}{3}}}$ or $\ln x = \sqrt{\frac{y}{3}}$ or $y = 3(\ln x)^2$
	Differentiate function of a function
	Obtain $\frac{dx}{dy} = k \sqrt{\frac{e}{y}} e^{\sqrt{\frac{y}{3}}}$ or $\frac{dy}{dx} = k \times \frac{1}{x} \ln x$
4	Obtain $\frac{dx}{dy} = \frac{1}{6} \sqrt{\frac{3}{y}} e^{\sqrt{\frac{y}{3}}}$ or $\frac{dy}{dx} = 6 \times \frac{1}{x} \ln x$
	$y - 3 = \frac{6}{e}(x - e)$
4	$y = \frac{6}{e}x - 3$

11(a)	$\frac{d}{dx} \sqrt{\sin 2x} = \frac{2 \cos 2x}{2\sqrt{\sin 2x}}$ Accept $k \frac{\cos 2x}{\sqrt{\sin 2x}}$
	Use correct product rule
	Obtain correct derivative in any form
	Equate the derivative to zero and obtain a horizontal equation
	Use correct trig formulae to obtain an equation in one trig function
	Obtain $a = \frac{1}{6} \pi$
11(b)	Use $[\pi] \int y^2 dx$
	Use double angle formula to obtain a form that can be integrated directly, e.g. $\int \cos^2 x \sin 2x dx = \int 2 \cos^3 x \sin x dx$
	Obtain $-(\pi) \times \frac{1}{2} \cos^4 x$
	Use correct limits correctly
	Obtain final answer $\frac{1}{2} \pi$

11(a)	Differentiate $\cos^2 x$ to obtain $-2\sin x \cos x$
	Use correct product rule
	Obtain derivative $-10\sin 2x \sin x \cos x + 10\cos 2x \cos^2 x$
	Equate derivative to zero and obtain an equation in one trig function
	Obtain $3 \tan^2 x = 1$, $4 \sin^2 x = 1$ or $4 \cos^2 x = 3$ or $\cos 3x = 0$
	Obtain $x = \frac{1}{6}\pi$ only
	Alternative Method for the Question 11(a)
	Use double angle formula to obtain $y = 10\sin x \cos^3 x$
	Use correct product rule
	Obtain derivative $10\cos^4 x - 30\sin^2 x \cos^2 x$
	Equate derivative to zero and obtain an equation in one trig function
	Obtain $3 \tan^2 x = 1$, $4 \sin^2 x = 1$ or $4 \cos^2 x = 3$ or $\cos 3x = 0$
	Obtain $x = \frac{1}{6}\pi$ only

11(a)	Alternative Method 2 for the Question 11(a)
	Use double angle formula to obtain $y = \frac{5}{2} \sin 2x (\cos 2x + 1)$
	Use double angle formula to obtain $y = \frac{5}{4} \sin 4x + \frac{5}{2} \sin 2x$
	Obtain derivative $5 \cos 4x + 5 \cos 2x$
	Equate derivative to zero and obtain an equation in $\cos 2x$
	Obtain $\cos 2x = \frac{1}{2}$ only
	Obtain $x = \frac{1}{6} \pi$ only

11(b)	$\frac{du}{dx} = -\sin x$
	Reach an integral of the form $\int Au^3 du$
	Obtain $-10 \int u^3 du$
	Substitute correct limits correctly in an expression of the form Cu^4 or $C\cos^4 x$
	Obtain answer $\frac{15}{8}$ or 1.875