

6.1 The Poisson distribution

Name: _____ Class: _____ Date: _____ **Total: 13 marks**

KEY WORDS poisson distribution 泊松分布 • approximation 近似 • variance 方差

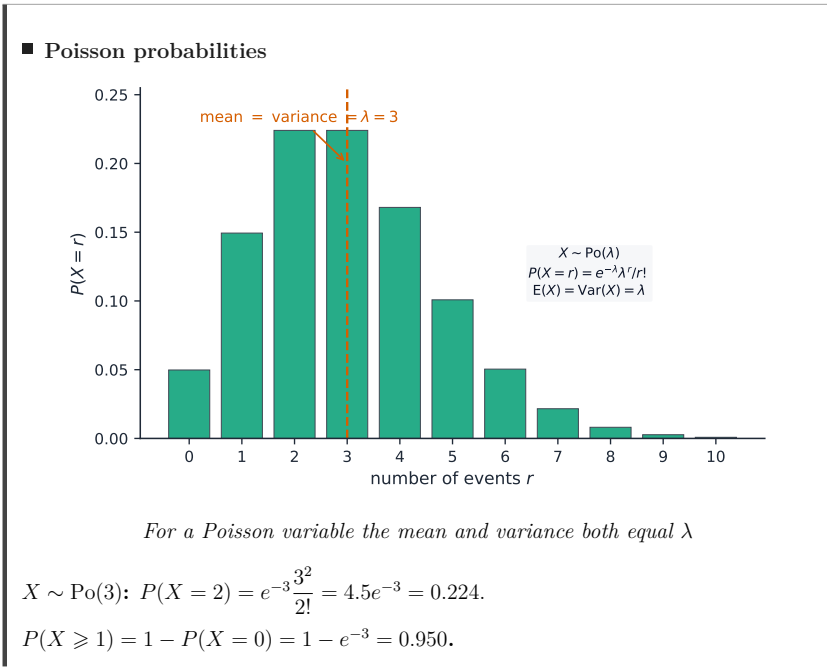
Objective

Build the skills to answer exam questions on the **Poisson distribution** 泊松分布 — using $Po(\lambda)$, adding Poisson variables, and the Poisson approximation to the binomial.

You must be able to:

- use $P(X = r) = e^{-\lambda} \frac{\lambda^r}{r!}$ (mean = variance = λ)
- combine independent Poisson variables (the sum is Poisson)
- use $Po(np)$ to approximate $B(n, p)$ when n large, p small

1 Worked examples



2 Practice

2.1 $X \sim Po(2)$. Find $P(X = 0)$. [2]

2.2 State the variance of $Po(4.5)$. [1]

3 Exam-style questions

3.1 For $X \sim Po(\lambda)$, the mean equals: [1]

- | | |
|---|---------------------|
| A | λ^2 |
| B | $\sqrt{\lambda}$ |
| C | λ |
| D | $\frac{1}{\lambda}$ |

3.2 Calls arrive at a switchboard at a mean rate of 1.5 per minute, as a Poisson process.

(a) Find the probability of exactly 2 calls in a given minute. [2]

(b) Find the probability of at least 1 call in a 2-minute period. [3]

3.3 A factory makes items with a 0.5% defect rate. A box holds 400 items. Using a Poisson approximation, find the probability that a box contains exactly 3 defective items. [4]