

2.2 Logarithmic and exponential functions

Name: _____ Class: _____ Date: _____

Total: 13 marks

KEY WORDS logarithmic and exponential functions 对数与指数函数

- laws of logarithms 对数定律 • logarithms 对数 • exponential function 指数函数
- linear form 线性形式

Objective

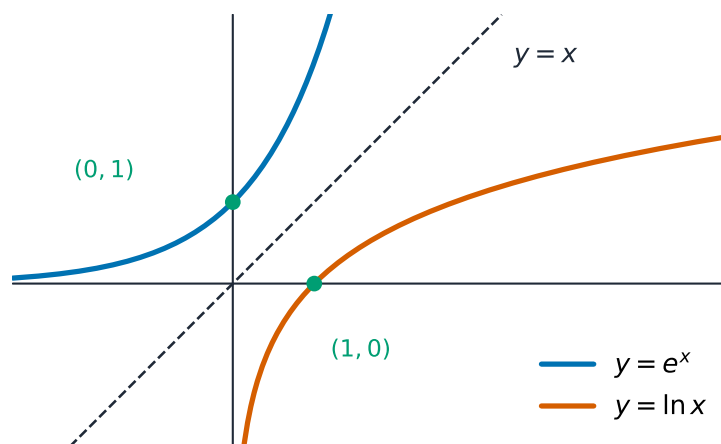
Build the skills to answer exam questions on **logarithmic and exponential functions** 对数与指数函数 — the laws of logs, solving equations with the unknown in the power, and reducing $y = Ax^n$ to **linear form** 线性形式.

You must be able to:

- use the laws of logarithms and $\ln/e^x$ as inverses
- solve equations such as $a^x = b$ by taking logs
- use a log–log (or log–linear) plot to find unknown constants

1 Worked examples

- Solving and linearising



ln and exp inverse · reflect in $y = x$

e^x and $\ln x$ undo each other, so each is the other reflected in $y = x$

Solve $4^x < 0.05$. $x \ln 4 < \ln 0.05 \Rightarrow x < \frac{\ln 0.05}{\ln 4} = -2.16$ (3 s.f.).

Linear form: $y = Ax^n \Rightarrow \ln y = \ln A + n \ln x$ — plot $\ln y$ against $\ln x$: gradient n , intercept $\ln A$.

2 Practice

2.1 Write $\log 12$ in terms of $\log 2$ and $\log 3$.

[2]

2.2 Solve $e^{2x} = 7$, giving x to 3 s.f.

[2]

3 Exam-style questions

3.1 The solution of $3^x = 20$ is $x =$ [1]

A	B
C	D

- A** $\frac{\ln 20}{\ln 3}$
B $\frac{\ln 3}{\ln 20}$
C $\ln \frac{20}{3}$
D $20 - 3$

3.2 Solve the equation $\ln(2x + 1) + \ln 3 = \ln(4x + 9)$. [3]

3.3 The variables x and y satisfy $y = Ax^n$. When $\ln y$ is plotted against $\ln x$, a straight line of gradient 1.5 passing through $(0, 2)$ is obtained.

(a) Find the values of n and A . [3]

(b) Find y when $x = 4$. [2]
