

1

$$T \cos \theta = mg$$

$$T \sin \theta = m\omega^2 r$$

$$\frac{5}{3}mg \sin \theta = m\omega^2 a \sin \theta$$

$$\omega = \sqrt{\frac{5g}{3a}}$$

4

|                    |                 |                    |                           |
|--------------------|-----------------|--------------------|---------------------------|
| Areas              | $2a^2$          | $\frac{1}{2}a(2a)$ | $2a^2 + \frac{1}{2}a(2a)$ |
| Distances from $D$ | $-\frac{1}{2}a$ | $\frac{2}{3}a$     | $\bar{x}$                 |

$$-2a^2\left(\frac{1}{2}a\right) + \frac{1}{2}(2a^2)\left(\frac{2}{3}a\right) = (3a^2)\bar{x}$$

$$m\left(\frac{1}{9}a\right) = km(2a)$$

$$k = \frac{1}{18}$$

**Alternative method for question 4**

|                 |        |                    |                              |
|-----------------|--------|--------------------|------------------------------|
| Ratio of masses | $2a^2$ | $\frac{1}{2}a(2a)$ | $k(2a^2 + \frac{1}{2}a(2a))$ |
|-----------------|--------|--------------------|------------------------------|

$$2\left(\frac{1}{2}a\right) = 1\left(\frac{2}{3}a\right) + 3k(2a)$$

$$k = \frac{1}{18}$$

1

Let  $v_A$  and  $v_B$  be the speeds of  $A$  and  $B$  respectively after the collision.

$$4mv_A + mv_B = 4mu$$

$$-v_A + v_B = eu$$

$$v_A = \frac{3}{4}u, \quad v_B = u$$

$$e = \frac{1}{4}$$

**Alternative method for question 1**Let  $v_A$  and  $v_B$  be the speeds of  $A$  and  $B$  respectively after the collision.

$$4mv_A + mv_B = 4mu$$

$$-v_A + v_B = eu$$

$$v_A = \frac{1}{5}u(4 - e), \quad v_B = \frac{4}{5}u(1 + e)$$

$$\frac{4m\left(\frac{1}{5}u(4 - e)\right)}{m\left(\frac{4}{5}u(1 + e)\right)} = 3, \quad e = \frac{1}{4}$$

2

$$\uparrow N_1 \cos \theta_1 = mg$$

$$\rightarrow N_1 \sin \theta_1 = m(r \sin \theta_1) \omega_1^2$$

$$\uparrow N_2 \cos \theta_2 = mg$$

$$\rightarrow N_2 \sin \theta_2 = m(r \sin \theta_2) \omega_2^2$$

$$\frac{\frac{5}{4}g}{\frac{5}{3}g} = \frac{r\omega_1^2}{r\omega_2^2}$$

$$\frac{\omega_1}{\omega_2} = \frac{1}{2}\sqrt{3}$$

1

$$T_A \cos 45^\circ + T_B \sin 45^\circ = m\omega^2 l \sin 45^\circ$$

$$T_A \sin 45^\circ - T_B \cos 45^\circ = mg$$

$$2T_A = m\omega^2 l + \sqrt{2}mg$$

$$T_A = \frac{1}{2}m(\omega^2 l + \sqrt{2}g)$$