

1	Let v_A and v_B be the speeds of A and B respectively after the collision. $4mv_A + mv_B = 4mu$
	$-v_A + v_B = eu$
	$v_A = \frac{3}{4}u, \quad v_B = u$
	$e = \frac{1}{4}$
	Alternative method for question 1
	Let v_A and v_B be the speeds of A and B respectively after the collision. $4mv_A + mv_B = 4mu$
	$-v_A + v_B = eu$
	$v_A = \frac{1}{5}u(4 - e), \quad v_B = \frac{4}{5}u(1 + e)$
	$\frac{4m\left(\frac{1}{5}u(4 - e)\right)}{m\left(\frac{4}{5}u(1 + e)\right)} = 3, \quad e = \frac{1}{4}$

5(a)	$u \sin \alpha = v \sin(2\alpha)$
	$v = \frac{5}{8}u$
5(b)	$m \cos \alpha = m v \cos(2\alpha) + k m w$
	$e u \cos \alpha = w - v \cos(2\alpha)$
	$\frac{5}{8k} = \frac{4}{5}e + \frac{5}{8} \times \frac{7}{25}$
	$e = \frac{25}{32k} - \frac{7}{32}$
5(c)	$0 \leq \frac{25}{32k} - \frac{7}{32} \leq 1$
	$7k \leq 25 \leq 39k$
	$\frac{25}{39} \leq k \leq \frac{25}{7}$

7	Perpendicular to the wall: $eu \sin \alpha = v \sin \theta$
	$P_1 P_2 = uT$ $P_2 P_3 = vkT$
	$\sin \alpha = \frac{d}{P_1 P_2} \quad \sin \theta = \frac{d}{P_2 P_3}$
	$\sin \alpha = \frac{d}{uT} \quad \sin \theta = \frac{d}{vkT}$
	$\frac{eud}{uT} = \frac{vd}{vkT}$
	$e = \frac{1}{k}$

6(a)	$\frac{9}{2} \times \frac{1}{2} \times 2mv_A^2 = \frac{1}{2}mv_B^2 \quad [3v_A = v_B]$
	$2mu = 2mv_A + mv_B$
	$[v_A = \frac{2}{5}u] \quad v_B = \frac{6}{5}u$
6(b)	Let w denote the speed after the second collision. Perpendicular to wall: $v_B \cos \alpha = w \cos \beta$
	Parallel to wall: $e v_B \sin \alpha = w \sin \beta$
	$e^2 v_B^2 \sin^2 \alpha = w^2 \sin^2 \beta \quad \left[\frac{576}{625} \sin^2 \alpha = \frac{144}{125} \sin^2 \beta \right]$ $v_B^2 \cos^2 \alpha = w^2 \cos^2 \beta \quad \left[\frac{36}{25} \cos^2 \alpha = \frac{144}{125} \cos^2 \beta \right]$
	$\frac{576}{625} \sin^2 \alpha + \frac{36}{25} (1 - \sin^2 \alpha) = \frac{144}{125}$
	$[\sin^2 \alpha = \frac{5}{9}] \quad \sin \alpha = \frac{1}{3} \sqrt{5}$
	$\sin(\alpha + \beta) = 1$

6(a)	Let v and w denote the horizontal components of the velocities for A and B respectively after the collision. $2mu \cos \theta - mu \cos \theta = mw + mv$
	$w - v = e(3u \cos \theta)$
	$w = \frac{1}{2}(3eu \cos \theta + u \cos \theta) \quad \left[= \frac{1}{2}(3e + 1)u \cos \theta \right]$
	$\frac{\frac{1}{2}(3e + 1)u \cos \theta}{u \sin \theta} = \tan \theta$
	$\tan^2 \theta = \frac{1}{2}(3e + 1)$
	$\tan \theta = \sqrt{\frac{1}{2}(3e + 1)}$
6(b)	$w = 3eu \cos \theta = u \cos \theta$ $e = \frac{1}{3}$
	$\tan \theta = 1, \quad \theta = 45^\circ$
	Alternative method for question 6(b)
	$v = 0, \quad w = u \cos \theta \quad \text{and} \quad \frac{w}{u \sin \theta} = \tan \theta$
	$u \cos \theta = u \sin \theta \tan \theta, \quad \tan^2 \theta = 1, \quad \theta = 45^\circ$